

Practical 3

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Part A

1. Importing Data and Creating a Markdown File

```
Practical3a <- read.csv(file="Data-Practical3a.csv", head=TRUE, sep=";")
head(Practical3a)
```

##	Student	teacher	group	Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	Q9	Q10	Q11	Q12	Q13	Q14	Q15	Q16
## 1	1	A	1A	10	5	5	7	4	2	4	14	5	5	5	0	5	0	0	4
## 2	2	A	1A	12	5	4	8	4	4	5	18	5	0	5	0	0	5	0	4
## 3	3	A	1A	10	4	5	6	2	3	0	8	0	5	5	0	5	0	0	4
## 4	4	A	1A	18	5	6	8	5	3	4	15	5	5	5	0	5	0	5	4
## 5	5	A	1B	20	5	6	7	5	4	4	19	5	5	5	0	5	0	0	5
## 6	6	A	1A	16	5	6	8	6	3	1	19	0	0	5	0	5	0	0	4
##	Q17	TOTAL	Grade																
## 1	12	87	6																
## 2	17	96	7																
## 3	11	68	5																
## 4	12	105	8																
## 5	13	108	8																
## 6	11	89	6																

```
Practical3a$TOTAL <- as.integer(Practical3a$TOTAL)
Practical3a$Student <- as.factor(Practical3a$Student)
Practical3a$teacher <- as.factor(Practical3a$teacher)
Practical3a$group <- as.factor(Practical3a$group)
str(Practical3a)
```

```
## 'data.frame':   130 obs. of  22 variables:
## $ Student: Factor w/ 130 levels "1","2","3","4",...: 1 2 3 4 5 6 7 8 9 10 ...
## $ teacher: Factor w/ 2 levels "A","B": 1 1 1 1 1 1 1 1 1 1 ...
## $ group   : Factor w/ 5 levels "1A","1B","1C",...: 1 1 1 1 2 1 1 1 1 1 ...
## $ Q1      : int   10 12 10 18 20 16 10 7 20 11 ...
## $ Q2      : int    5 5 4 5 5 5 3 4 4 5 ...
## $ Q3      : int    5 4 5 6 6 6 4 6 6 5 ...
## $ Q4      : int    7 8 6 8 7 8 8 6 6 7 ...
## $ Q5      : int    4 4 2 5 5 6 5 3 6 6 ...
## $ Q6      : int    2 4 3 3 4 3 3 2 3 3 ...
## $ Q7      : int    4 5 0 4 4 1 3 0 4 2 ...
## $ Q8      : int   14 18 8 15 19 19 16 14 17 17 ...
## $ Q9      : int    5 5 0 5 5 0 0 0 5 5 ...
## $ Q10     : int    5 0 5 5 5 0 5 0 5 5 ...
## $ Q11     : int    5 5 5 5 5 5 5 5 5 5 ...
## $ Q12     : int    0 0 0 0 0 0 5 0 0 0 ...
## $ Q13     : int    5 0 5 5 5 5 5 0 5 0 ...
## $ Q14     : int    0 5 0 0 0 0 0 0 0 0 ...
## $ Q15     : int    0 0 0 5 0 0 0 0 5 0 ...
## $ Q16     : num    4 4 4 4 5 4 2 5 4 4 ...
## $ Q17     : int   12 17 11 12 13 11 11 2 8 12 ...
## $ TOTAL   : int   87 96 68 105 108 89 85 54 103 87 ...
## $ Grade   : int    6 7 5 8 8 6 6 4 7 6 ...
```

