



Toward Entailment Checking: Explore Eigenmarking Search

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Big Picture

- Entailment is central to logic reasoning.
- Model checking goes through all combinations of logical symbols for validation of entailment: $O(2^n)$.
- Our work is to propose improved quantum search targeting a more efficient model checking.

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Logic Entailment: Model Checking

$KB \models \alpha$ if and only if, in **every truth scenario** in which KB is true, α is true.

Model checking = truth evaluation given truth values of all symbols.

KB:

- Durians are spiky.
- Durians are yummy.

α_1 : Montong durian is spiky.

α_2 : Montong durian is not spiky.

α_3 : There is life on Mars.

α_4 : There is no life on Mars.



Spiky Montong	Life on Mars	KB	α_1	α_2	α_3	α_4	
F	F	F	F	T	F	T	} $O(2^n)$
F	T	F	F	T	T	F	
T	F	T	T	F	F	T	
T	T	T	T	F	T	F	

$KB \models \alpha_1$

$KB \not\models \alpha_2$

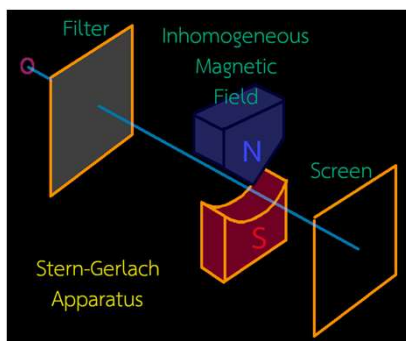
$KB \not\models \alpha_3$

$KB \not\models \alpha_4$

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Quantum Computing and Quantum Mechanical Properties



- Quantum computing utilizes quantum mechanical properties for computing.
- The quantum effect is more prominent at a small scale.
 - Linear evolution
 - Measurement
 - **Superposition**, Entanglement, Tunneling.

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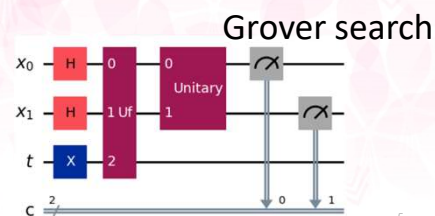
Grover Search

Classical

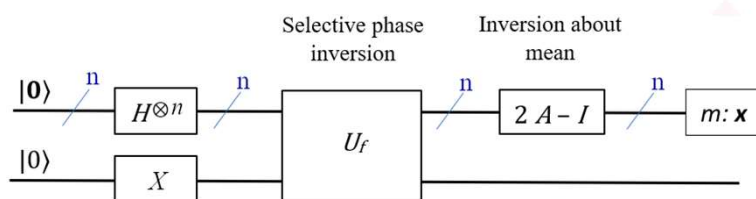
$x = 00 \dots 0 \dots x = 11 \dots 1$



- Problem: Given unknown $f(\cdot)$, find an answer $x' \in \{0,1\}^n$: $f(x') = 1$
- Promise: one and only one answer x' : $f(x') = 1$ and $f(x) = 0$ for all $x \neq x'$.
- Classical approach: trial-and-error
 - Average computation cost $\sim O\left(\frac{N}{2}\right) = O(2^{n-1})$
 - All possible candidates $N = 2^n$.



Grover Algorithm: Key Ideas



- Evolve the probability amplitude of the answer eigenstate such that when measured, the answer is more likely to be observed.
- ~ Parallelism using superposition!
- Implementation:
 - Selective phase inversion: mark the answer.
 - Inversion about the mean: amplify the answer's probability amplitude.
 - This relies on that the answer is minority!



Challenges and Our Approach

Spiky Montong	Life on Mars	KB	α_1	α_2	α_3	α_4	
F	F	F	F	T	F	T	
F	T	F	F	T	T	F	
T	F	T	T	F	F	T	
T	T	T	T	F	T	F	

When KB = T,

No F

2 Fs

1 F

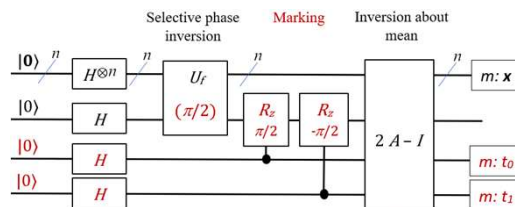
1 F

- Original Grover search addresses 1-F case.
- Our approach:
 - Additional qubits
 - Maintain minority condition for Grover amplification
 - Facilitate easy identification of no-winner case

