Verify muralizer algorithm on the arduino

Inverse transformation (to check results)

```
 \begin{split} & \text{In[142]:= inversexform[refpoints_] := Function} \Big[ \{ \text{radii} \} \,, \\ & \text{Block} \Big[ \{ \text{ra = radii[1], rb = radii[2], xa = refpoints[1, 1],} \\ & \text{ya = refpoints[1, 2], xb = refpoints[2, 1], yb = refpoints[2, 2]} \,, \\ & \left\{ \frac{\text{xa + xb}}{2} + \frac{(\text{ra - rb}) (\text{ra + rb}) (-\text{xa + xb})}{2 \left( (-\text{xa + xb})^2 + (-\text{ya + yb})^2 \right)} + \frac{(-\text{ya + yb})^2 + (-\text{ya + yb})^
```

Mathematica output

```
\ln[141]:= mathematicapath = {{124, 208}, {123, 207}, {123, 206}, {123, 205}, {122, 204}, {122, 203},
           {122, 202}, {121, 201}, {121, 200}, {121, 199}, {121, 198}, {120, 197}, {120, 196},
           {120, 195}, {120, 194}, {119, 193}, {119, 192}, {119, 191}, {119, 190}, {119, 189},
           {118, 188}, {118, 187}, {118, 186}, {118, 185}, {118, 184}, {118, 183}, {118, 182},
           {117, 181}, {117, 180}, {117, 179}, {117, 178}, {117, 177}, {117, 176}, {117, 175},
           {117, 174}, {117, 173}, {117, 172}, {117, 171}, {117, 170}, {117, 169}, {116, 168},
           {116, 167}, {116, 166}, {116, 165}, {117, 164}, {117, 163}, {117, 162}, {117, 161},
           {117, 160}, {117, 159}, {117, 158}, {117, 157}, {117, 156}, {117, 155}, {117, 154},
           {117, 153}, {117, 152}, {118, 151}, {118, 150}, {118, 149}, {118, 148}, {118, 147},
           {118, 146}, {118, 145}, {119, 144}, {119, 143}, {119, 142}, {119, 141}, {119, 140},
           \{120, 139\}, \{120, 138\}, \{120, 137\}, \{120, 136\}, \{121, 135\}, \{121, 134\}, \{121, 133\},
           {121, 132}, {122, 131}, {122, 130}, {122, 129}, {123, 128}, {123, 127}, {123, 126}, {124, 125}, {124, 124}, {124, 123}, {125, 122}, {125, 121}, {125, 120}, {126, 119},
           {126, 118}, {127, 117}, {127, 116}, {127, 115}, {128, 114}, {128, 113}, {129, 112},
           {129, 111}, {129, 110}, {130, 109}, {130, 108}, {131, 107}, {131, 106}, {132, 105},
           {132, 104}, {133, 103}, {133, 102}, {134, 101}, {134, 100}, {135, 99}, {135, 98},
           {136, 97}, {136, 96}, {137, 95}, {137, 94}, {138, 93}, {138, 92}, {139, 91}, {139, 90},
           {140, 89}, {141, 88}, {141, 87}, {142, 86}, {142, 85}, {143, 84}, {143, 83}, {144, 82},
           {145, 81}, {145, 80}, {146, 79}, {146, 78}, {147, 77}, {148, 76}, {148, 75}, {149, 74},
           \{149, 73\}, \{150, 72\}, \{151, 71\}, \{151, 70\}, \{152, 69\}, \{153, 68\}, \{153, 67\}, \{154, 66\},
           {155, 65}, {155, 64}, {156, 63}, {157, 62}, {157, 61}, {158, 60}, {159, 59}, {159, 58},
           {160, 57}, {161, 56}, {161, 55}, {162, 54}, {163, 53}, {163, 52}, {164, 51}, {165, 50},
           {166, 49}, {166, 48}, {167, 47}, {168, 46}, {169, 45}, {169, 44}, {170, 43},
           {171, 42}, {171, 41}, {172, 40}, {173, 39}, {174, 38}, {174, 37}, {175, 36},
           {176, 35}, {177, 34}, {177, 33}, {178, 32}, {179, 31}, {180, 30}, {181, 29}};
```