2. Descriptives and Graphs for Groups

2a

```
install.packages("psych")
```

```
##
## The downloaded binary packages are in
## /var/folders/_6/4dcygrqd30z3yrk1v6121lt40000gn/T//RtmpePIGN2/downloaded_packages
```

```
library("psych")
G1A <- subset(Practical3a, group == "1A")
G1B <- subset(Practical3a, group == "1B")
G1C <- subset(Practical3a, group == "1C")
G1D <- subset(Practical3a, group == "1D")
G1E <- subset(Practical3a, group == "1E")
aggregate(TOTAL~group, Practical3a, max)
```

```
##      group TOTAL
## 1      1A   106
## 2      1B   119
## 3      1C    92
## 4      1D   116
## 5      1E   116
```

```
aggregate(TOTAL~group, Practical3a, min)
```

```
##      group TOTAL
## 1      1A    10
## 2      1B    22
## 3      1C    28
## 4      1D    22
## 5      1E    40
```

```
aggregate(TOTAL~group, Practical3a, mean)
```

```
##      group      TOTAL
## 1      1A 76.07692
## 2      1B 81.24242
## 3      1C 64.56522
## 4      1D 69.00000
## 5      1E 73.08333
```

```
aggregate(TOTAL~group, Practical3a, range)
```

```
##      group TOTAL.1 TOTAL.2
## 1      1A      10     106
## 2      1B      22     119
## 3      1C      28      92
## 4      1D      22     116
## 5      1E      40     116
```

```
aggregate(TOTAL~group, Practical3a, sd)
```

```
##      group      TOTAL
## 1      1A 21.60726
## 2      1B 21.82033
## 3      1C 18.70543
## 4      1D 27.21732
## 5      1E 24.01072
```

```
describe(Practical3a$TOTAL)
```

```
##      vars      n  mean      sd median trimmed      mad min max range  skew kurtosis      se
## X1      1 130 73.49 23.19      75      74.24 25.95  10 119   109 -0.28      -0.47 2.03
```

Table 1: Shows the Max, Min, Mean, Range, and Standard Deviation Proficiency Scores for the Students by Group

value	Overall	G1A	G1B	G1C	G1D	G1E
mean	73.5	76.1	81.2	64.6	69.0	73.1
max	119	106	119	92	116	116
min	10	10	22	28	22	40
range	109	96	97	64	94	76
sd	23.2	21.6	21.8	18.7	27.2	24.0

- 1. The Group 1B seems to have performed the best.
- 2. The Group 1C performed most homogeneously.

2b

```
aggregate(TOTAL~teacher,Practical3a,mean)
```

```
##      teacher      TOTAL
## 1          A 78.40000
## 2          B 69.28571
```

```
aggregate(TOTAL~teacher,Practical3a,sd)
```

```
##      teacher      TOTAL
## 1          A 21.95156
## 2          B 23.54960
```

Teacher A performed best as it scored more homogeneously (closer to the mean) and its mean is higher

than Teacher B.

2c

```
boxplot(TOTAL~teacher, data=Practical3a, main="TOTAL over Teachers", xlab="Teacher  
s", ylab="TOTAL")
```



Figure 1: Boxplot of Total Score over Teacher groups A&B

3. Checking for Normality

3a

```
hist(Practical3a$TOTAL, prob=TRUE, xlab="TOTAL")  
curve(dnorm(x, mean=mean(Practical3a$TOTAL), sd=sd(Practical3a$TOTAL)), add=TRUE)
```

