



# Hog Contest Rules cs61a.org/proj/hog\_contest

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 Max of one entry per person

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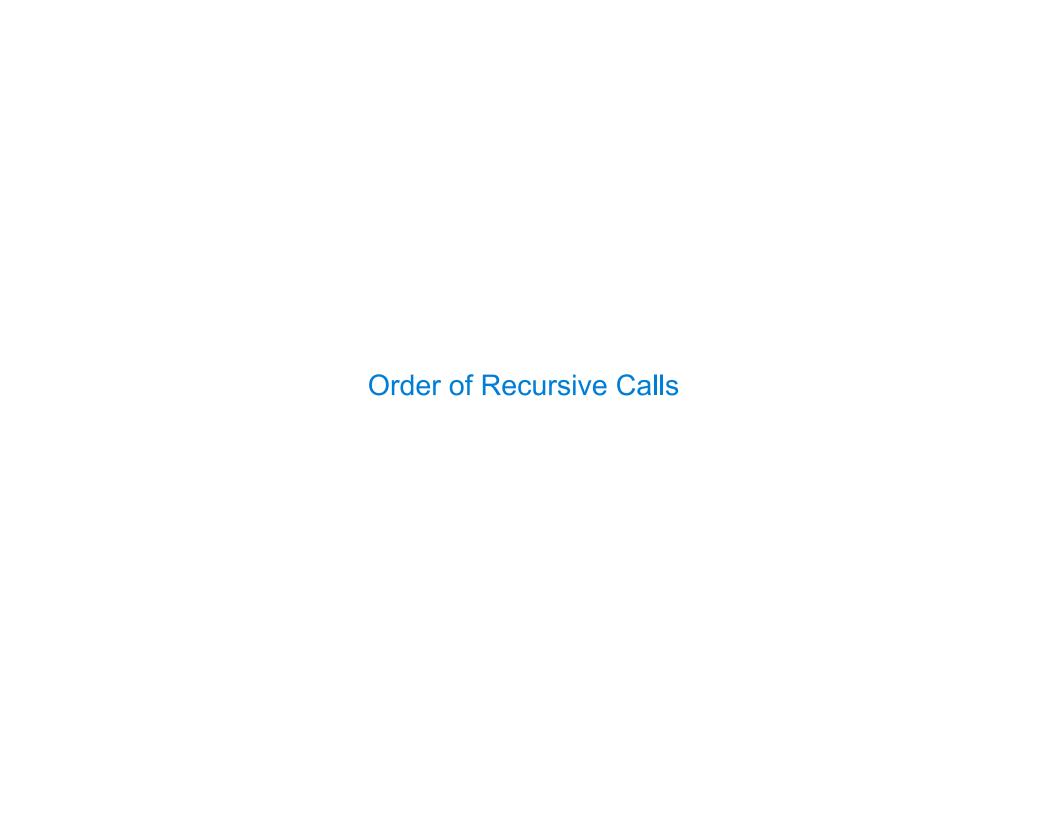
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```
1 def cascade(n):
2    if n < 10:
3        print(n)
4    else:
5        print(n)
6        cascade(n//10)
7        print(n)
8
9 cascade(123)</pre>
```

```
(Demo)

Global frame func cascade(n) [parent=Global]

cascade related for the cascade function of the
```

## Program output:

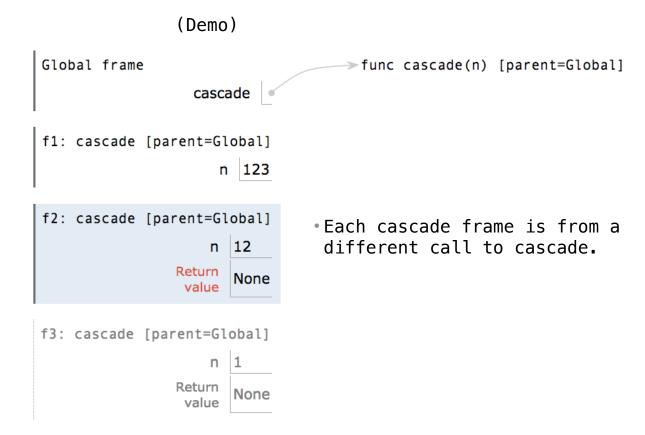
```
123
12
1
12
```

```
(Demo)
Global frame
                                     → func cascade(n) [parent=Global]
                  cascade
f1: cascade [parent=Global]
                     n 123
f2: cascade [parent=Global]
                    n 12
                Return
f3: cascade [parent=Global]
                Return
                 value
```

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## Program output:

| 123 |  |  |
|-----|--|--|
| 12  |  |  |
| 1   |  |  |
| 12  |  |  |
|     |  |  |

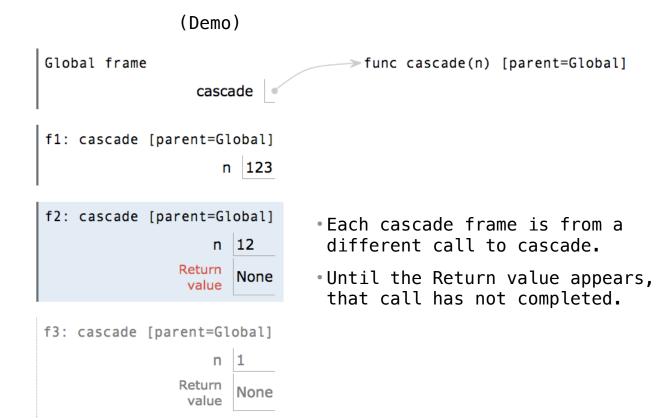


<u>Interactive Diagram</u>

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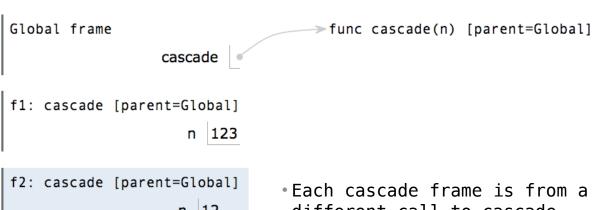
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|-----|--|
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|     |  |



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           print(n)
      else:
          print(n)
          cascade(n//10)
           print(n)
  cascade(123)
```

## Program output:

| 123 |  |
|-----|--|
| 12  |  |
| 1   |  |
| 12  |  |
|     |  |



- n 12 Return None value
- f3: cascade [parent=Global] Return value
- different call to cascade.
- Until the Return value appears, that call has not completed.
- Any statement can appear before or after the recursive call.

