

Object-Oriented Programming

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Contents

What is object-oriented programming?	2
Type Systems	13
Polymorphism and type safety	25

What is object-oriented programming?

What is object-oriented programming?

*... Object-oriented programming (OOP) is a programming paradigm based on the concept of **objects**. Objects can contain data (called fields, attributes or properties) and have actions they can perform (called procedures or **methods** and implemented in code).*

— Wikipedia

Classes and objects : taxonomy

- **class-based** : in many languages, you first define a **class** (\approx template of objects)
 - an object is made from a class (object = **instance** of a class)
 - C++, Python, Go, Julia, Rust
- **prototype-based** or **classless** : in other languages, you can create an object with or without defining a class
 - an object can be made by a generic object expression or from a class
 - Javascript, OCaml

Classes and objects : examples

Python class definition

```
class point:  
    def __init__(self, x, y):  
        self.x = x;  
        self.y = y;
```

Object creation

```
a = point(1.2, 3.4)
```

Classless object creation : example

Javascript

```
let a = { "x" : 1.2, "y" : 3.4 }
```

OCaml (classless)

```
let a = object method x = 1.2 method y = 3.4 end
```

OCaml (with class)

```
class point (x : float) (y : float) =  
  object method x = x method y = y end;;  
let a = new point 1.2 3.4
```

Relevant keywords/syntax in our languages

language	class definition	object creation
Go	<code>type Point struct ...</code>	<code>Point(1.2, 3.4)</code>
Julia	<code>struct Point ...</code>	<code>Point(1.2, 3.4)</code>
Rust	<code>struct Point ...</code>	<code>Point(1.2, 3.4)</code>
OCaml	<code>class point ...</code>	<code>object ... end</code>

Methods

- method \approx function or procedures in any other language
- so what is different?
 - *multiple definitions* of a method of the same name can exist
 - e.g., an `area` method for `rectangle`, `circle`, `triangle`, etc.
 - ***dynamic dispatch*** : when calling a method, which one gets called depends on which objects it is called for

Dynamic dispatch : taxonomy

- **single dispatch** : many languages determine which method gets called by the type of a *single* argument (object)
 - it is called a “*receiver*” object
 - C++, Python, Go, OCaml, Rust
- **multiple dispatch** : some languages determine which method gets called by the types of *multiple* arguments (objects)
 - Julia

Single dispatch : example

- multiple definitions of `area` method in Python

```
class circle:
    ...
    def area(self):
        r = self.r
        return pi * r * r

class rect:
    ...
    def area(self):
        return self.w * self.h
```

- dispatch, based on whether `s` is `circle` or `rect`

```
shapes = [circle(...), rect(...)]
for s in shapes:
    s.area() # method call
```

An equivalent Julia example

- multiple definitions of `area` method in Julia

```
function area(c :: Circle)    function area(r :: Rect)
    pi * c.r * c.r            r.w * r.h
end                            end
```

- dispatch, based on whether `s` is `circle` or `rect`

```
shapes = [Circle(...), Rect(...)]
for s in shapes
    area(s)
end
```

Multiple dispatch

- let's say we define a method `contains(a, b)` that computes whether *a* contains *b*
- Julia allows you to define it based on *both* *a* and *b*

```
function contains(c0 :: Circle, c1 :: Circle) ...  
function contains(c0 :: Circle, r1 :: Rect) ...  
function contains(r0 :: Rect, c1 :: Circle) ...  
function contains(r0 :: Rect, r1 :: Rect) ...
```

Type Systems

Types

- **types** in programming languages \approx *kind* of data. e.g.,
 - integers, floating point numbers, array of integers, ...
 - there are user-defined types (e.g., `circle`, `rect`, etc.)
- the type of data generally determines what operations are valid on it, e.g.,
 - `s.area(...)` is valid if `s` is a `circle`, `rect`, or other type that defines an `area` method
 - `a[i] = x` is valid if `a` is an array, or other type that supports indexed assignment (`..[..] = ...`)

Type errors at runtime

- at runtime, each data naturally has its type (*dynamic type* or *runtime type*)
- when an operation not defined on the runtime type of data is applied, a *runtime type error* results.
- e.g., Python code below gets an error in the third iteration

```
shapes = [circle(...), rect(...), (3,4)]
for s in shapes:
    print(s.area())
```


Runtime type errors are disastrous

- some languages perform *runtime type checking*, which detects runtime type errors and gracefully aborts the program with error messages
 - Python, Javascript, Julia
- some languages do not perform runtime type checking, which may cause *segmentation fault* or even worse, *data corruption*
 - C, C++

Static types and static type checking

- other languages guarantee, *prior to execution*, that no runtime type errors will happen (*static type checking*)
- it generally works by
 - calculating *the static or compile-time type of each expression*, and
 - judging the validity of each operation by static types,
 - before execution

An example (in a hypothetical Python-like language)

```
l = [circle(..), circle(..)]  
for c in l:  
    c.area()
```