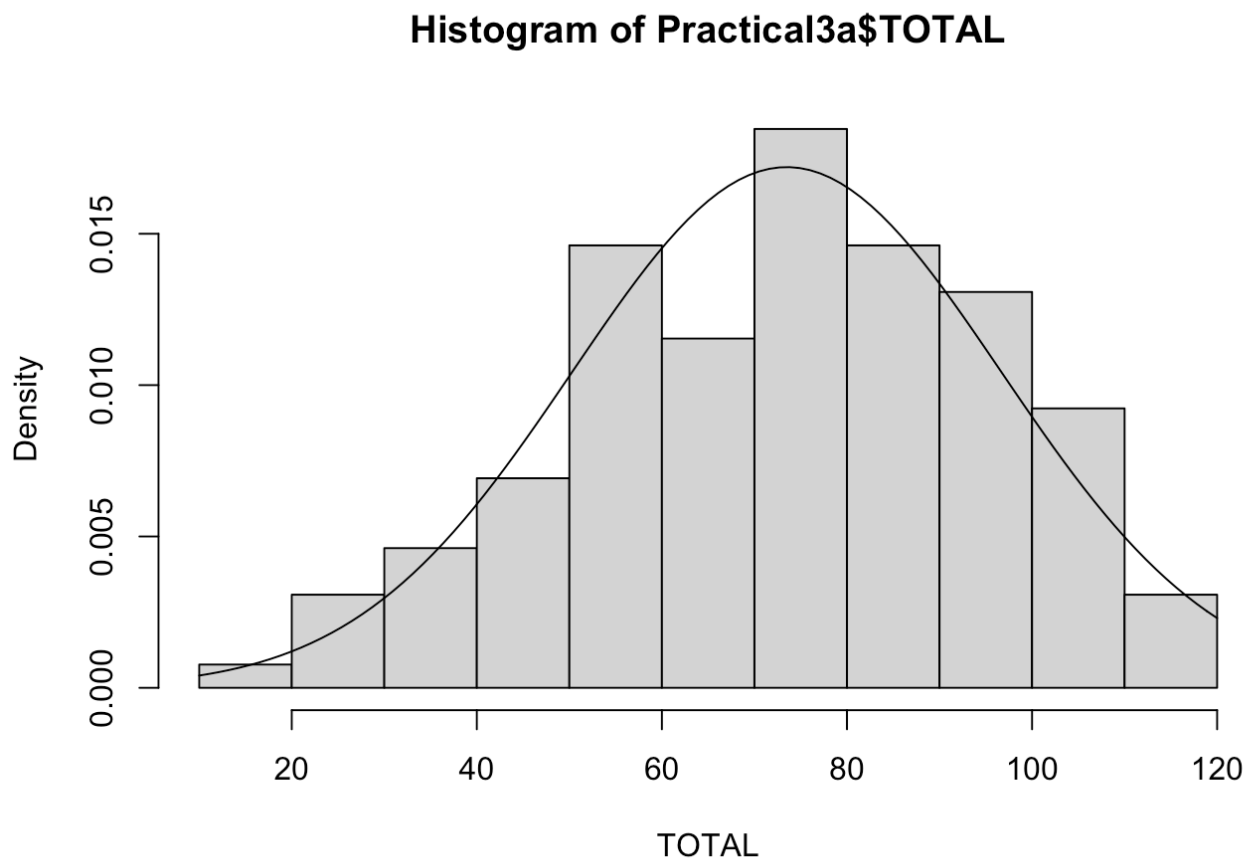


Figure 2: Histogram of Density over Total Score

3b

At face value when looking at the histogram, the results approximately follow the normal distribution although there are some clear outliers.

4. Using Z-Scores

```
scale(Practical3a$TOTAL, center = TRUE, scale = TRUE)
```

```
##           [,1]
## [1,] 0.58244822
## [2,] 0.97052591
## [3,] -0.23682690
## [4,] 1.35860360
## [5,] 1.48796283
## [6,] 0.66868771
## [7,] 0.49620874
## [8,] -0.84050330
## [9,] 1.27236412
## [10,] 0.58244822
## [11,] 0.71180745
## [12,] 0.79804694
## [13,] -1.31482048
## [14,] -2.73777201
## [15,] -0.58178484
## [16,] 0.88428643
## [17,] -0.71114407
## [18,] 0.02189156
## [19,] -0.58178484
## [20,] -0.02122818
## [21,] 1.40172335
## [22,] -0.06434792
## [23,] -0.53866510
## [24,] -0.02122818
## [25,] -0.02122818
## [26,] 0.19437054
## [27,] -0.71114407
## [28,] 0.66868771
## [29,] 0.49620874
## [30,] -0.40930587
## [31,] -0.75426382
## [32,] 1.44484309
## [33,] -1.74601791
## [34,] 0.92740617
## [35,] 0.10813105
## [36,] 0.45308899
## [37,] 0.19437054
## [38,] 0.10813105
## [39,] 0.79804694
## [40,] -0.92674279
## [41,] 0.79804694
## [42,] -0.27994664
## [43,] 1.91916027
## [44,] 1.96228001
## [45,] -2.22033509
## [46,] -0.40930587
```

```
## [47,] -1.22858099
## [48,]  0.40996925
## [49,]  0.19437054
## [50,]  0.53932848
## [51,]  1.22924437
## [52,]  0.23749028
## [53,]  0.88428643
## [54,] -1.96161663
## [55,]  1.09988514
## [56,] -0.06434792
## [57,]  0.66868771
## [58,] -0.45242561
## [59,]  0.84116668
## [60,]  0.15125079
## [61,]  0.71180745
## [62,]  0.06501131
## [63,] -0.19370715
## [64,]  0.32372976
## [65,]  0.06501131
## [66,] -1.09922176
## [67,]  0.23749028
## [68,] -1.83225740
## [69,]  0.79804694
## [70,]  0.23749028
## [71,] -1.22858099
## [72,] -0.49554536
## [73,] -1.83225740
## [74,] -0.36618613
## [75,] -0.27994664
## [76,] -0.53866510
## [77,] -0.02122818
## [78,] -2.00473637
## [79,] -0.02122818
## [80,] -1.27170074
## [81,] -2.22033509
## [82,] -0.75426382
## [83,]  0.49620874
## [84,] -1.01298228
## [85,]  0.49620874
## [86,] -0.15058741
## [87,]  0.62556797
## [88,] -0.88362305
## [89,]  1.83292078
## [90,]  0.92740617
## [91,]  1.57420232
## [92,] -1.74601791
## [93,]  1.48796283
```



```
## [94,] -0.32306638
## [95,] 0.92740617
## [96,] 1.22924437
## [97,] -0.88362305
## [98,] 0.53932848
## [99,] -0.53866510
## [100,] 0.84116668
## [101,] -1.35794022
## [102,] 0.28061002
## [103,] -0.92674279
## [104,] -1.27170074
## [105,] -0.27994664
## [106,] -0.58178484
## [107,] 0.49620874
## [108,] 0.10813105
## [109,] 1.35860360
## [110,] 1.44484309
## [111,] -0.10746767
## [112,] -0.71114407
## [113,] -0.75426382
## [114,] 1.14300489
## [115,] -1.22858099
## [116,] 0.97052591
## [117,] -0.92674279
## [118,] 1.83292078
## [119,] -0.06434792
## [120,] -0.75426382
## [121,] 1.40172335
## [122,] -0.75426382
## [123,] 0.06501131
## [124,] 1.14300489
## [125,] -0.79738356
## [126,] -1.44417971
## [127,] 0.53932848
## [128,] -0.96986253
## [129,] 1.14300489
## [130,] -1.44417971
## attr(,"scaled:center")
## [1] 73.49231
## attr(,"scaled:scale")
## [1] 23.19123
```

```
Practical3a$zscore <- scale(Practical3a$TOTAL, center = TRUE, scale = TRUE)
S11 <- subset(Practical3a, student = "11")
S33 <- subset(Practical3a, student = "33")
S44 <- subset(Practical3a, student = "44")
S55 <- subset(Practical3a, student = "55")
by = c("11", "33", "44", "55")
dataframe = subset(Practical3a, Student %in% by)
show(dataframe)
```

