



ALMA MATER STUDIORUM
UNIVERSITÀ DI BOLOGNA

Lesson 4

ILAI (M1) @ LAAI I.C. @ LM AI

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These slides draw very heavily from Simone Martini's slides.

One-slide recap of Lecture 3

Object: value enveloped in an identity. Different objects (identities) may have the same value
Identity accessible with `id()`. Identities compared with `is`. NB: `==` compares values, instead

Objects with same type have same methods. Methods are invoked on objects with the dot `.`

`tuple` is a compound/structured type (group of values each of its type). Immutable sequence.
Same operations of other immutable sequences

Generalized assignment: `<sequence of # names> = <sequence with the same # of elements>`

Slice: a «window» on a sequence. `[b:e:p]` between `b` included and `e` excluded, with step `p`
(default: 1. Can be negative to select backward)

Operations create new objects. On the contrary, assignments can create aliasing situations

`range`: a special sequence (not expanded). Indexes work like in slices. `for i in range() ... to`
iterate over numbers – usually indexes of a sequence

`while`: unbound iteration. I need to take care of initializing and modifying the guard.



Next lectures for ILAI

Monday, 30 September 15:00 - 18:00 (Regular, room 0.5)

Thursday 3 Oct: NO LECTURE (prof. Lodi busy)

Monday 7 Oct: NO LECTURE (cancelled in all ING area, I believe, on 7-8-9)

Thursday, 10 October 09:00 - 11:30 (Regular, room 2.8)

**ALL UPDATES ALREADY
ON THE COURSE WEBSITE**

Use this time for trying exercises on Virtuale ;-)



A new data type:

lists

Lists: list

- **structured** type (like tuple)
- *mutable* sequences of objects



Lists

Values: finite sequences of values, **mutable**

Presentation: [`<object1>`, ... , `<objectk>`]

`[]` is the empty list

a list with a single element: [`<element>`]

(or also [`<element>`,])

Operations: concatenation (+), repetition (*),
length `len()`, selection [...]

but also...



Mutable

Contrary to all types we have seen so far:
we may **modify the *value*** of an object
preserving its identity

Example:

```
L = [10, 20, 30]
```

```
L[1] = 200
```

The object bound to L **did not change**

Its value changed

Warning: LHS of = is **not** a name



Assignment, again

The simplest form (from L1):

`<name> = <expression>`

Now:

`<selection> = <expression>`

`<selection>` must be on a mutable object (and cannot be a name)

Plus the extended versions we saw in L3:

`<name1>, ..., <namek> = <sequence with exactly k elements>`

`A, B = B, A`

`L[i+1], L[i] = L[i], L[i+1]`



Assignment, again

Now:

<selection> = <expression>

<selection> must be on a mutable object (and cannot be a name)

Semantics:

- evaluate *<expression>* and obtain an object *o*
- evaluate **<selection>** and obtain a component *p* of a modifiable object *m*
- the component *p* of *m* is modified in *o*

Observe: there is **no** modification of the **bindings between names and values** in the internal state



Function that takes a list of int and modifies every 0 into 100

```
L = [1, 2]
V = [10, 20]
W = L + V
L = L + [3]
L[0] = 100
Z = ['s', V, 10]
Z[1][0] = 0
print(V)
```

```
L = [1, 2]
V = [10, L, 20]
W = [30, L, 40]
printV)
print(W)
```

```
LL = L[:]
VV = V[:]
Z = ...
```

Example: double the value of elements

Given a list L of int, modify any element,
transforming it in its double

=> file double.py

given L=[10,20,30,40],
transform L in [20,40,60,80]



Aliasing and side effects

```
L = [10, 20, 30]
```

```
V = L
```

```
L[0]=100
```

```
print(V)
```

Since there is aliasing (V and L are alias for the same object),

V has been modified by *side effect*

We also say:

```
L[0]=100
```

has the side effect to modify V



Aliasing and side effects, 2

We may have aliasing also on tuples (or int, or float etc.):

```
T = (10, 20, 30)
R = (100, T, 300)
```

the “same” on lists:

```
L = [10, 20, 30]
W = [100, L, 300]
```

On list we may modify L, and this will be seen also from W



Aliasing and side effects

Small examples on
aliasing_example.py



Aliasing and side effects, moral

Aliasing and side effects are present in the language *by design*

They are important to do meaningful things!

