ECON1310 Introductory Statistics for Social Sciences

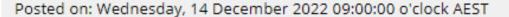
Tutorial 4: PROBABILITY II

Tutor: Francisco Tavares Garcia



CML 01 and CML 02.

CML 1 and 2 Reminder



Dear Students,

A reminder that:

- 1. CML 1 (2nd Attempt) is now open and will close at 4pm this Friday (16 December)
- 2. CML 2 (1st Attempt) is now open and will close at 4pm on Monday 19 December (Week 4)
- 3. Please note that you MUST check, save and submit your CMLs, are they do not auto-submit.
- Familiarise yourselves with the CML Information Sheet (Assessment > CML Quizzes > CML Administrative Folder), which contains CML rules, how questions are marked, and how to access your CML answers (once they have closed) etc.
- You are now able to view your answers for CML 1 (1st Attempt) under 'My Grades' in Blackboard. Page 7 of the CML Information Sheet outlines instructions for this

Feel free to email me if you have any questions.

Best of luck!

Dominic



LBRT 01 – First week of 2023!

LBRT #1

Type: Online Quiz

Learning Objectives Assessed: 1, 2, 3, 4, 5

Due Date: 03 Jan 23 9:00 - 04 Jan 23 16:00 2nd attempt: 5-6 Jan 2023, 09:00-16:00

Weight: 20%

Reading: 0 minutes

Duration: 90 minutes

Format: Multiple-choice, Problem solving

Task Description:

LBRT #1 will involve solving problems based on the learning materials covered in Lectures 1 to 4 inclusively. This includes all learning materials presented in Lectures 1 to 4 and the associated tutorials, as well as CML1 and CML2. All answers must be entered into Blackboard by the due date and time.

Criteria & Marking:

UQ Students: Please access the profile from Learn.UQ or mySI-net to access marking criteria held in this profile.



Stats from Tutorial 03:

Students attending: **34** (33)

- Students enrolled in this tutorial: **32** (28)
- Students not enrolled: **2** (5) (Welcome!)
 - If you haven't yet, please email d.byrne@uq.edu.au to inform him you would like to attend this tutorial (4 pm).

Time Spent (total time per student – multiple logins added)

- Max time: 95 (100) minutes (Francisco 107 min)
- Min time: 23 (10) minutes (does it count as attending?)
- Mean time: **77.88** (82.6) minutes
- Standard deviation: **12.3** (15.7) minutes

Poll participation

- Answered all 3+ polls: **15** (27)
- 2 polls: **11** (3) students
- 1 poll: **3** (0) students
- 0 polls: **5** (3) students



ECON1310 Tutorial 4 – Week 5

PROBABILITY II

At the end of this tutorial you should be able to

- Construct a discrete probability distribution.
- Calculate the mean and variance for a discrete probability distribution.
- Describe the characteristics of a binomial distribution.
- Calculate the probability of a particular outcome of a binomial distribution using a calculator.



Q1. The number of car radios sold each week by a large company has been recorded for the past 100 weeks. No radios have been sold in 3 of the weeks. One radio has been sold in 20 of the weeks. Two radios in 50 of the weeks, three in 20, four in 5 and five in two of the weeks. No more than five radios were sold in any of the past 100 weeks. Construct a probability distribution for the number of car radios sold in a week using the relative frequencies as probabilities. In the long run what is the average and standard deviation of number of car radios sold per week?

(Excel)



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P(X)
0.03
0.2
0.5
0.2
0.05
0.02

(Poll)



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P(X)
0.03
0.2
0.5
0.2
0.05
0.02

Average μ (mu)
0
0.2
1
0.6
0.2
0.1
2.1



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X	P(X)
0	0.03
1	0.2
2	0.5
3	0.2
4	0.05
5	0.02

Variance σ^2
(sigma squared)
0.1323
0.242
0.005
0.162
0.1805
0.1682
0.89



Q1. The number of car radios sold each week by a large company has been recorded for the past 100 weeks. No radios have been sold in 3 of the weeks. One radio has been sold in 20 of the weeks. Two radios in 50 of the weeks, three in 20, four in 5 and five in two of the weeks. No more than five radios were sold in any of the past 100 weeks. Construct a probability distribution for the number of car radios sold in a week using the relative frequencies as probabilities. In the long run what is the average and standard deviation of number of car radios sold per week?