##	Student	teacher	group	Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	Q9	Q10	Q11	Q12	Q13	Q14	Q15	Q16	
##	11	11	A	1A	17	4	4	8	5	1	2	14	5	5	5	0	5	0	0	4
##	33	33	A	1B	3	4	0	5	2	2	0	11	0	0	0	0	0	0	0	2
##	44	44	A	1B	25	5	6	9	6	4	4	14	5	5	5	0	5	0	5	4
##	55	55	A	1B	14	5	6	7	6	4	2	11	0	5	5	5	5	0	5	4
##	Q17	TOTAL	Grade	zscore																
##	11	11	90	6	0.7118075															
##	33	4	33	2	-1.7460179															
##	44	17	119	9	1.9622800															
##	55	15	99	7	1.0998851															

Since the z-scores show how many standard deviations a student is away from the mean, Student 11 is 0.71 above the mean, Student 33 is 1.75 below the mean, Student 44 is 1.96 above the mean, and Student 55 is 1.10 above the mean.

5. Preparing for Inductive Statistics

5a

My first impression about the difference between the groups of the two teachers is that the group of Teacher A based on TOTAL performs better than the group of Teacher B.

5b

The null hypothesis belonging to the research question is that there is no significant difference between the total scores of the students of teacher A and the total scores of the students of teacher B.

5c

```
install.packages("pastecs")
```

```
##
## The downloaded binary packages are in
## /var/folders/_6/4dcygrqd30z3yrk1v6121lt40000gn/T//RtmpePIGN2/downloaded_packages
```

```
library("pastecs")
stat.desc(Practical3a$TOTAL, basic=FALSE, norm=TRUE)
```

```
##      median      mean      SE.mean CI.mean.0.95      var      std.dev
## 75.0000000 73.4923077 2.0340057 4.0243300 537.8332737 23.1912327
##   coef.var   skewness   skew.2SE   kurtosis   kurt.2SE  normtest.W
## 0.3155600 -0.2798097 -0.6586535 -0.4701042 -0.5573098 0.9865427
## normtest.p
## 0.2314139
```

```
by(Practical3a$TOTAL, Practical3a$teacher, stat.desc,
   basic=FALSE, norm=TRUE)
```

```
## Practical3a$teacher: A
##      median      mean      SE.mean CI.mean.0.95      var      std.dev
## 81.0000000 78.4000000 2.83393480 5.67069043 481.87118644 21.95156456
##   coef.var   skewness   skew.2SE   kurtosis   kurt.2SE  normtest.W
## 0.27999445 -0.73118727 -1.18432407 0.62067899 0.51001408 0.96340779
## normtest.p
## 0.06913996
## -----
## Practical3a$teacher: B
##      median      mean      SE.mean CI.mean.0.95      var      std.dev
## 69.5000000 69.28571429 2.81471605 5.61520488 554.58385093 23.54960405
##   coef.var   skewness   skew.2SE   kurtosis   kurt.2SE  normtest.W
## 0.33989119 0.07963182 0.13885212 -0.82629072 -0.72959704 0.98226327
## normtest.p
## 0.42431929
```