Yet, they are a delicate, subtle ingredient of the language

- to be understood
- to be controlled
- because they are source of errors which are difficult to locate and discover



Deleting elements from a list: del

Command del:

```
del L[i]
```

Semantics:

L[i] is eliminated from L

the elements "following" L[i] are "shifted to the left"

(indexes are recomputed)



Given list L of int, delete the zeros

`L = [1, 2, 0, 0, 3, 0, 5, 0]`

Given list L of int, delete the zeros

```
L = [1, 2, 0, 0, 3, 0, 5, 0]
```

```
i=0
```

```
while i < len(L):
```

```
    if L[i] == 0:
```

```
        del L[i]
```

```
    else:
```

```
        i=i+1
```

```
# here L is [1, 2, 3, 5]
```

Observe that the index is incremented *only*
when `del` is *not executed* (file `removezero.py`)



It does not work with for!

```
L = [1,2,0,3,0,5,0]
i=0
while i<len(L):
    if L[i]==0:
        del L[i]
    else:
        i=i+1
# here L is [1,2,3,5]
```

```
L = [1,2,0,3,0,5,0]
for i in range(len(L)):
    if L[i]==0:
        del L[i]
# here L is ??
```

WRONG: IT DOES NOT WORK!



Don't use `for` on lists in presence of side effects!

Never (never !)
use `for` on lists,
*if their length
is modified in the `for` body*

Don't use `for` on lists in presence of side effects!

*The heading of the `for` command freezes
the sequence object (its identity)*

not its value

del

In the "modifying assignment"

<selection> = <expression>

<selection> *must be an explicit selection*

In

del <selection>

<selection> *must be an explicit selection*

Compare:

```
L = [10, 20, 30]
```

```
del L[1]
```

```
L = [10, 20, 30]
```

```
e = L[1]
```

```
del e
```

Beware: del <name> will remove <name> from the internal state!



Add/delete elements: methods

Invoking a method on an object of type list
may *modify the object*



Some methods on list

`L.append(x)`

append x as last element of L; returns None

`L[len(L):]=[x]`

`L.insert(i,x)`

insert x in L at index i (shifting indexes),
or append if $i \geq \text{len}(L)$; returns None

`L[i:i]=[x]`

`L.extend(V)`

extends L with list V (in place concatenation)

`L[len(L):]=V`

`L.clear()`

empties L

`del L[:]`

→→→ all of them return None



Add/delete elements: slice

<selection> = <expression>

<selection> may be a *slice*

If <selection> is a slice:

- *RHS must be a list, whose elements are inserted for the slice*
- *as a result of the assignment, the list at LHS may grow, or shrink*



Add/delete elements: slice

Selection may be a *slice*. Examples:

`L = [1, 2, 3]`

1	2	3
---	---	---

`L[0:2] = [10, 20]`

10	20	3
----	----	---

`L[0:1] = [5, 6]`

5	6	20	3
---	---	----	---

`L[-1:] = [4]`

5	6	20	4
---	---	----	---

`L[1:1] = [1, 2]`

5	1	2	6	20	4
---	---	---	---	----	---

`L[0:2] = []`

2	6	20	4
---	---	----	---

`L[0:0] = [1]`

1	2	6	20	4
---	---	---	----	---

`L[len(L) :] = [30]`

1	2	6	20	4	30
---	---	---	----	---	----



Warnings

1)

`del L[i:j]` is equivalent to `L[i:j]=[]`

2)

`L[1:2]=[4,5,6]` and `L[1]=[4,5,6]`

are two (very!) different things

- `L[1:2]=[4,5,6]` *extends* L

- `L[1]=[4,5,6]` leaves unchanged the length of L,: the element L[1] is replaced by the (list) object [1,2,3]



Warnings

Semantically equivalent to slicing

- In general, using methods is more efficient



Careful

`L=L+[elemento]`

is not the same as

`L.append(elemento)`

In the first, a new object is created

In the second, no new object

Then...