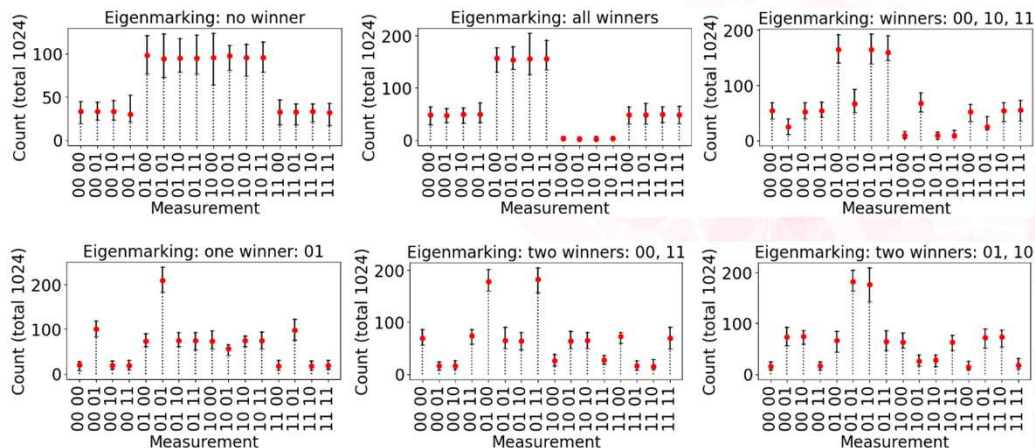
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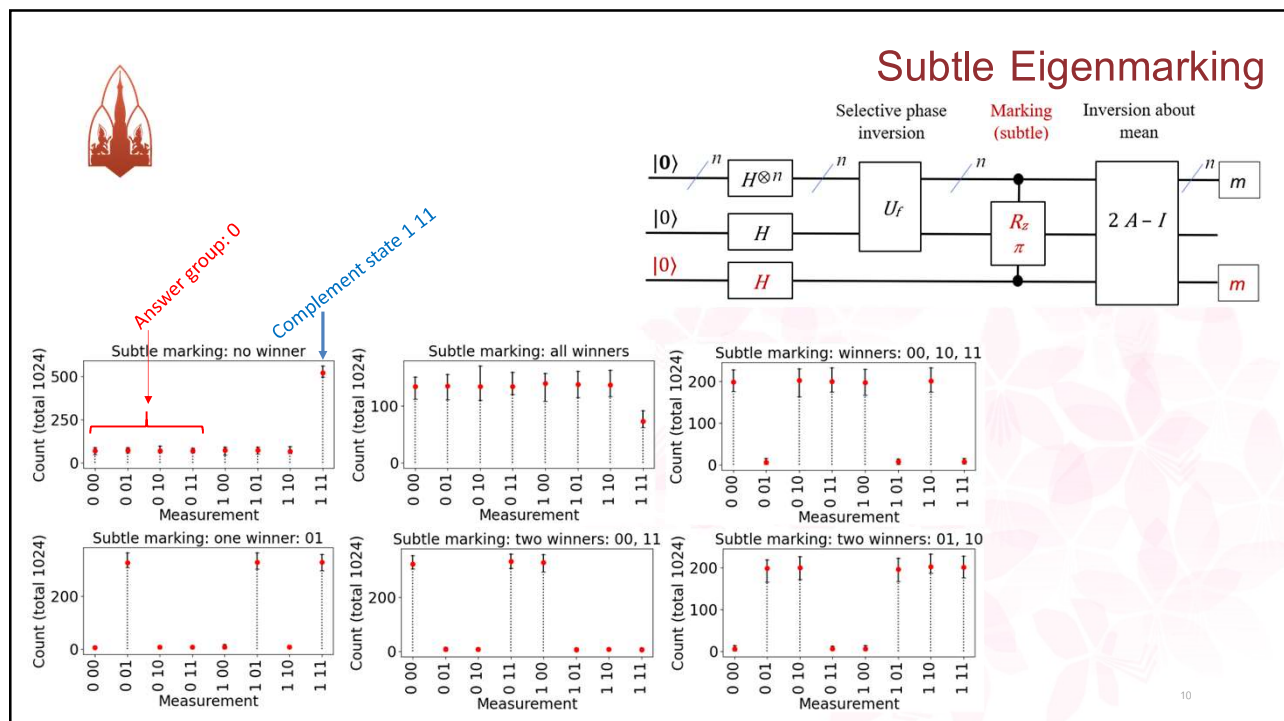
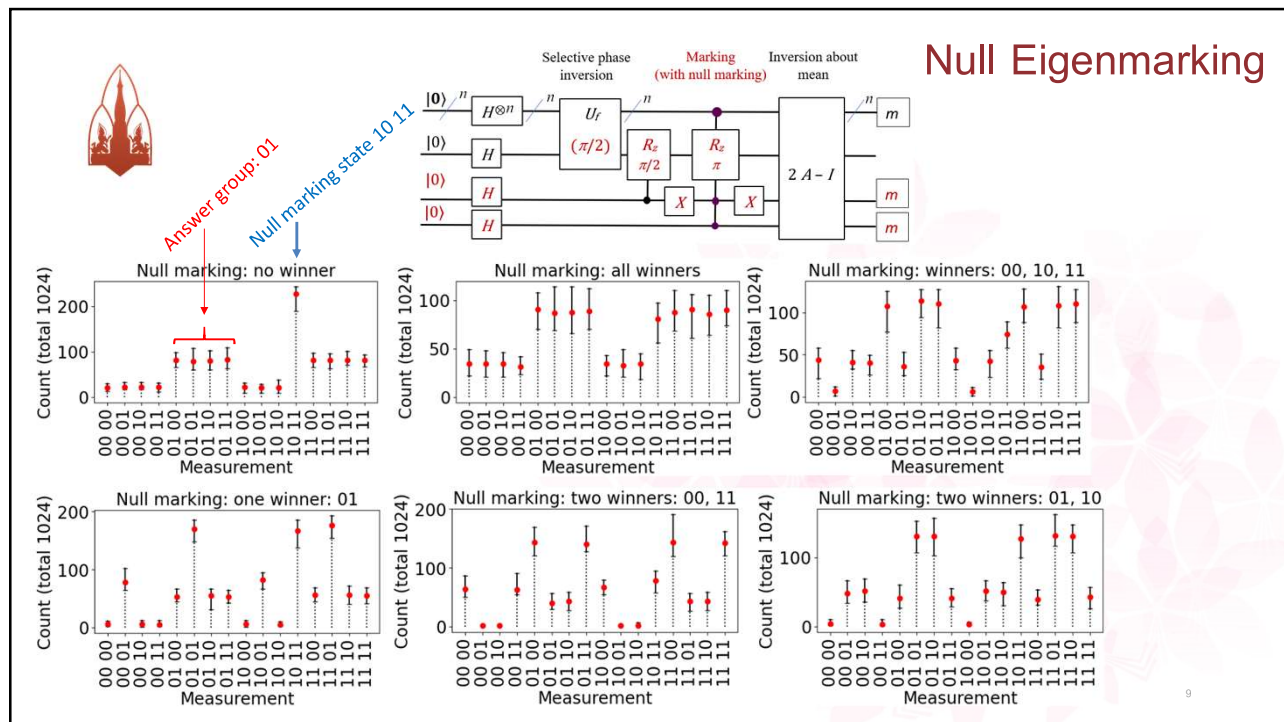
Answer group: 01
Complement group: 10



Eigenmarking



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Conclusion & Discussion

- **The ideas work!** (at least for a two-qubit case, in a simulator.)
- Quality of outcomes
 - Eigenmarking
 - Better at suppressing chances of dummy states: best global winning margin.
 - Quite well on distinguishability: best relative scores.
 - Subtle marking
 - Quite well on every aspect:
 - best local winning margin,
 - best absolute distinguishability.
- Architectural aspect: **subtle marking requires less modification, but needs multiple-qubit controls.**
- Limitations: **Scalability?** (more qubits) **Reliability?** (theoretical analysis) **Robustness?** (real QC)

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Thank you

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धन्यवाद।



Image: https://commons.wikimedia.org/wiki/File:Phrathat_Kham_Kaen.jpg

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