The values of Skew.2SE and Kurt.2SE are within the -1.29 and 1.29 range: Skew.2SE for teacher A is -1.18 and Kurt.2SE for teacher A is 0.51. Skew.2SE for teacher B is 0.14 and Kurt.2SE is -0.73. Because the sample is of 130 students, we can assume that the values are close enough to a normal distribution. Since both teacher A and teacher B have Skew.2SE and Kurt.2SE values that are also within the -1.29 and 1.29 range, we can say that the data of the two teachers are normally distributed.

6. Checking for Normality Using a Test

6a

The null hypothesis for comparing our group's distribution to the normal distribution is that the data are not distributed according to the normal distribution.

6b

```
TA = subset(Practical3a, teacher == "A")
TB = subset(Practical3a, teacher == "B")
shapiro.test(as.numeric(unlist(TA)))
```

```
##
## Shapiro-Wilk normality test
##
## data:  as.numeric(unlist(TA))
## W = 0.46728, p-value < 2.2e-16
```

```
shapiro.test(as.numeric(unlist(TB)))
```

```
##
## Shapiro-Wilk normality test
##
## data:  as.numeric(unlist(TB))
## W = 0.45112, p-value < 2.2e-16
```

For both teacher A and teacher B, the significance value is less than $2.2e-16$, which means that it is not above 0.05 and it cannot be assumed that the data are normally distributed.

7. Checking for Equality of Variance

7a

```
sd(unlist(G1A))
```

```
## [1] 16.33577
```

```
sd(unlist(G1B))
```

```
## [1] 19.48486
```

```
sd(unlist(G1C))
```

```
## [1] 19.16235
```

```
sd(unlist(G1D))
```

```
## [1] 23.54226
```

```
sd(unlist(G1E))
```

```
## [1] 27.49295
```

The largest standard deviation is 27.5 and the smallest standard deviation is 16.3. These groups are equal in their variance, using the rule of thumb that the largest standard deviation is not more than twice as big as the smallest standard deviation.

7b

In this case, H_0 would be that there is no difference between the equal variance of the groups.

7c

```
install.packages('car')
```

```
##
## The downloaded binary packages are in
## /var/folders/_6/4dcygrqd30z3yrklv6121lt40000gn/T//RtmpePIGN2/downloaded_packages
```

```
library('car')
```

```
## Loading required package: carData
```

```
##
## Attaching package: 'car'
```

```
## The following object is masked from 'package:psych':
##
##      logit
```

```
leveneTest(TOTAL~teacher, data=Practical3a)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##           Df F value Pr(>F)
## group    1    0.967 0.3273
##          128
```

Since the $\text{Pr}(>F)$ significance level is smaller than 0.05 at 0.33, equal variances cannot be assumed.

8. Performing the T-Test

8a

```
t.test(Practical3a$TOTAL ~ Practical3a$teacher, var.equal = FALSE)
```

```
##
##  Welch Two Sample t-test
##
## data:  Practical3a$TOTAL by Practical3a$teacher
## t = 2.2819, df = 127.08, p-value = 0.02416
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##   1.210487 17.018085
## sample estimates:
## mean in group A mean in group B
##           78.40000           69.28571
```

8b

The conclusion I would draw with regard to the research question in 2b is that the teacher group A performs better compared to teacher group B. The chance of incorrectly rejecting the H0 is 0.0242 or 2.42%. This means that we can reject the H0. My conclusion about the H0 is in line with what I would expect from the descriptives.