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1 def cascade(n):
2    if n < 10:
3        print(n)
4    else:
5        print(n)
6        cascade(n//10)
7        print(n)
8
9 cascade(123)</pre>
```

## Program output:

| 123 |  |  |
|-----|--|--|
| 12  |  |  |
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| 12  |  |  |
|     |  |  |

# 

n 12

(Demo)

- None Until the Return value appears, that call has not completed.
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different call to cascade.

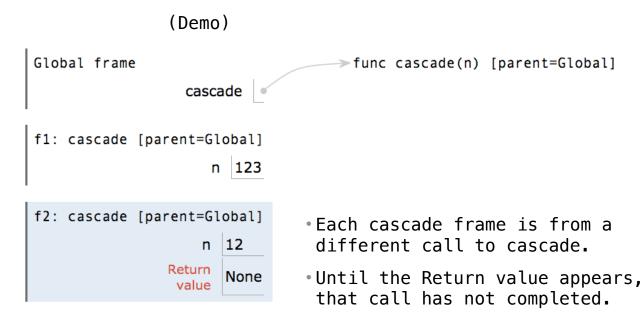
Return value

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| 1   |  |  |
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|     |  |  |

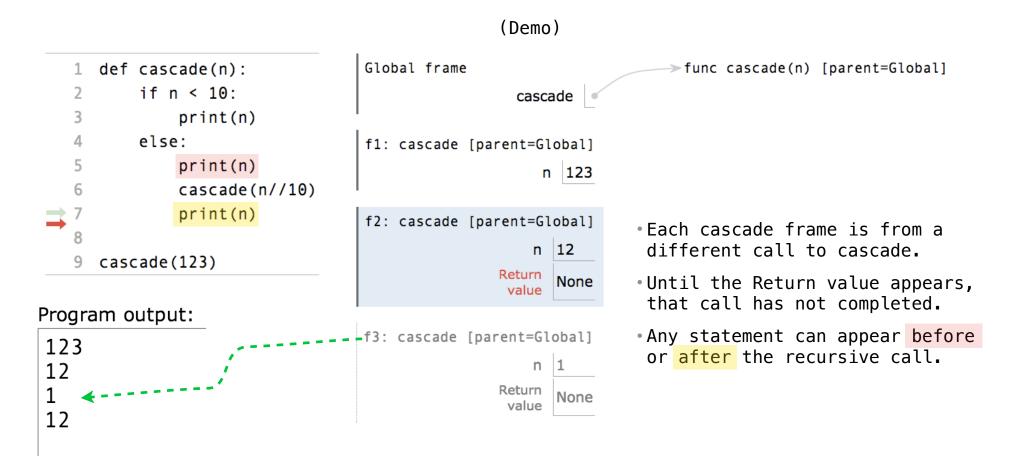


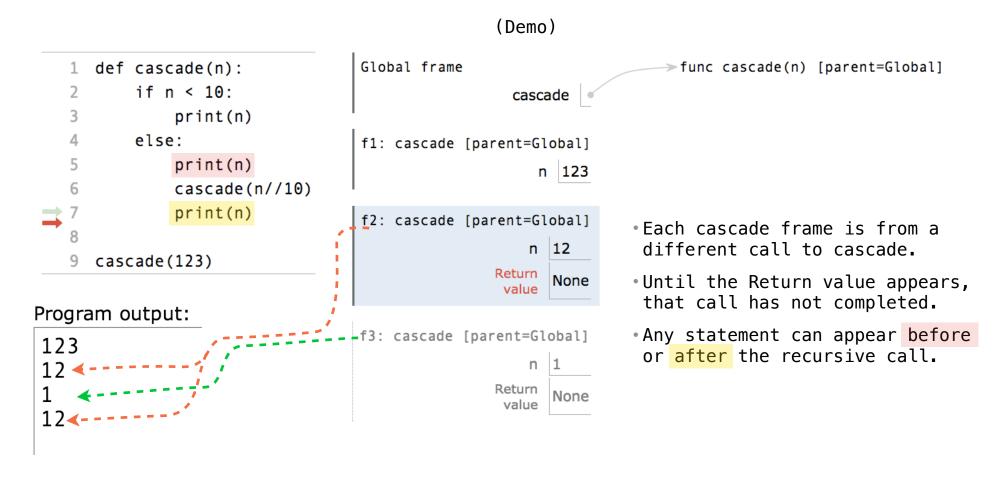
Any statement can appear before

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Return value

f3: cascade [parent=Global]





```
def cascade(n):
    if n < 10:
        print(n)
        print(n)
        if n >= 10:
        cascade(n/10)
        print(n)
        cascade(n//10)
        print(n)
```

(Demo)

If two implementations are equally clear, then shorter is usually better

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- In this case, the longer implementation is more clear (at least to me)

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- When learning to write recursive functions, put the base cases first

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- In this case, the longer implementation is more clear (at least to me)
- When learning to write recursive functions, put the base cases first
- Both are recursive functions, even though only the first has typical structure

Example: Inverse Cascade

# **Inverse Cascade**

Write a function that prints an inverse cascade:

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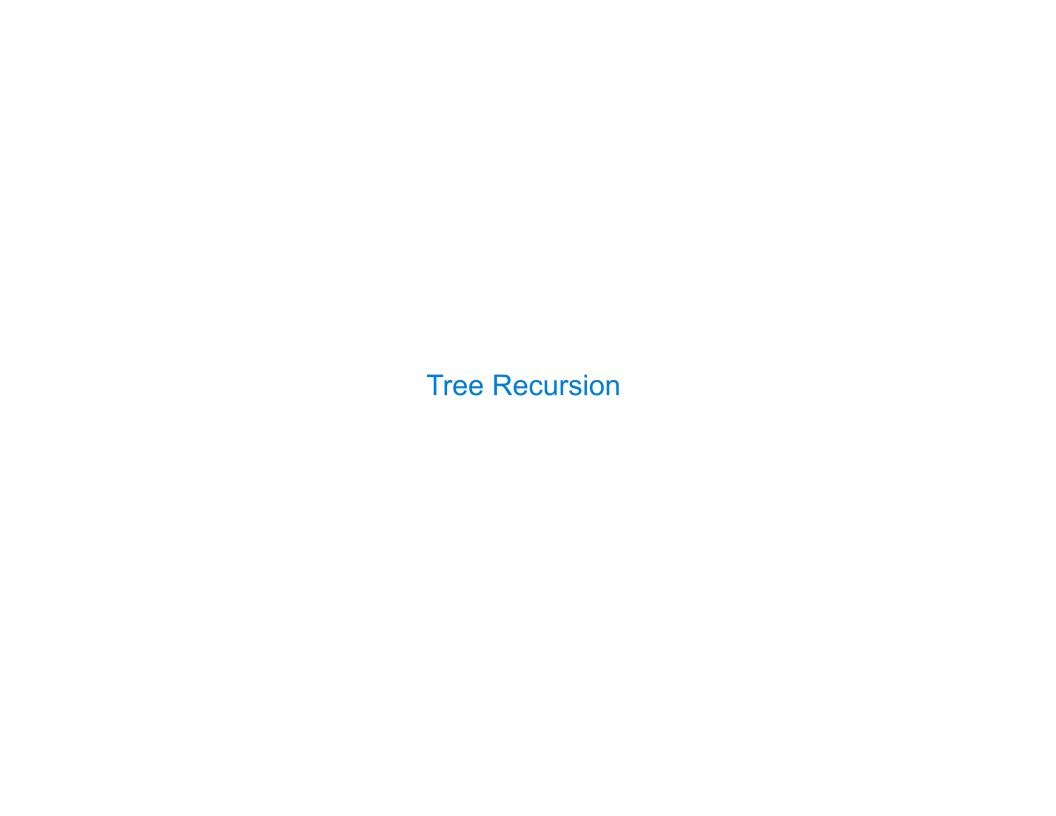
Write a function that prints an inverse cascade:

Write a function that prints an inverse cascade:

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Write a function that prints an inverse cascade:





Tree-shaped processes arise whenever executing the body of a recursive function makes more than one recursive call

**n:** 0, 1, 2, 3, 4, 5, 6, 7, 8,



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**n:** 0, 1, 2, 3, 4, 5, 6, 7, 8,

fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,



Tree-shaped processes arise whenever executing the body of a recursive function makes more than one recursive call

**n:** 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35

fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,



Tree-shaped processes arise whenever executing the body of a recursive function makes more than one recursive call

**n:** 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35

fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465



Tree-shaped processes arise whenever executing the body of a recursive function makes more than one recursive call

**n:** 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35

fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465

def fib(n):