X	P(X)
0	0.03
1	0.2
2	0.5
3	0.2
4	0.05
5	0.02

Average μ (mu)	
ο O	
0.2	
1	
0.6	
0.2	
0.1	
2.1	

Variance σ^2
(sigma squared)
0.1323
0.242
0.005
0.162
0.1805
0.1682
0.89

Standard Deviation	
σ (sigma)	
0.9434	



- Q2. A travel company is considering introducing a new package tour. Based on market research, if sales are high, they can make a profit of 107 thousand dollars per year on the new route. Moderate sales would mean they can make \$35 thousand, whereas poor sales would imply a loss of \$37 thous per year. If the probabilities for the profit scenarios are 0.57 and 0.31, respectively,
 - a. Determine the expected profit
 - b. Determine the standard deviation of profit



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 - a. Determine the expected profit $E(X) = \mu = ?$
 - b. Determine the standard deviation of profit

(Poll)



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 - a. Determine the expected profit $E(X) = \mu = ?$
 - b. Determine the standard deviation of profit

P(X)
0.57
0.31
0.12



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 - a. Determine the expected profit $E(X) = \mu = 67.4$
 - b. Determine the standard deviation of profit

0.57	60.99
0.31	10.85
0.12	-4.44
	67.4



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 - a. Determine the expected profit $E(X) = \mu = 67.4$
 - b. Determine the standard deviation of profit $sd(X) = \sigma = \sqrt{\sigma^2} = \sqrt{var(X)} = ?$

X	P(X)	Average μ (mu)
107	0.57	60.99
35	0.31	10.85
-37	0.12	-4.44
		67.4



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 - a. Determine the expected profit $E(X) = \mu = 67.4$
 - b. Determine the standard deviation of profit $sd(X) = \sigma = \sqrt{\sigma^2} = \sqrt{var(X)} = 50.27$ (\$th)

X	P(X)	Average μ (mu)
107	0.57	60.99
35	0.31	10.85
-37	0.12	-4.44
		67.4

Variance σ^2				
(sigma squared)				
893.8512				
325.4256				
1307.9232				
2527.2				

Standard Deviation σ (sigma) 50.2713



- Q3. (i) It was thought that 32% of people preferred Pepsi to Coke. Thirty-five people participated in a Pepsi versus Coke taste test. Each person was given two samples and asked to say which they preferred.
 - a) Is this a binomial situation? What are the properties of the binomial distribution?
 - b) What is the expected number of participants preferring Pepsi?
 - c) What is the variance of the distribution?

(Poll)



- Q3. (i) It was thought that 32% of people preferred Pepsi to Coke. Thirty-five people participated in a Pepsi versus Coke taste test. Each person was given two samples and asked to say which they preferred.
 - a) Is this a binomial situation? What are the properties of the binomial distribution? Yes
 - b) What is the expected number of participants preferring Pepsi?
 - c) What is the variance of the distribution?
- 1) The trials are identical each person was given two samples.
- 2) Two possible outcomes either Pepsi or Coke.
- 3) Trials are independent random people participated.
- 4) Constant probability thought that 32% of people preferred Pepsi.



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 - b) What is the expected number of participants preferring Pepsi?
 - c) What is the variance of the distribution?



- Q3. (i) It was thought that 32% of people preferred Pepsi to Coke. Thirty-five people participated in a Pepsi versus Coke taste test. Each person was given two samples and asked to say which they preferred.
 - a) Is this a binomial situation? What are the properties of the binomial distribution? Yes
 - b) What is the expected number of participants preferring Pepsi?
 - c) What is the variance of the distribution?

expected number of successes = $E(X) = \mu = ?$



- Q3. (i) It was thought that 32% of people preferred Pepsi to Coke. Thirty-five people participated in a Pepsi versus Coke taste test. Each person was given two samples and asked to say which they preferred.
 - a) Is this a binomial situation? What are the properties of the binomial distribution? Yes
 - b) What is the expected number of participants preferring Pepsi? 11.2
 - c) What is the variance of the distribution?

expected number of successes = $E(X) = \mu = n^*p = 35^*0.32 = 11.2$



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 - a) Is this a binomial situation? What are the properties of the binomial distribution? Yes
 - b) What is the expected number of participants preferring Pepsi? 11.2
 - c) What is the variance of the distribution?

expected number of successes = $E(X) = \mu = n^*p = 35^*0.32 = 11.2$

variance =
$$var(X) = \sigma^2 = ?$$



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 - a) Is this a binomial situation? What are the properties of the binomial distribution? Yes
 - b) What is the expected number of participants preferring Pepsi? 11.2
 - c) What is the variance of the distribution?

expected number of successes = $E(X) = \mu = n^*p = 35^*0.32 = 11.2$

variance =
$$var(X) = \sigma^2 = n^*p^*q = ?$$



- Q3. (i) It was thought that 32% of people preferred Pepsi to Coke. Thirty-five people participated in a Pepsi versus Coke taste test. Each person was given two samples and asked to say which they preferred.
 - a) Is this a binomial situation? What are the properties of the binomial distribution? Yes
 - b) What is the expected number of participants preferring Pepsi? 11.2
 - c) What is the variance of the distribution? 7.62

expected number of successes =
$$E(X) = \mu = n^*p = 35^*0.32 = 11.2$$

variance =
$$var(X) = \sigma^2 = n^*p^*q = n^*p^*(1 - p) = 35^*0.32^*0.68 = 7.62$$

standard deviation =
$$sd(X) = \sigma = \sqrt{\sigma^2} = \sqrt{var(X)} = 2.76$$



Q4. Use your calculator to find (binomial) $P(X=9 \mid n=14, p=0.4)$ and $P(X<3 \mid n=11, p=0.65)$