Part B

```
Practical3b <- read.csv(file="Data-Practical3b.csv", head=TRUE, sep=";")
head(Practical3b)
```

```
##   Participant Motivation Voc.Score
## 1           1         Low        22
## 2           2         Low        28
## 3           3        High        28
## 4           4         Low        26
## 5           5         Low        18
## 6           6         Low        31
```

```
Practical3b$Participant <- as.factor(Practical3b$Participant)
Practical3b$Motivation <- as.factor(Practical3b$Motivation)
str(Practical3b)
```

```
## 'data.frame':    424 obs. of  3 variables:
## $ Participant: Factor w/ 424 levels "1","2","3","4",...: 1 2 3 4 5 6 7 8 9 10
## ...
## $ Motivation : Factor w/ 2 levels "High","Low": 2 2 1 2 2 2 2 1 1 1 ...
## $ Voc.Score  : int  22 28 28 26 18 31 22 25 20 25 ...
```

```
High <- subset(Practical3b, Motivation == "High")
Low <- subset(Practical3b, Motivation == "Low")
aggregate(Voc.Score~Motivation, Practical3b, max)
```

```
## Motivation Voc.Score
## 1 High 39
## 2 Low 37
```

```
aggregate(Voc.Score~Motivation, Practical3b, min)
```

```
## Motivation Voc.Score
## 1 High 9
## 2 Low 8
```

```
aggregate(Voc.Score~Motivation, Practical3b, mean)
```

```
## Motivation Voc.Score
## 1 High 23.88426
## 2 Low 22.86538
```

```
aggregate(Voc.Score~Motivation, Practical3b, range)
```

```
## Motivation Voc.Score.1 Voc.Score.2
## 1 High 9 39
## 2 Low 8 37
```

```
aggregate(Voc.Score~Motivation, Practical3b, sd)
```

```
## Motivation Voc.Score
## 1 High 5.219867
## 2 Low 5.243920
```

```
describe(Practical3b$Voc.Score)
```

```
##      vars   n mean   sd median trimmed  mad min max range  skew kurtosis   se
## X1      1 424 23.38 5.25    23   23.46 4.45   8  39   31 -0.09    0.27 0.25
```

```
boxplot(Voc.Score~Motivation, data=Practical3b, main="Vocabulary Score over Motiva
tion", xlab="Motivation", ylab="Vocabulary Score")
```