arduino output

Java

```
In[143]:= SetDirectory["/data/arduino/arduino-0015"]
     FileNames[]
Out[143]= /data/arduino/arduino-0015
Out[144]= {arduino, arduinolog, curve, examples, hardware,
       lib, .metadata, muralizer, reference, sketchbook, straightline}
In[147]:= TableForm[arduinoraw = Import["arduinolog", "Table"]]
Out[147]//TableForm=
     Stable
                                                  Library
     _____
                                                               Version = RXTX-2.1-7
Version = RXTX-2.1-7
     Native
                                                  lib
```

Binary sketch size: 7952 bytes (of

lib

0. 0.

0.

(124,208)

(181, 28)

15376.

43264.

0.

0. 0.

-0.01

-y

-x(123, 207)

-y

(123,206)

- (123, 205)
- $-\lambda$
- -x (122,204)
- -y
- (122,203)
- -y
- (122,202)
- $-\lambda$
- -x
- (121,201)
- -y
- (121,200)
- $-\mathbf{y}$
- (121,199)
- -y
- (121, 198)
- -y
- -x
- (120,197)
- $-\lambda$
- (120,196)
- $-\lambda$
- (120,195)
- -y
- (120,194)
- $-\lambda$
- -x
- (119,193)
- -y
- (119,192)
- $-\lambda$
- (119,191)
- -y
- (119,190)
- -y
- (119,189)
- $-\boldsymbol{\lambda}$
- -x
- (118,188)
- $-\lambda$
- (118,187)
- -y
- (118,186) -y
- _

(118,185)

 $-\mathbf{y}$

(118,184)

-y

(118,183)

-y

(118,182)

 $-\lambda$

-x

(117,181)

-y

(117,180)

 $-\lambda$

(117, 179)

 $-\mathbf{y}$

(117,178)

-y

(117,177)

 $-\mathbf{y}$

(117, 176)

 $-\lambda$ (117,175)

-y

(117,174)

-y

(117, 173) $-\lambda$

(117,172)

-y

(117,171)

 $-\lambda$

(117,170)

-y

(117,169)

 $-\lambda$

-x

(116,168)

 $-\mathbf{y}$

(116,167)

-y

(116,166)

-y

(116,165)

-y

(116,164)

- -y
- (116,163)
- -y
- (116,162)
- -y
- (116,161)
- -y
- (116,160)
- $-\mathbf{y}$
- (116,159)
- -y
- (116,158)
- -y
- (116,157)
- -y
- (116,156)
- -y
- (116,155)
- -y
- (116,154)
- -y
- (116,153)
- -y
- (116,152)
- $-\mathbf{y}$
- (116,151)
- $-\lambda$
- (116,150)
- -y
- (116,149)
- $-\lambda$
- (116,148)
- $-\lambda$
- (116,147)
- -y
- (116,146)
- $-\mathbf{y}$
- (116,145)
- $-\lambda$
- (116,144)
- $-\lambda$
- +x
- (117,143)
- -y
- +x

- (118,142)
- $-\lambda$
- +x (119,141)
- -y
- (119,140)
- -y
- +x
- (120,139)
- -y
- (120,138)
- $-\mathbf{y}$
- (120,137)
- $-\mathbf{y}$
- (120,136)
- -y
- +x
- (121, 135)
- -y
- (121, 134)
- $-\boldsymbol{\lambda}$
- (121, 133)
- $-\mathbf{y}$
- (121, 132)
- -y
- +x
- (122,131)
- -y
- (122,130)
- $-\lambda$
- (122, 129)
- -y
- +x
- (123, 128)
- -y
- (123,127)
- -y
- (123, 126)
- -À
- +x
- (124, 125)
- -y
- (124, 124)
- -y
- (124,123)

 $-\mathbf{y}$

+x

(125, 122)

 $-\lambda$

(125,121)

-y

(125,120)

-y

+x

(126,119)

 $-\lambda$

(126,118)

 $-\lambda$

+X

(127,117)

-y

(127,116)

 $-\mathbf{y}$

(127,115)