Don't use `for` on lists in presence of side effects!

The heading of the `for` command freezes the sequence object (its identity)

not its value

Compare:

```
L=[10]
for e in L:
    L.append(e)
print(L)
```

```
L=[10]
for e in L:
    L=L+[e]
print(L)
```



Warning!

The heading of the `for` command freezes the sequence object (its identity)

not its value

Compare:

```
L=[10]
for e in L:
    L.append(e)
print(L)
```

```
L=[10]
for e in L:
    L=L+[e]
print(L)
```

The first is an infinite loop, the second prints [10,10]



Careful

`L=L+[elemento]`

is not the same as

`L.append(elemento)`

Suppose there is aliasing on the object bound to L:

```
L=[10,20,30]
```

```
W=L
```

```
L.append(40)
```

```
print(W)
```

```
L=L+[60]
```

```
print(W)
```

```
print(L)
```



One example with methods

Read from the keyboard a series of positive integers, until the user inserts 9999
Store the numbers in a list

file inser.py



assignment: one more variant

augmented assignment

In iteration scans one often uses:

```
res = res + val
```

or also

```
count = count*val
```

We may use *contracted forms*



assignment: one more variant

augmented assignment

In iteration scans one often uses:

```
res = res + val
```

or also

```
count = count*val
```

We may use *contracted forms*

```
res += val
```

```
count *= val
```



Augmented assignments

`+=` `-=` `*=` `/=` `//=` `%=` `**=`

and even others

Operations are overloaded:

`T += v`

is addition, or concatenation, etc.

depending from the type of T



Augmented assignments

$$x += v$$

$$x = x + v$$

Similar, *but not the same*, to its "normal" analogue

1. the operation is done *in place* if possible
2. *x is evaluated only once*
3. *LHS is evaluated first*

Let's dig deeper



Augmented assignments

Similar, but *not the same* as their "normal" analogues

1. The operation is done *in place* if possible

```
L = [1, 2, 3]  
L += [4]
```

```
V = [1, 2, 3]  
V = V + [4]
```

are two *different things*:

`+=` is extend (append) on lists!



Augmented assignments

Similar, but *not the same* as their "normal" analogues

2. *x is evaluated only once*

Let $f(x)$ be a function

$$L[f(i)] += val$$
$$L[f(i)] = L[f(i)] + val$$

$+=$ calls $f(i)$ only once

➔ if $f()$ has side effects, they happen once only!

Augmented assignments

Similar, but *not the same* as their "normal" analogues

3. *LHS is evaluated first*, then RHS, then the binding in the state is modified

Let $f(x)$ be a function

$L[f(i)] += exp$

*If $f(i)$ has side effects, they happen **before** the evaluation of exp*

(file augmented.py)



More methods on list

`L.remove(x)`

remove from L the first element `L[i]` equal (`==`) to `x`
error if `x` not in L
returns `None`

`L.copy()`

`L[:]`

returns a (shallow) copy of L

`L.reverse()`

reverses L (in place)
returns `None`

What is the difference with `L=L[::-1]` ??
remember the mantra: "operations create new objects"

`L.sort()`

sort L (in place)

compare with the builtin function `M = sorted(L)`
remember the mantra: "operations create new objects"



More methods on list

`L.pop(i)`

returns and removes the element at index `i`

`pop()` returns and removes `L[-1]`

returns a value: `L[i]`

modify in place the list, removing the element at index `i`

leave unchanged the identity of `L`



Double (nested) iteration

Sometimes we need to iterate *inside* another iteration.
This programming schema is called double (or nested) iteration

Trivial example: Given a tuple of tuples of integers, count the zeros

```
def zeros(ToT):  
    count=0  
    for t in ToT:  
        for e in t:  
            if e==0:  
                count += 1  
    return count
```

file tuples.py

Individual exercises at the end of the slides



Can functions modify global mutable objects?

Can functions modify global objects?

Observe that with *immutable* objects, this is impossible:

```
b=20
def f(a):
    a=10
    b=100
    return None
f(b)
print(b)
```

a,b in the body of f are local names!