```
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35

fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465
```

```
def fib(n):
    if n == 0:
```



```
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35

fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465
```

```
def fib(n):
    if n == 0:
        return 0
```



```
n: 0, 1, 2, 3, 4, 5, 6, 7, 8, ..., 35

fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465
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def fib(n):
    if n == 0:
        return 0
    elif n == 1:
```



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    elif n == 1:
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    else:
```



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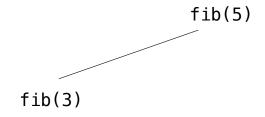
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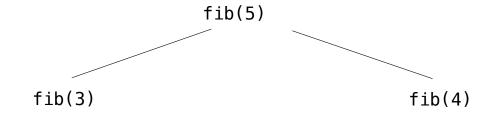
```
def fib(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return fib(n-2) + fib(n-1)
```



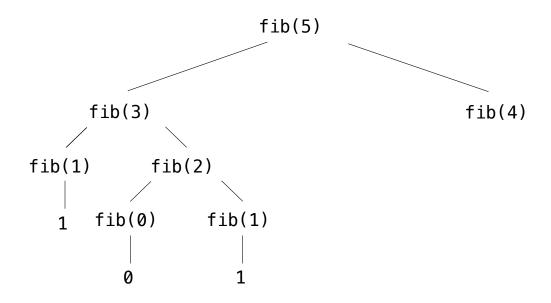
The computational process of fib evolves into a tree structure

fib(5)

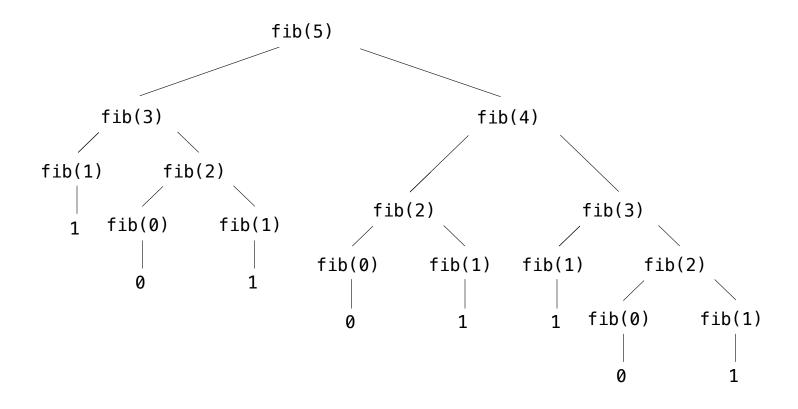


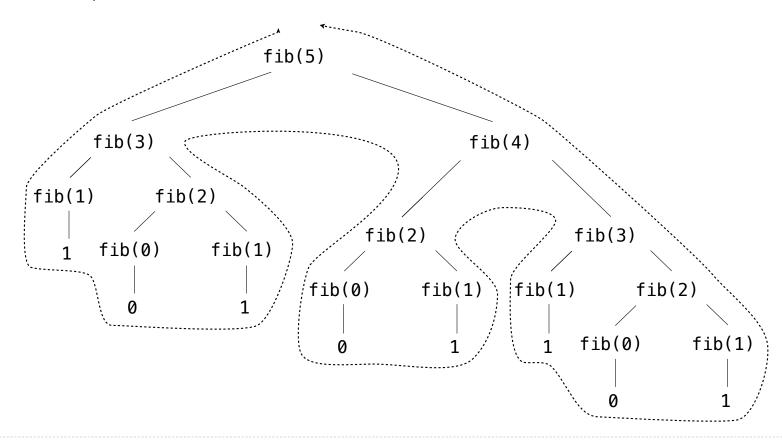


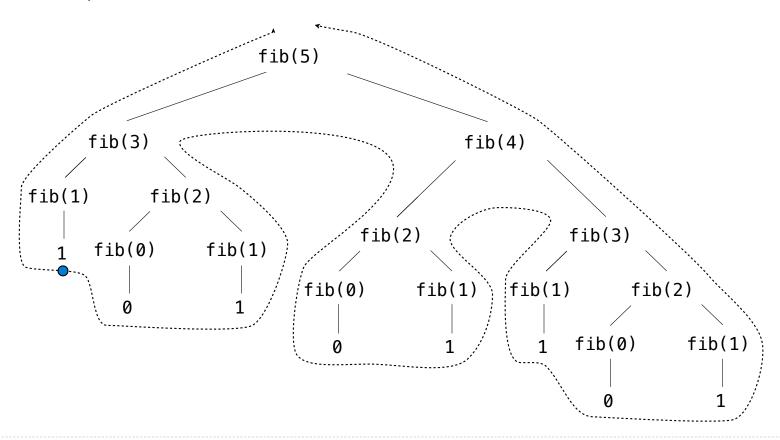
The computational process of fib evolves into a tree structure