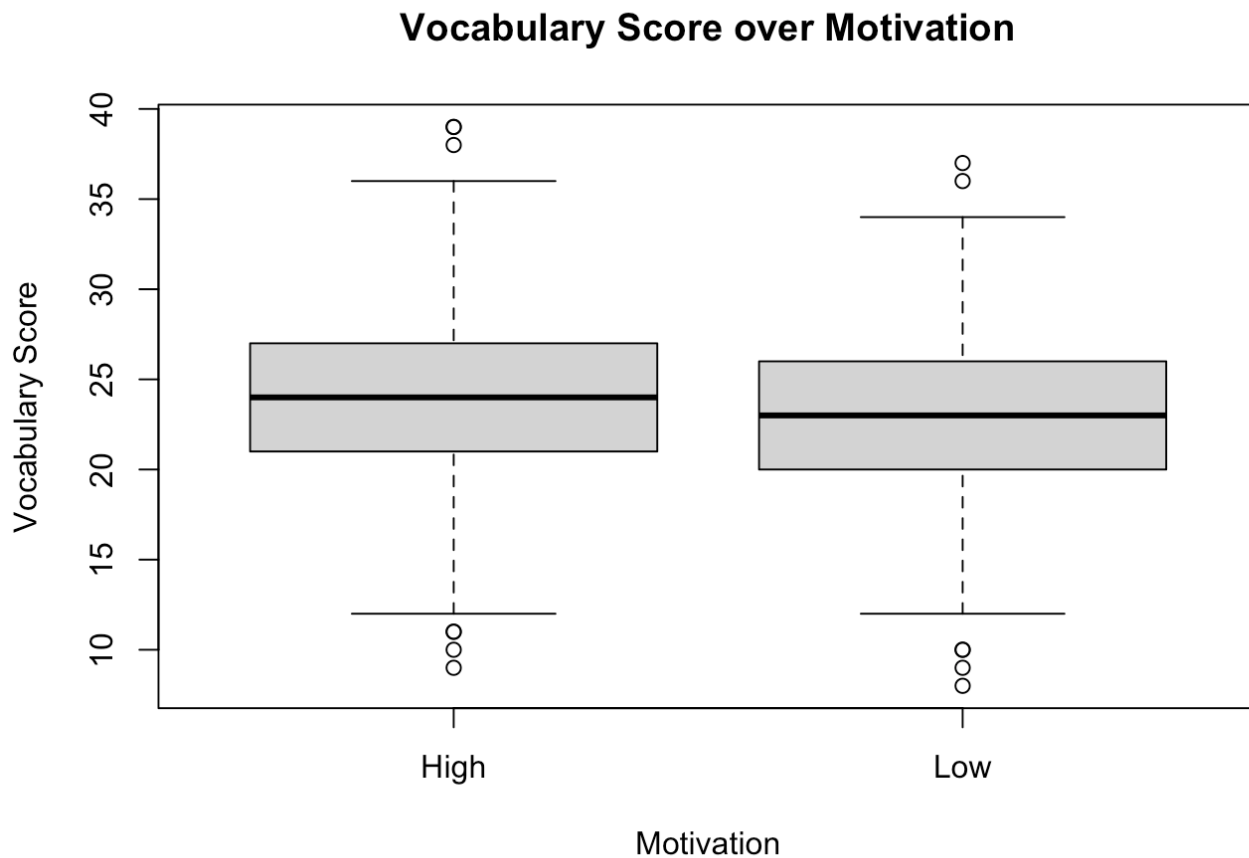


Figure 3: Boxplot of Vocabulary Score over Motivation

```
hist(Practical3b$Voc.Score, prob=TRUE, xlab="Vocabulary Score")
curve(dnorm(x, mean=mean(Practical3b$Voc.Score),sd=sd(Practical3b$Voc.Score)), add
=TRUE)
```

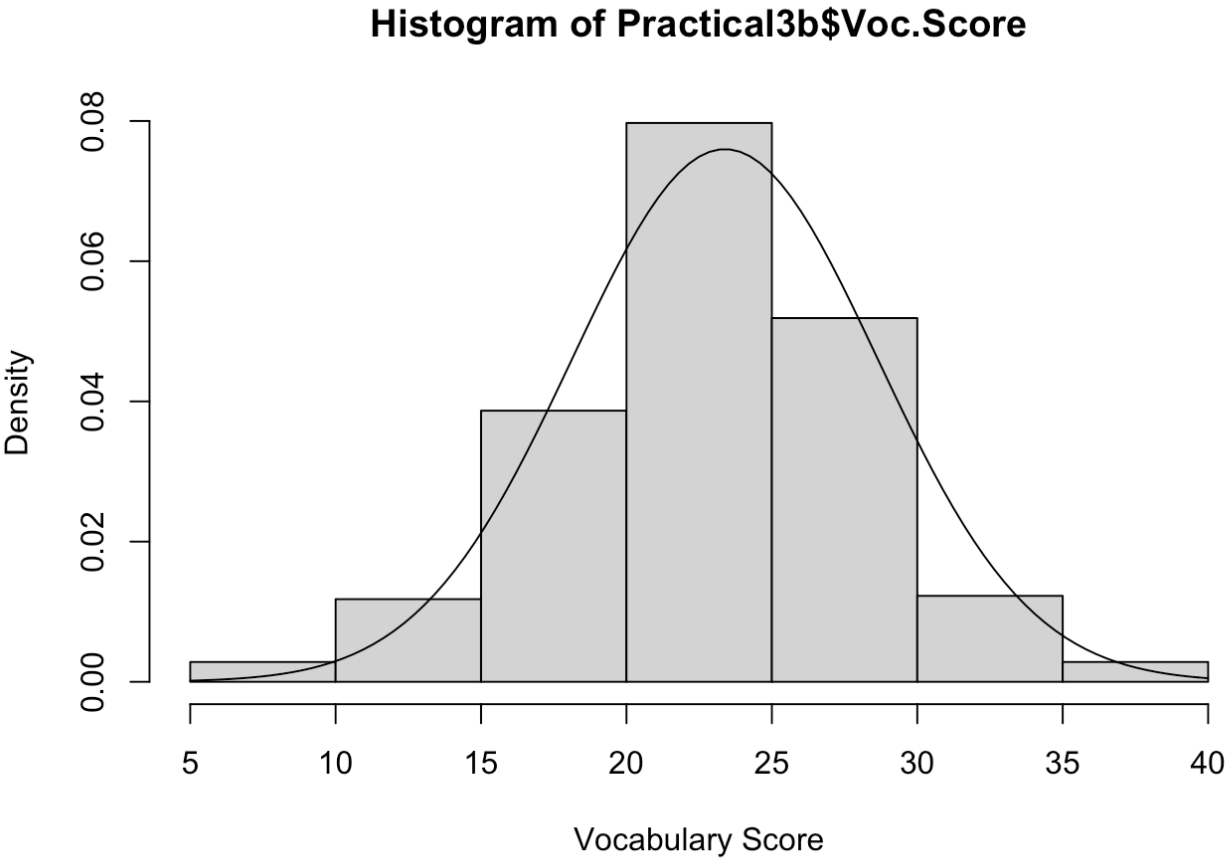



Figure 4: Histogram of Density over Vocabulary Score

```
stat.desc(Practical3b$Voc.Score, basic=FALSE, norm=TRUE)
```