-y

+x

(128,114)

-y

(128,113)

 $-\lambda$

+x

(129,112)

-y

(129,111)

 $-\lambda$

(129,110)

 $-\lambda$

+x

(130,109)

 $-\lambda$

(130,108)

 $-\mathbf{y}$

+x

(131, 107)

 $-\lambda$

(131, 106)

 $-\lambda$

+x

(132,105)

 $-\lambda$

(132, 104)

- $-\mathbf{y}$
- +x
- (133,103)
- $-\lambda$
- (133,102)
- -y
- +x
- (134,101)
- -y
- (134,100)
- $-\lambda$
- +x
- (135,99)
- -y
- (135,98)
- $-\lambda$
- +x
- (136,97)
- $-\lambda$
- (136,96)
- -y
- +x
- (137,95)
- -y
- (137,94)
- $-\boldsymbol{\lambda}$
- +x
- (138,93)
- $-\lambda$
- (138,92)
- $-\lambda$
- +x
- (139,91)
- $-\lambda$
- (139,90)
- $-\mathbf{y}$
- +x (14
- (140,89)
- $-\lambda$
- +x
- (141,88)
- $-\lambda$
- (141,87)
- $-\lambda$
- +x
- (142,86)

- -y
- (142,85)
- $-\lambda$
- +x
- (143,84)
- -y
- (143,83)
- -y
- +x
- (144,82)
- -y
- +x
- (145,81)
- $-\mathbf{y}$
- (145,80)
- $-\lambda$
- +x
- (146,79)
- $-\mathbf{y}$
- (146,78)
- -y
- +x
- (147,77)
- -y
- +x
- (148,76)
- -y
- (148,75)
- $-\lambda$
- +x
- (149,74)
- $-\lambda \\$
- (149,73)
- $-\lambda$
- +x
- (150,72)
- $-\lambda$
- +x
- (151,71)
- $-\lambda$
- (151,70)
- -y
- +x
- (152,69)
- $-\lambda$
- +x

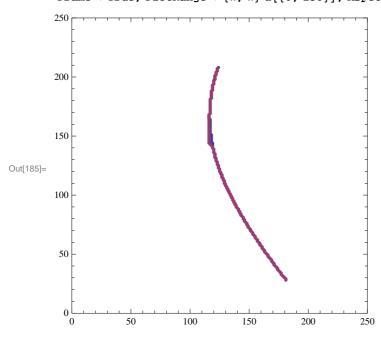
- (153,68)
- $-\lambda$
- (153,67)
- -y
- +x
- (154,66)
- -y
- +x
- (155,65)
- -y
- (155,64)
- -y
- +x
- (156,63)
- $-\lambda$
- +x
- (157,62)
- -y
- (157,61)
- -y
- +x
- (158,60)
- $-\lambda$
- +x
- (159,59)
- -y
- (159,58)
- -y
- +x
- (160,57)
- -y
- +x
- (161,56)
- $-\lambda$
- (161,55)
- $-\lambda$
- +x
- (162,54)
- $-\mathbf{y}$
- +x
- (163,53)
- -y
- (163,52)
- $-\mathbf{y}$
- +x
- (164,51)