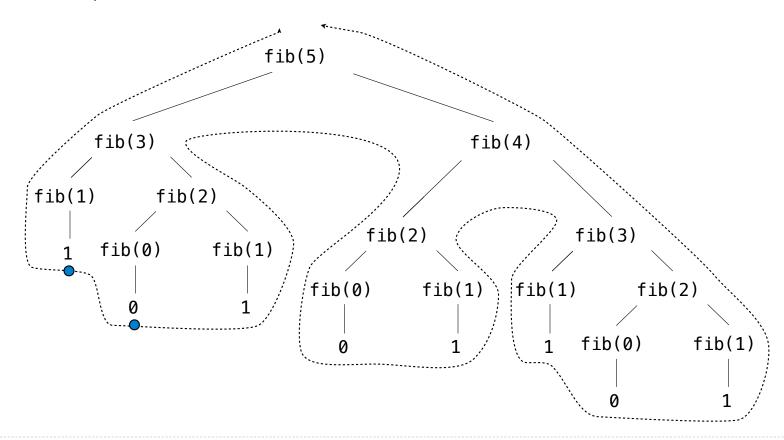


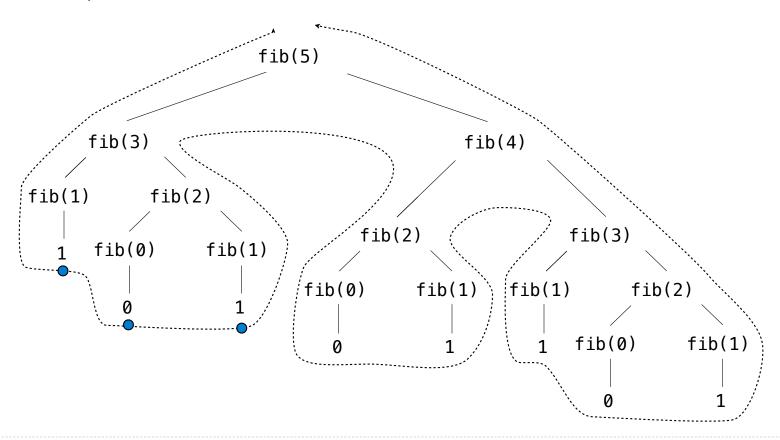
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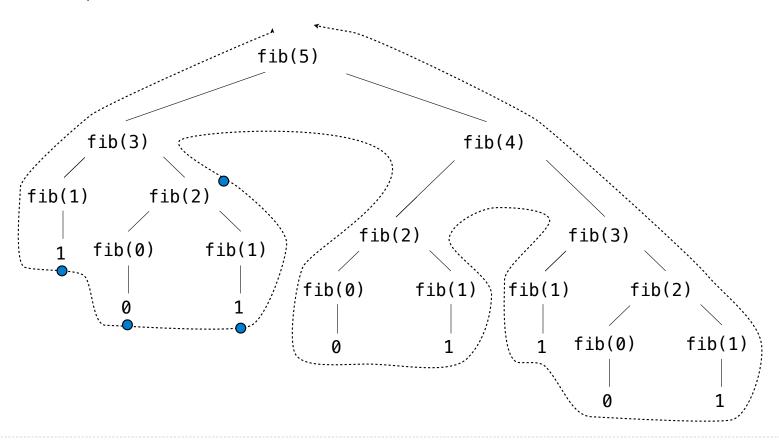