##	median	mean	SE.mean	CI.mean.0.95	var	std.dev
##	23.00000000	23.38443396	0.25497784	0.50118139	27.56580914	5.25031515
##	coef.var	skewness	skew.2SE	kurtosis	kurt.2SE	normtest.W
##	0.22452180	-0.08889372	-0.37495312	0.27449594	0.58025231	0.99296579
##	normtest.p					
##	0.04443836					

```
by(Practical3b$Voc.Score, Practical3b$Motivation, stat.desc,  
basic=FALSE, norm=TRUE)
```

```
## Practical3b$Motivation: High
##      median      mean      SE.mean CI.mean.0.95      var      std.dev
## 24.00000000 23.88425926 0.35516693 0.70005502 27.24700689 5.21986656
##      coef.var      skewness      skew.2SE      kurtosis      kurt.2SE      normtest.W
## 0.21854840 0.04372938 0.13209317 0.44723142 0.67849436 0.99099767
## normtest.p
## 0.20150683
## -----
## Practical3b$Motivation: Low
##      median      mean      SE.mean CI.mean.0.95      var      std.dev
## 23.00000000 22.86538462 0.36360045 0.71683479 27.49869937 5.24392023
##      coef.var      skewness      skew.2SE      kurtosis      kurt.2SE      normtest.W
## 0.22933882 -0.22393648 -0.66397292 -0.02728182 -0.04063285 0.99180496
## normtest.p
## 0.29387426
```

```
shapiro.test(unlist(High))
```

```
##
## Shapiro-Wilk normality test
##
## data:  unlist(High)
## W = 0.67926, p-value < 2.2e-16
```

```
shapiro.test(unlist(Low))
```

```
##
## Shapiro-Wilk normality test
##
## data:  unlist(Low)
## W = 0.68212, p-value < 2.2e-16
```

```
leveneTest(Voc.Score~Motivation, data=Practical3b)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value Pr(>F)
## group 1 0.1184 0.7309
##      422
```

```
t.test(Practical3b$Voc.Score ~ Practical3b$Motivation, var.equal = FALSE)
```

```
##
##  Welch Two Sample t-test
##
## data:  Practical3b$Voc.Score by Practical3b$Motivation
## t = 2.0046, df = 421.24, p-value = 0.04565
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  0.01979307 2.01795621
## sample estimates:
## mean in group High  mean in group Low
##           23.88426           22.86538
```

Table 2: Shows the Max, Min, Mean, Range, and Standard Deviation Proficiency Scores for the Vocabulary Score by Motivation

value	Overall	High	Low
mean	23.4	23.88	22.86
max	39	39	37
min	8	9	8
range	31	30	29
sd	5.25	5.22	5.24

The H0, or null hypothesis, is that there is no significant effect of motivation on the vocabulary scores. The High motivation group performed better and scored more homogeneously. At face value when looking at the histogram, the majority of the results approximately follow the normal distribution. The values of Skew.2SE and Kurt.2SE are within the -1.29 and 1.29 range: Skew.2SE for high motivation is 0.13 and Kurt.2SE is 0.68. Skew.2SE for low motivation is -0.66 and Kurt.2SE is -0.04. Because the sample is of 130 students, we can assume that the values are close enough to a normal distribution. Since both high and low motivation have Skew.2SE and Kurt.2SE values that are also within the -1.29 and 1.29 range, we can say that the data of the two teachers are normally distributed. For both high and low motivation, the significance value is less than 2.2e-16, which means that it is not above 0.05 and it cannot be assumed that the data are normally distributed. Since the Pr(>F) significance level is larger than 0.05 at 0.73, equal variances can be assumed. The chance of incorrectly rejecting the H0 is 0.0457 or 4.57%. This means that we can reject the H0. My conclusion about the H0 is in line with what I would expect from the descriptives.