- static types (“*expr : type*” means *expr* has *type*)
 - `circle(..)` : `circle`
 - `[circle(..), circle(..)]` : list of `circle`
 - `l` : list of `circle`
 - `c` : `circle`
 - `c.area()` : `float`
- this program is *(well-)typed* and never causes a runtime error

Another example

```
l = [(3,4), (5,6)]  
for p in l:  
    p.area()
```

- static types
 - ▶ (3,4) : pair of int
 - ▶ [(3,4), (5,6)] : list of pair of int
 - ▶ l : list of string
 - ▶ p : pair of int
 - ▶ p.area() : **error** (area on pair of int)

(A bit pedantic) taxonomy

- languages performing static type checking are generally called *statically typed*
- not all statically typed languages *guarantee* absence of runtime type errors
 - C, C++, Java
- statically typed languages that do are called *type safe*
 - Go, OCaml, and Rust (without `unsafe`) are type safe

Is type safety difficult to achieve?

- in the simple case, no
- specifically, it is not difficult if the static type of an expression *uniquely determines* its runtime type
 - we call such a language *simply typed*
 - in simply typed languages, each expression or variable can take values of only a single runtime type
- then what's the matter?

Why simply typed languages do not suffice?

- they are *inflexible* and hinder *code reusability*. e.g.,
- cannot put elements of different types in a single container

```
l = [rect(..), circle(..)]  
for s in l:  
    s.area() # what is the static type of s??
```

Why simply typed languages do not suffice?

- cannot have a single function definition of an array of different types, even when element type should not matter

```
def n_elems(l): # list of what?
    n = 0
    for x in l:
        n += 1
    return n
```

```
n_elems([1,2,3])
n_elems(["a", "b", "c"])
```


Polymorphism

- in each of the examples, a single expression can take values of different types at runtime

```
l = [rect(..), circle(..)]    n_elems([1,2,3])
for s in l:                    n_elems(["a", "b", "c"])
    s.area()
```

- a variable or expression is said to be *polymorphic* when it can take values of different runtime types
- a language is said to support *polymorphism* when it allows polymorphic variables or expressions

Polymorphism and type safety

Polymorphism and type safety

- forget about type safety \Rightarrow polymorphism is easy to achieve
 - Julia, Python, Javascript, or many scripting languages
- forget about polymorphism (i.e., settle for simply typed languages) \Rightarrow type safety is easy to achieve
- achieving *both* polymorphism and type safety is difficult

Static type system for polymorphism

- informally, we need a static type representing multiple dynamic types
- two common approaches
 1. *subtype polymorphism* : allows a single static type that accommodates multiple types
 2. *parametric polymorphism* : allows a static type having *parameter(s)*, which can be instantiated into multiple types

Subtype polymorphism

- `s` has a static type, like “shape”, that accommodates both `rect` and `circle`

```
l = [rect(..), circle(..)]  
for s in l:  
    s.area()
```

- in this example, we say `rect` (and `circle`) is a *subtype* of `shape`
- or, `shape` is a *supertype* of `rect` (and `circle`)
- more on this later

Parametric polymorphism

- `n_elems` has a static type (like “ $\forall \alpha. \text{array of } \alpha \rightarrow \text{int}$ ”), which can be instantiated into “array of int” and “array of string”

```
n_elems([1,2,3])
```

```
n_elems(["a", "b", "c"])
```

- we’ll cover this more in the next week

How static type checking works with subtyping

- in the hypothetical Python-like language

```
def smaller(s0 : shape, s1 : shape) -> shape:  
    return (s0 if s0.area() < s1.area() else s1)
```

```
smaller(rect(..), circle(..))  
smaller(circle(..), rect(..))
```

- $s0, s1 : \text{shape}$
- $\Rightarrow s0.\text{area()}, s1.\text{area()} : \text{float}$
- $\Rightarrow s0.\text{area()} < s1.\text{area()} : \text{boolean}$
- $\Rightarrow s0 \text{ if } \dots \text{ else } s1 : \text{shape}$

The key question

- in the example above,
 - `smaller(rect(...), circle(...))` is valid. i.e.,
 - passing a value of “rect” (or “circle”) type to a parameter of “shape” type is allowed
- the key question:

for two types S and T when is an *assignment-like operation* $S \leftarrow T$ valid (safe if allowed)?

Note: assignment-like operation

- intuitively, any operation that flows a value to another place
 - assignment (left hand side : $S \leftarrow$ right hand side T)
 - passing arguments (formal arg : $S \leftarrow$ actual arg : T)
- in general, any operation where a value whose static type is T becomes a value of another expression whose static type is S
 - returning a value (return type $S \leftarrow$ returned expression : T)
 - conditional expression (result type $S \leftarrow$ then/else expression : T)

When is $S \leftarrow T$ safe?