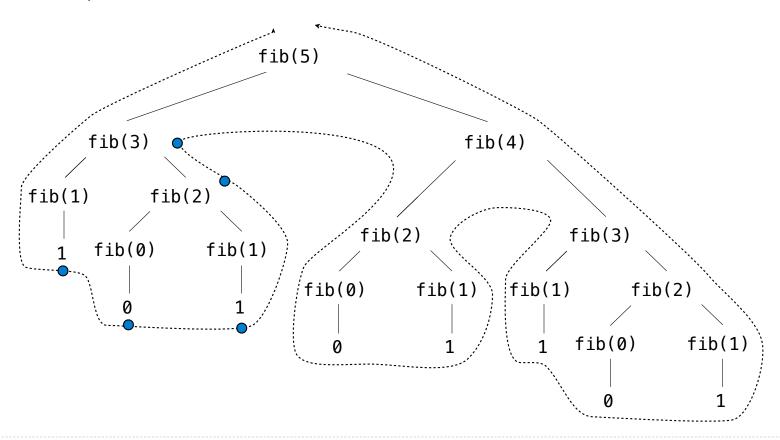


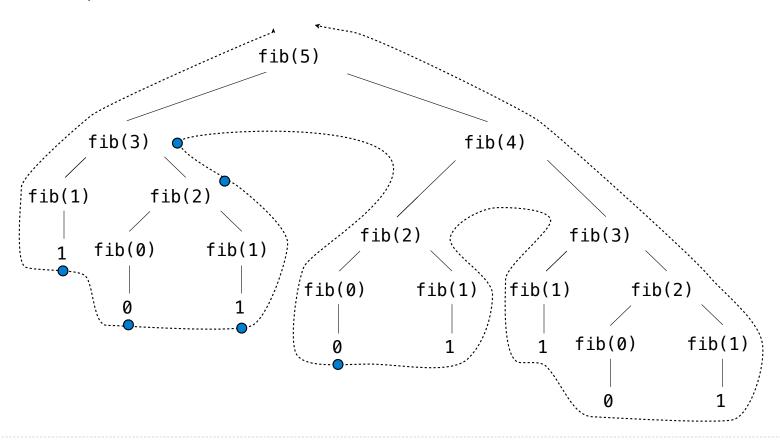


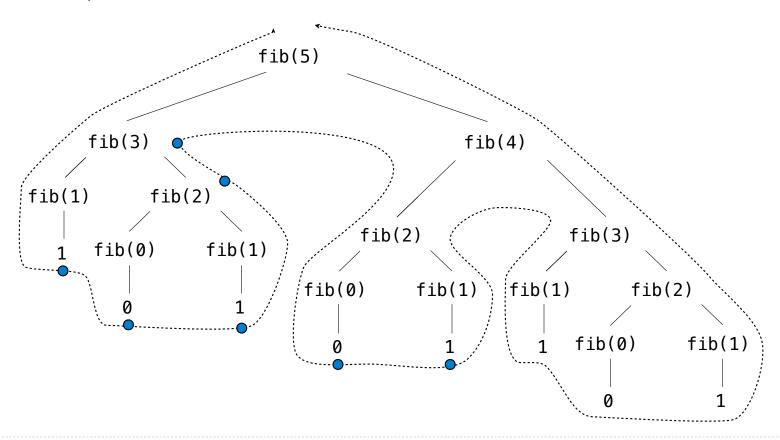


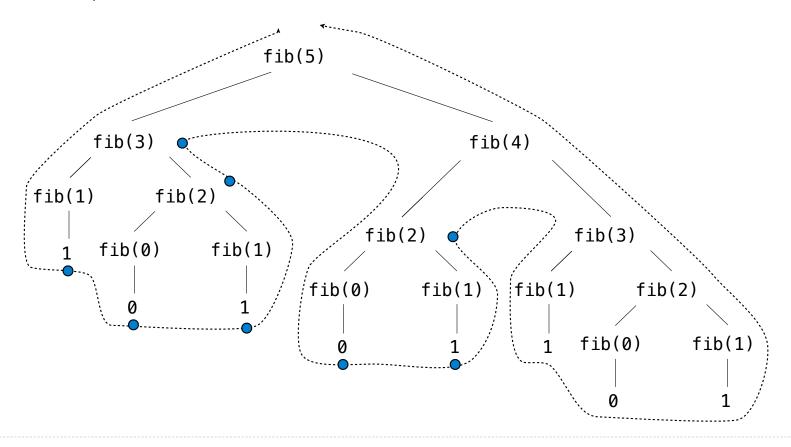


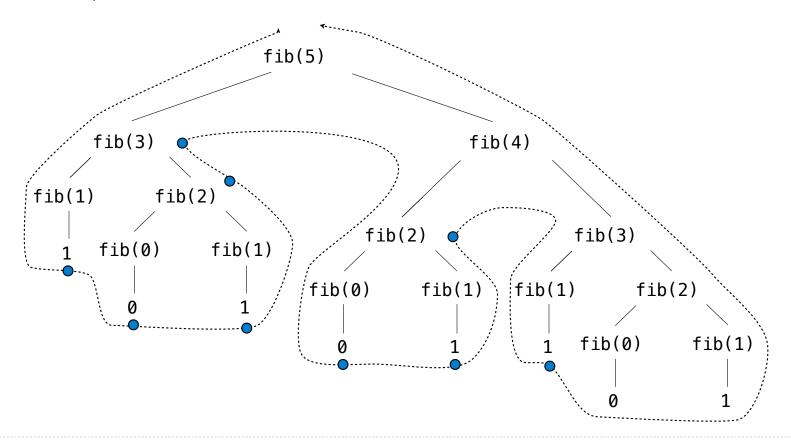


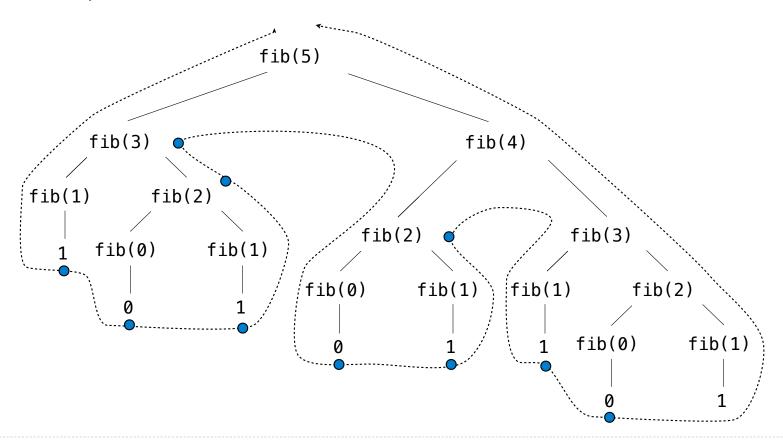


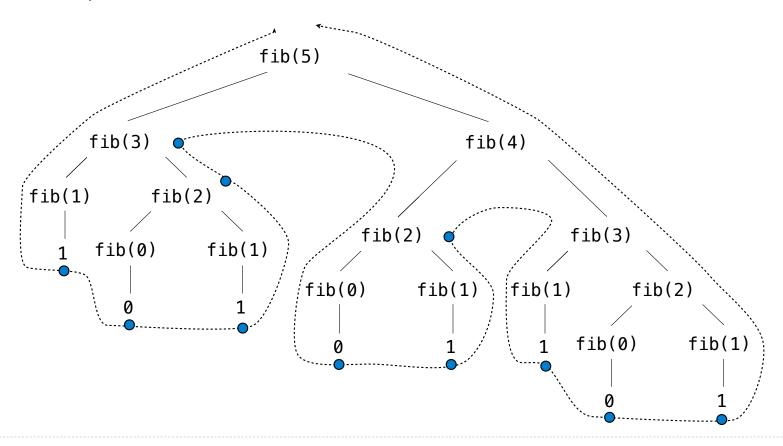


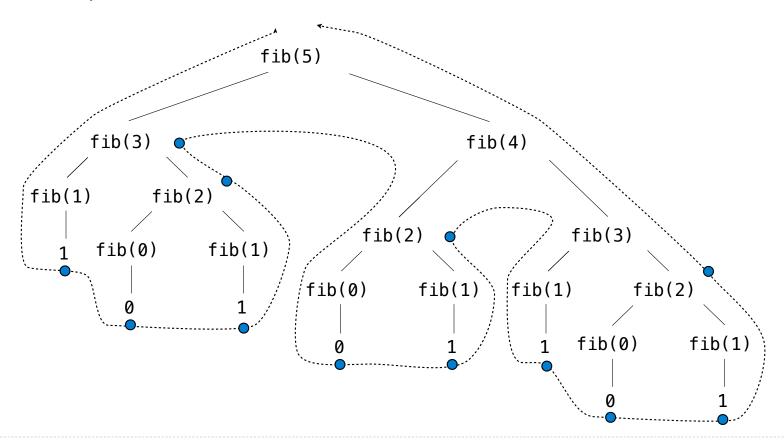


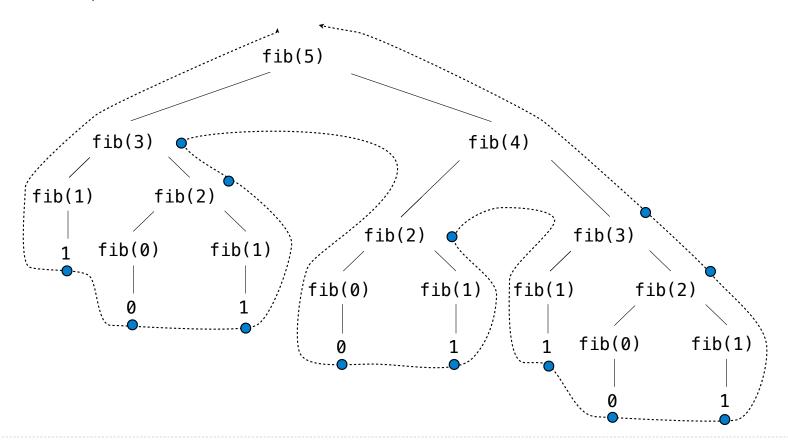


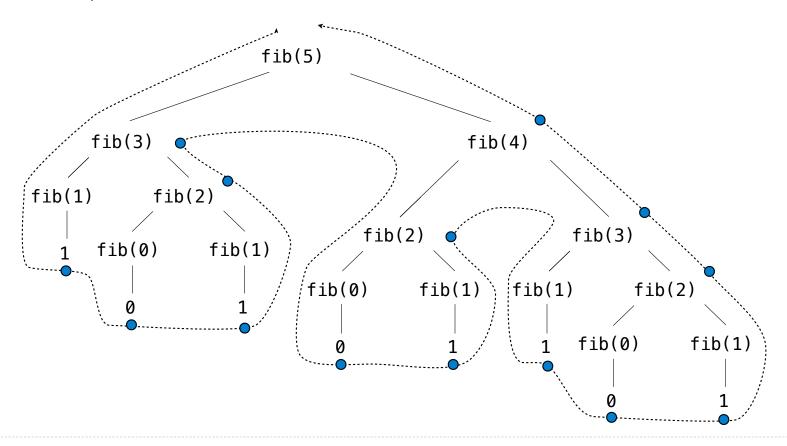


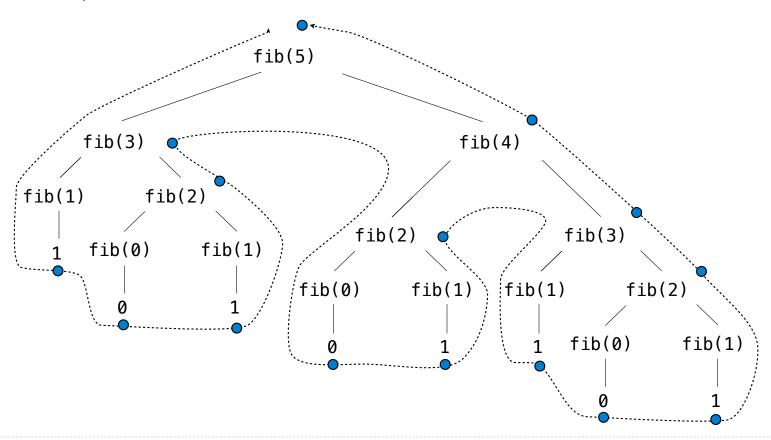


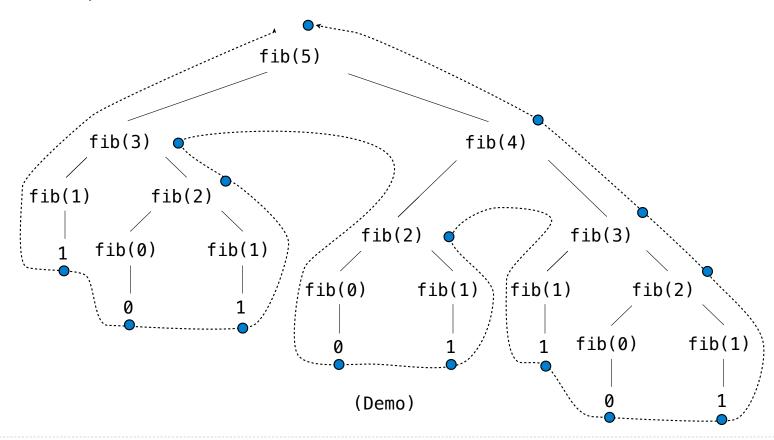












# Repetition in Tree-Recursive Computation

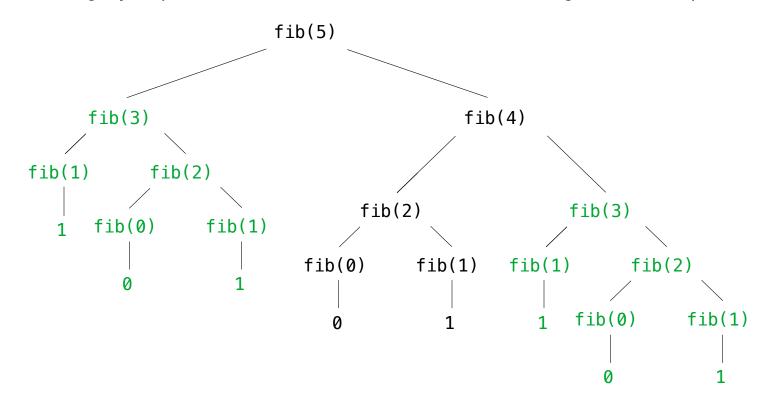