Intermezzo: global (more in next lecture)

Observe that with *immutable* objects, this is impossible,
unless a global declaration is used

```
b=20
def f(a):
    global b
    a=10
    b=100
    return None
f(b)
print(b)
```

a is local; b is the one in the main frame



Can functions modify global mutable objects?

With mutable objects: **possible**, in several ways

1. *Through a mutable actual parameter:*

```
b = [20]
def f(a):
    a[0] = 100
    # return None
f(b)
print(b)
```

In Pythontutor...

Of course the assignment `a[0] = 100` would result in an error when `f` is called on an immutable actual parameter



Can functions modify global mutable objects?

With mutable objects: **possible**, in several ways

2. *Through a global name, bound to a mutable object*

```
b = [20]
def f():
    b[0] = 100
f()
print(b)
```

In Pythontutor...

Observe: at the left of = there is a *selection* not a name

Hence the rule: "name at the left of = is local" cannot be applied



Some exercises and challenges

For home 1: ordered insertion

Write a function

```
def ins_ord(L,el):
```

```
    """L: ordered list, in increasing order
```

```
    insert el in L, in place"""
```

Example:

```
S=[2,4,6,8]
```

```
ins_ord(S,5) must modify S in [2,4,5,6,8]
```

Some solutions in file `inserimento-in-lista-ord.py`



For home 2: Floyd triangles

A *Floyd triangle* of order 5:

five rows, with the integers from 1; any row has one more element of the previous row

```
1
2  3
4  5  6
7  8  9 10
11 12 13 14 15
```

Write a function `Floyd(n)` which prints a Floyd triangle of order `n`

We want a *pretty print*



For home 2: Floyd triangles

We want a *pretty print*

print may have additional arguments "**by keyword**":

sep: string used to separate values *in the same print* (default: ' ')

end: string used to *terminate, after a print* (default: newline: '\n')

```
print(10,20)
print(30,40)
print(10,20,sep=' & ',end=' * ')
print(30,40,sep=' & ')
print(50)
```

\t is "tab"

\n is "neline"

etc: look in the doc

```
10 20
30 40
10 & 20 * 30 & 40
50
```



Double iteration: matrices

Python does not have a type for array/matrices

(but we will see and use the library NumPy)

AS TOY EXERCISE for nested iterations, encode a $n \times m$ matrix as:

- list of lists
 - a list of n elements (the rows),
 - each element is a list of m elements
(the m elements of the row)

$$A = \begin{pmatrix} 0 & 1 \\ 3 & 2 \\ 5 & 6 \end{pmatrix}$$

$$LA = \begin{bmatrix} [0, 1], \\ [3, 2], \\ [5, 6] \end{bmatrix}$$

Double iteration: matrices

Element $a_{i,j}$ of matrix A

is encoded as element $L[i-1][j-1]$ of list LA

(supposing that the indexes of A start at 1)

For simplicity: suppose that both start from zero

$$A = \begin{pmatrix} 0 & 1 \\ 3 & 2 \\ 5 & 6 \end{pmatrix}$$

$$LA = \begin{bmatrix} [0, 1], \\ [3, 2], \\ [5, 6] \end{bmatrix}$$

Double iteration: matrices

Exercise 1:

Write a function

```
def is_sum_mat(A,B,S):
```

```
    '''A, B, S: matrices encoded as lists
```

```
    verify that S is the matrix sum of A and B:
```

```
    for any i and j:  $S[i][j] = A[i][j] + B[i][j]$ '''
```



Double iteration: matrices

Exercise 2:

Write a function

```
def sum_mat(A,B):
```

```
    '''A, B: matrices encoded as lists
```

```
    return a new list S, the matrix sum of A and B, as a list of lists'''
```



Double iteration: matrices

Exercises 3-4-5:

- (1) Function which computes and returns the *transpose* of a matrix, taken as a parameter
- (2) Function which takes two *lists* (non matrices!) of the same length, and computes and returns the *scalar product of the two lists*
- (3) Function which returns the *product of two matrices* A and B, given as parameters (you may assume they are in the correct format).

Hint: you may use the transpose to make the scalar product between the rows of A and the rows of the transpose of B