- informally, $S \leftarrow T$ is safe when *any operation applicable to S is also applicable to T (*)* (Liskov substitution principle)
 - ex: “shape \leftarrow rect” is safe, because operation applicable to (any) shape will be applicable to rect (whether it’s true depends on how they are actually defined, of course)
- intuitively, T is a kind of S
 - ex: rect (circle) is a kind of shape

Subtype

- we write $T \leq S$ and say T is a **subtype** of S (and S is a **supertype** of T) when (*) is the case
 - ex: $\text{rect} \leq \text{shape}$, $\text{circle} \leq \text{shape}$
- if we think of a type as a set, \leq represents a subset relation
- the exact definition of \leq varies between languages, but (*) must hold to achieve type safety

Most generic subtype relationship

- if both S and T are record-like types (struct, class, etc.), $T \leq S$ holds if the following two conditions (†) are met
 1. T has all the (public) methods/fields of S
 2. for each public method m ,
type of m in $T \leq$ type of m in S

Subtype relationship example (1)

- `shape`
 - has `area()` method returning float
- `rect`
 - has `area()` method returning float
 - has additional `width()` and `height()` methods
- `rect ≤ shape` holds

Subtype relationship example (2)

- shape
 - has `area()` method returning float and
 - `perimeter()` method returning float
- rect is the same as before
- $\text{rect} \leq \text{shape}$ does not (*should not*) hold
- to see why, consider

```
s : shape = rect(..)
s.perimeter()
```

Subtype relationship tricky example (3)

- `shape`
 - has `area()` method returning float and
 - `eq(s : shape)` method returning bool
- `rect`
 - has `area()` method returning float,
 - has `width()` and `height()` method each returning float, and
 - `eq(r : rect)` method returning bool
- does `rect ≤ shape` hold?

Subtype relationship tricky example (3)

- no, it *should not* hold
- to see why not, consider

```
s : shape = rect(..)
s.eq(circle(..))
```

- which passes circle type to a formal argument of eq (rect type)

Subtype relationship tricky example (3)

- more algorithmically,

$\text{rect} \leq \text{shape}$

$\Rightarrow \text{type of eq in rect} \leq \text{type of eq in shape}$

$\Rightarrow \text{rect} \rightarrow \text{bool} \leq \text{shape} \rightarrow \text{bool}$

- in general, $a' \rightarrow b' \leq a \rightarrow b$ holds when
 - $b' \leq b$ and $a' \geq a$ (next slide)

$\Rightarrow \text{shape} \leq \text{rect}$ (false)

Subtype relationship between functions

- $a' \rightarrow b' \leq a \rightarrow b$ holds when
 - $b' \leq b$ and $a' \geq a$
- recall substitution principle (*)
 - assume $f' : a' \rightarrow b'$ and $f : a \rightarrow b$,
 - and ask when $f \leftarrow f'$ is safe?
- it is when “ f' can take any data f can take (a)”. i.e.,
 - $a' \geq a$ (a' is a *supertype* of a)

Covariant and contravariant

- in general, a type $T(\alpha)$ parameterized by α , is said to be
 - **covariant on α** if replacing α with its subtype α' yields its subtype (i.e., $\alpha' \leq \alpha \Rightarrow T(\alpha') \leq T(\alpha)$)
 - **contravariant on α** if replacing α with its supertype α' yields its subtype (i.e., $\alpha' \geq \alpha \Rightarrow T(\alpha') \leq T(\alpha)$)
- in this terminology, a function type is
 - *covariant* on output type ($b' \leq b \Rightarrow a \rightarrow b \leq a \rightarrow b'$)
 - *contravariant* on input type ($a' \leq a \Rightarrow a' \rightarrow b \leq a \rightarrow b$)

Taxonomy of subtype relationships

- **interface** subtyping vs. **concrete-type** subtyping
 - concrete-type subtyping (C++, Java, OCaml)
 - \leq is introduced between ordinary (concrete) types
 - interface subtyping (Go, Rust)
 - besides ordinary types, define *abstract types*, *interfaces* (Go), or *traits* (Rust)
 - \leq is introduced only between interfaces or between a concrete type and an interface

Taxonomy of subtype relationships

- **nominal** subtyping vs. **structural** subtyping
 - nominal (Rust)
 - \leq holds only when the programmer so specified explicitly
(`impl trait` for `struct`)
 - structural (Go, OCaml)
 - \leq is derived automatically from definitions

```
type Shape interface { area() float64 }  
type Rect struct { ... }  
func (r Rect) area() float64 { ... }
```

- with Go structural subtyping, $\text{Rect} \leq \text{Shape}$ is *automatically* established because `Rect` has an `area` method returning `float64`, allowing the following assignment

```
var s shape = rect{0, 0, 100, 100}
```

Subtyping in Rust

```
trait Shape { fn area(&self) -> f64; }  
struct Rect { ... }  
impl Shape for Rect {  
    fn area(&self) -> f64 { ... }  
}
```

- with Rust (nominal subtyping between struct and trait), $\text{Rect} \leq \text{Shape}$ is established by explicitly stating `impl Shape for Rect`, allowing the assignment below

```
let s : &dyn Shape = &Rect{ ... };
```

- OCaml does not require type (class) definitions to make objects
- when you define class, subtype relationship is automatically derived
- nor does it require type of variables to be specified
- ... everything just *naturally* happens (learn in the notebook)