| Repetition in | Tree-Recursive | Computation |
|---------------|----------------|-------------|
|---------------|----------------|-------------|

This process is highly repetitive; fib is called on the same argument multiple times

12

# Repetition in Tree-Recursive Computation

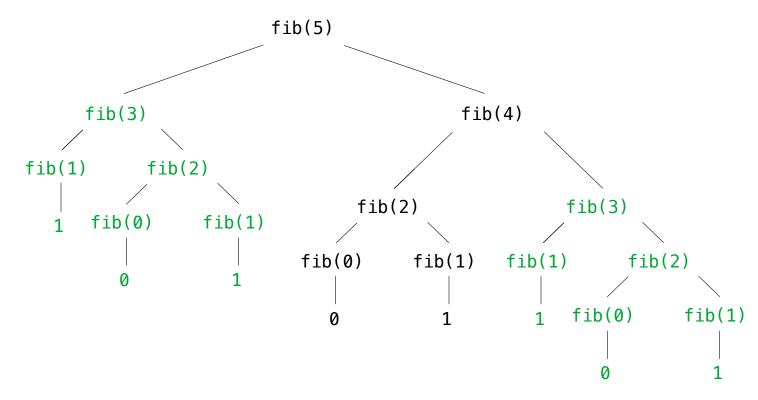
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# Repetition in Tree-Recursive Computation

This process is highly repetitive; fib is called on the same argument multiple times



(We will speed up this computation dramatically in a few weeks by remembering results)

