

Homework #8 (NQe311, Spring, 2020)

KAIST

(Due June 4)

1. Let's consider 1-D heat conduction equation below

$$\begin{aligned}\frac{\partial u(x,t)}{\partial t} &= \frac{\partial^2 u(x,t)}{\partial x^2} + f(x,t), \\ u(0,t) &= u(1,t) = 0, \\ u(x,0) &= \sin \pi x\end{aligned}$$

Assuming that the problem is solved by an implicit time differencing with a constant time step (Δt), show that the numerical scheme is unconditionally stable using the Fourier stability analysis. You can assume that a central difference with a uniform node size (Δx) is applied to the spatial differentiation.

2. For the following matrix A

$$A = \begin{pmatrix} 2 & 3 & 4 \\ 7 & -1 & 3 \\ 1 & -1 & 5 \end{pmatrix},$$

- i) Find the largest eigenvalue and corresponding eigenvector by the power method.
- ii) Find the smallest eigenvalue and corresponding eigenvector by the inverse power method.
- iii) Find the intermediate eigenvalue and corresponding eigenvector by the shifted inverse power method.

You have to develop your program for the tasks.