- $-\mathbf{y}$
- +x
- (165,50)
- $-\lambda$
- +x
- (166,49)
- -y
- (166,48)
- -y
- +x
- (167,47)
- $-\lambda$
- +x
- (168,46)
- $-\lambda$
- +x
- (169,45)
- $-\lambda$
- (169,44)
- -À
- +x
- (170,43)
- -y
- +x
- (171,42)
- $-\lambda$
- (171,41)
- -y
- +x
- (172,40)
- $-\lambda$
- +x
- (173,39)
- $-\lambda$
- +x
- (174,38)
- -y
- (174,37)
- $-\lambda$
- +x
- (175,36)
- $-\mathbf{y}$
- +x
- (176,35)
- -y
- +x

```
(177,34)
              -y
              (177,33)
              -y
              +x
              (178, 32)
              -y
              +x
              (179,31)
              -y
              +x
              (180,30)
              -y
              +x
              (181, 29)
                                                                                                                                                                  179
              Pixels
                                                                                                                               drawn:
              Experimental:
                                                                                                                               JNI_OnLoad
                                                                                                                                                                  called.
|n|_{175}:= arduinopath = ToExpression[StringReplace[#, {"(" \rightarrow "{", "})" \rightarrow "}"}]] & /@
                    Select[First /@ Select[arduinoraw, Length[#] == 1 &],
                       MatchQ[#, s_String /; StringMatchQ[s, "(*,*)*"]] &]
_{Out[175]=} \hspace{0.1cm} \{ \{124,\,208\},\,\{181,\,28\},\,\{123,\,207\},\,\{123,\,206\},\,\{123,\,205\},\,\{122,\,204\},\,\{122,\,203\},\,\{122,\,202\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,\,204\},\,\{122,
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                    \{116, 163\}, \{116, 162\}, \{116, 161\}, \{116, 160\}, \{116, 159\}, \{116, 158\}, \{116, 157\},
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                    {116, 149}, {116, 148}, {116, 147}, {116, 146}, {116, 145}, {116, 144}, {117, 143},
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                    \{121, 135\}, \{121, 134\}, \{121, 133\}, \{121, 132\}, \{122, 131\}, \{122, 130\}, \{122, 129\},
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                    \{125, 121\}, \{125, 120\}, \{126, 119\}, \{126, 118\}, \{127, 117\}, \{127, 116\}, \{127, 115\},
                    {128, 114}, {128, 113}, {129, 112}, {129, 111}, {129, 110}, {130, 109}, {130, 108}, {131, 107}, {131, 106}, {132, 105}, {132, 104}, {133, 103}, {133, 102}, {134, 101},
                    {134, 100}, {135, 99}, {135, 98}, {136, 97}, {136, 96}, {137, 95}, {137, 94}, {138, 93},
                    \{138, 92\}, \{139, 91\}, \{139, 90\}, \{140, 89\}, \{141, 88\}, \{141, 87\}, \{142, 86\}, \{142, 85\},
                    {143, 84}, {143, 83}, {144, 82}, {145, 81}, {145, 80}, {146, 79}, {146, 78}, {147, 77}, {148, 76}, {148, 75}, {149, 74}, {149, 73}, {150, 72}, {151, 71}, {151, 70}, {152, 69},
                    \{153, 68\}, \{153, 67\}, \{154, 66\}, \{155, 65\}, \{155, 64\}, \{156, 63\}, \{157, 62\}, \{157, 61\},
                    \{158, 60\}, \{159, 59\}, \{159, 58\}, \{160, 57\}, \{161, 56\}, \{161, 55\}, \{162, 54\}, \{163, 53\},
                    \{163, 52\}, \{164, 51\}, \{165, 50\}, \{166, 49\}, \{166, 48\}, \{167, 47\}, \{168, 46\}, \{169, 45\},
                    {169, 44}, {170, 43}, {171, 42}, {171, 41}, {172, 40}, {173, 39}, {174, 38}, {174, 37},
                    \{175, 36\}, \{176, 35\}, \{177, 34\}, \{177, 33\}, \{178, 32\}, \{179, 31\}, \{180, 30\}, \{181, 29\}\}
```

Comparison

In[185]:= ListPlot[{mathematicapath, arduinopath}, Frame \rightarrow True, PlotRange \rightarrow {#, #} &[{0, 250}], AspectRatio \rightarrow 1]



ln[181]:= inversexform[{{-100, 0}, {100, 0}}][{128, 81}]

Out[181]=
$$\left\{ \frac{9823}{400}, -\frac{9\sqrt{1717391}}{400} \right\}$$

 $\label{limits} $$ \ln[184] = $ ListPlot[inversexform[\{\{-100,\,0\},\,\{100,\,0\}\}] / @ \# \& / @ \{mathematicapath,\,arduinopath\}, $$ (a) $ (a) $ (a) $ (b) $ (b) $ (b) $ (b) $ (c) $ (c)$ Frame \rightarrow True, PlotRange \rightarrow {{-100, 100}, {-200, 0}}, AspectRatio \rightarrow 1]