**Example: Counting Partitions** 

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

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$$2 + 4 = 6$$

$$1 + 1 + 4 = 6$$

$$3 + 3 = 6$$

$$1 + 2 + 3 = 6$$

$$1 + 1 + 1 + 3 = 6$$

$$2 + 2 + 2 = 6$$

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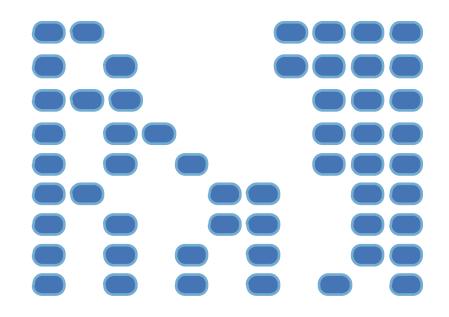
$$1 + 1 + 1 + 1 + 2 = 6$$

$$1 + 1 + 1 + 1 + 1 + 1 = 6$$

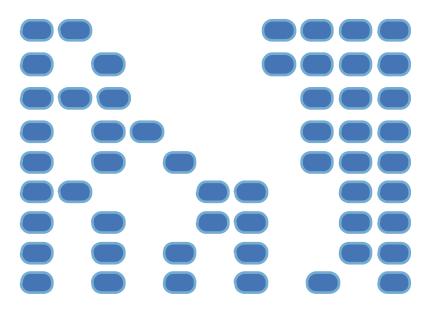




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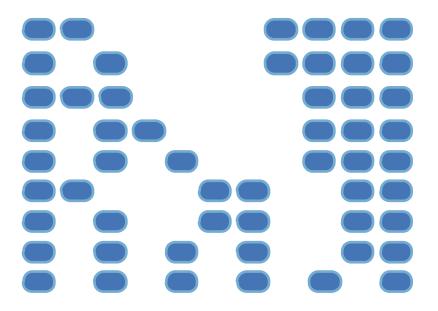
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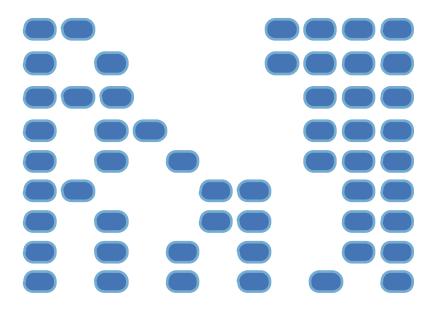
count\_partitions(6, 4)

 Recursive decomposition: finding simpler instances of the problem.



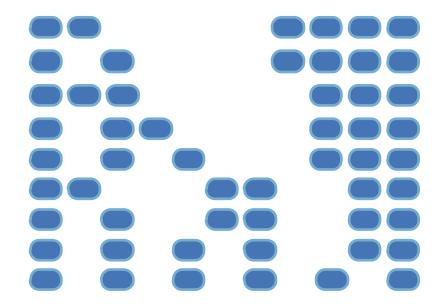
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- Recursive decomposition: finding simpler instances of the problem.
- •Explore two possibilities:



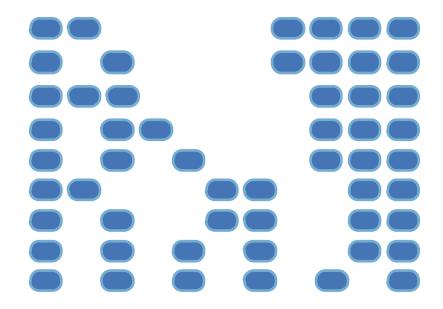
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- •Use at least one 4



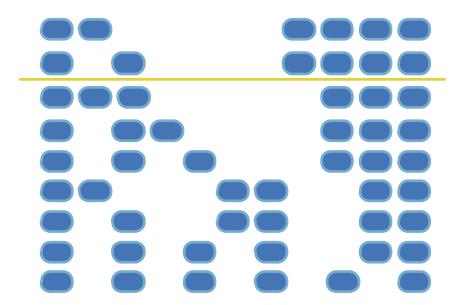
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- •Don't use any 4



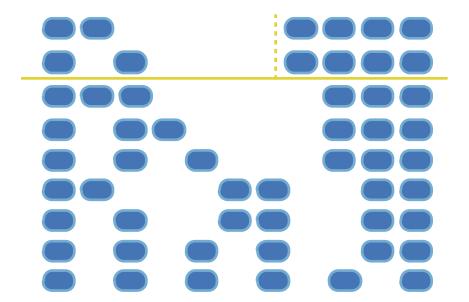
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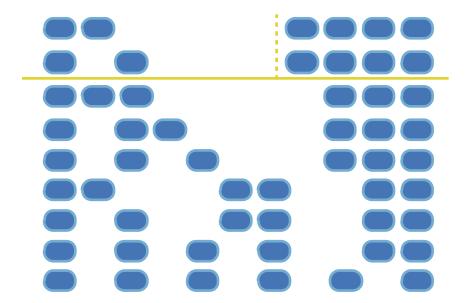
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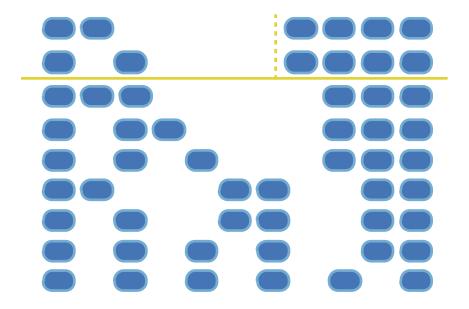
The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

- Recursive decomposition: finding simpler instances of the problem.
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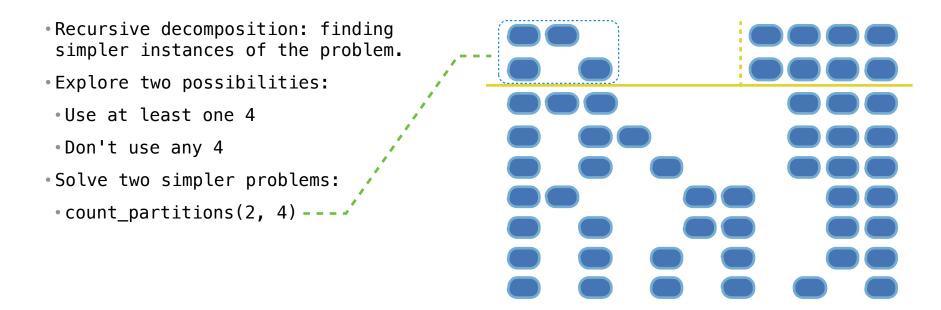


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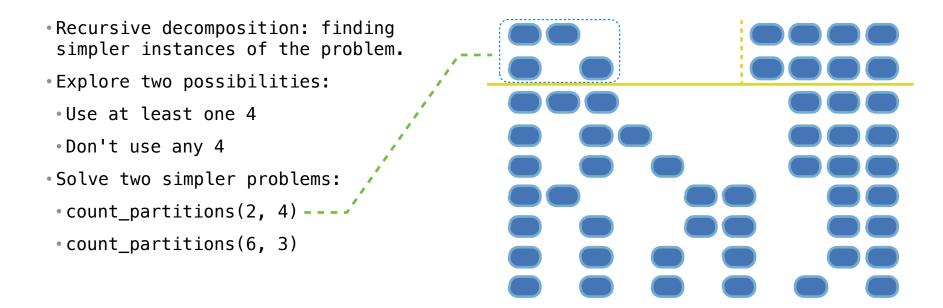
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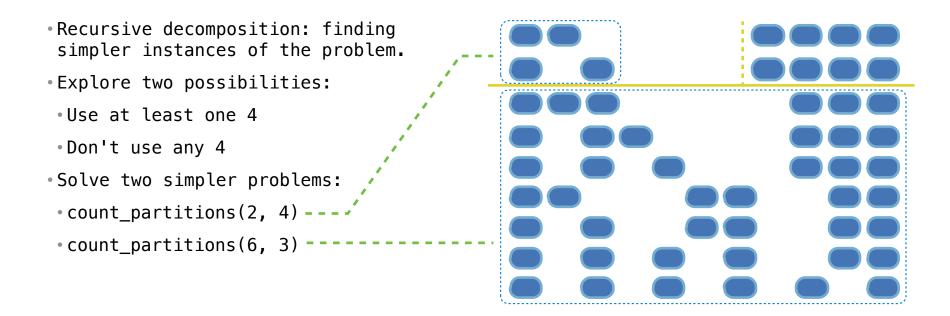
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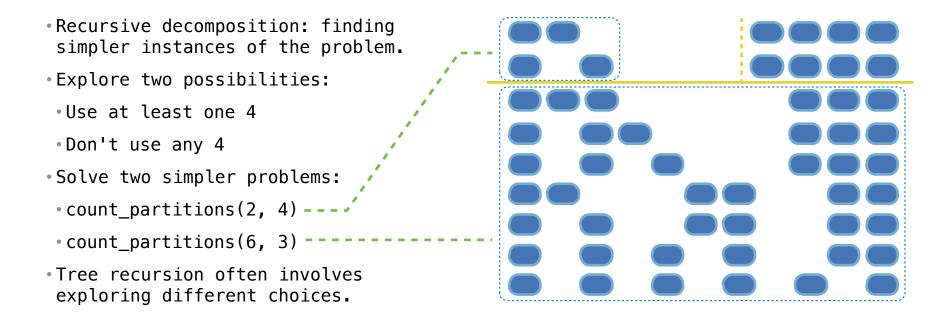
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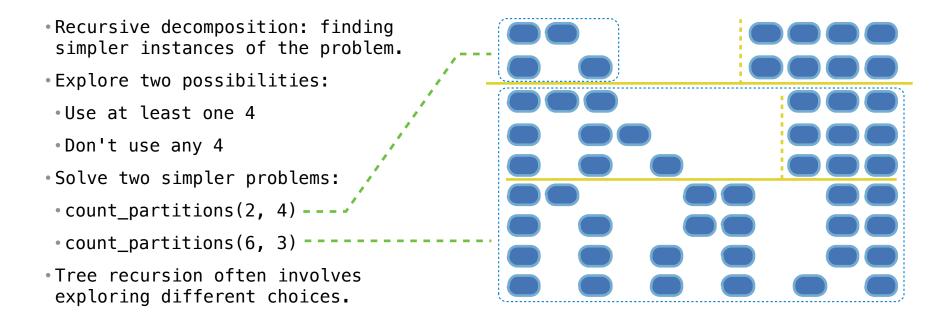
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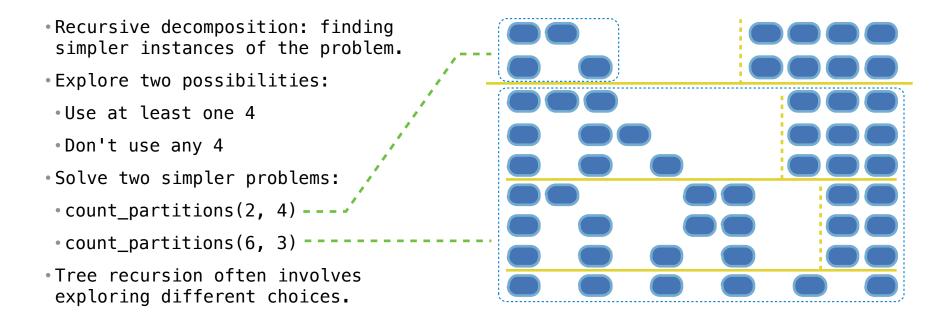
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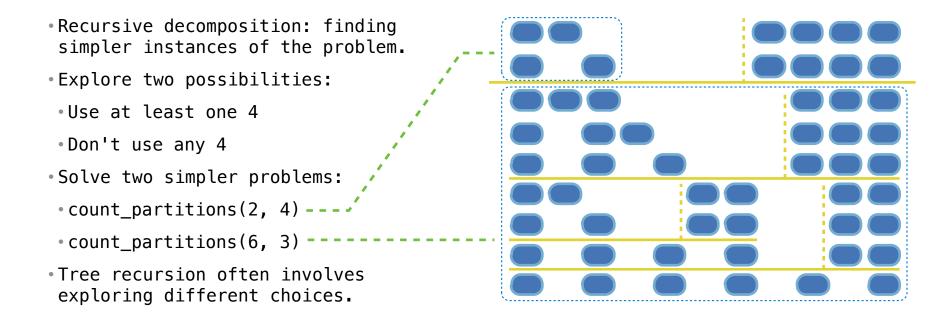
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### Count_partitio
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```
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def count partitions(n, m):

with m = count partitions(n-m, m)without m = count partitions(n, m-1)

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def count_partitions(n, m):
```

```
else:
```

```
with_m = count_partitions(n-m, m)
without_m = count_partitions(n, m-1)
return with_m + without_m
```

```
def count partitions(n, m):

    Recursive decomposition: finding

                                     if n == 0:
simpler instances of the problem.
                                        return 1
•Explore two possibilities:
                                     elif n < 0:
•Use at least one 4
•Don't use any 4
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•count_partitions(2, 4) ------ with_m = count_partitions(n-m, m)
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                                      (Demo)
```

<u>Interactive Diagram</u>