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Understanding the Binomial Formula

A coin is tossed three times. What is the probability of getting 2 heads?

$$P(X) = {^{n}C_{X}p^{X}q^{(n-X)}}$$

n = 3

p = probability of getting heads = 0.5

X = number of heads = 2 3 combinations of two heads and a tail

$${}^{3}C_{2} = \frac{3*2}{2*1} = 3$$
 (use calculator in ECON1310)

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Understanding the Binomial Formula

$$P(X = 0) = {}^{3}C_{0} * 0.5^{0} * 0.5^{(3-0)}$$
(no heads) = 1* 0.5⁰ * 0.5³

$$= 1*1*(1/2)^{3}$$

$$= 0.125$$

$$P(X = 1) = {}^{3}C_{1} * 0.5^{1} * 0.5^{(3-1)}$$
(one head) = $3 * 0.5^{1} * 0.5^{2}$
= $3 * 1/2 * 1/4$
= $3/8 = 0.375$

(Excel)



Q4. Use your calculator to find (binomial) $P(X=9 \mid n=14, p=0.4)$ and $P(X<3 \mid n=11, p=0.65)$

Understanding the Binomial Formula

A coin is tossed three times. What is the probability of getting 2 heads?

$$P(X) = {^{n}C_{X}p^{X}q^{(n-X)}}$$

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 (use calculator in ECON1310)

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Understanding the Binomial Formula

$$P(X = 0) = {}^{3}C_{0} * 0.5^{0} * 0.5^{(3-0)}$$

(no heads) $= 1*0.5^{0} * 0.5^{3}$
 $= 1*1*(1/2)^{3}$
 $= 0.125$

$$P(X = 1) = {}^{3}C_{1} * 0.5^{1} * 0.5^{(3-1)}$$

(one head) $= 3 * 0.5^{1} * 0.5^{2}$
 $= 3 * 1/2 * 1/4$
 $= 3/8 = 0.375$



- Q5. A life insurance salesman has arranged to call on three households tomorrow. Based on past experience, he feels there is a 20% chance of closing a sale on each call, and that the outcome of each call is independent of the others. Let X represent the number of sales he would close tomorrow.
 - a. Does this situation satisfy all of the binomial properties? Explain. State the parameters.
 - b. Determine the probability distribution of X.
 - c. Find the probability that more than one sale will be closed tomorrow.

(Poll)



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 - a. Does this situation satisfy all of the binomial properties? Explain. State the parameters. Yes
 - b. Determine the probability distribution of X.
 - c. Find the probability that more than one sale will be closed tomorrow.

- 1) The trials are identical call three households.
- 2) Two possible outcomes close the sale or not.
- 3) Trials are independent the outcome of each call is independent of the others.
- 4) Constant probability 20% chance of closing a sale on each call.



- Q5. A life insurance salesman has arranged to call on three households tomorrow. Based on past experience, he feels there is a 20% chance of closing a sale on each call, and that the outcome of each call is independent of the others. Let X represent the number of sales he would close tomorrow.
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 - a. Does this situation satisfy all of the binomial properties? Explain. State the parameters. Yes
 - b. Determine the probability distribution of X.
 - c. Find the probability that more than one sale will be closed tomorrow.

$$P(X=x \mid n=3, p=0.2) = ?$$



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 - a. Does this situation satisfy all of the binomial properties? Explain. State the parameters. Yes
 - b. Determine the probability distribution of X.
 - c. Find the probability that more than one sale will be closed tomorrow.

Number of sales X	0	1	2	3
P(X)	0.512	0.384	0.096	0.008



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 - c. Find the probability that more than one sale will be closed tomorrow.

Number of sales X	0	1	2	3
P(X)	0.512	0.384	0.096	0.008

$$P(X>1) = ?$$



- Q5. A life insurance salesman has arranged to call on three households tomorrow. Based on past experience, he feels there is a 20% chance of closing a sale on each call, and that the outcome of each call is independent of the others. Let X represent the number of sales he would close tomorrow.
 - a. Does this situation satisfy all of the binomial properties? Explain. State the parameters. Yes
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 - c. Find the probability that more than one sale will be closed tomorrow.

Number of sales X	0	1	2	3
P(X)	0.512	0.384	0.096	0.008

$$P(X>1) = P(X>=2) = ?$$

 $P(X>1) = 1 - P(X <= 1)$



- Q5. A life insurance salesman has arranged to call on three households tomorrow. Based on past experience, he feels there is a 20% chance of closing a sale on each call, and that the outcome of each call is independent of the others. Let X represent the number of sales he would close tomorrow.
 - a. Does this situation satisfy all of the binomial properties? Explain. State the parameters. Yes
 - b. Determine the probability distribution of X.
 - c. Find the probability that more than one sale will be closed tomorrow.

Number of sales X	0	1	2	3
P(X)	0.512	0.384	0.096	0.008

$$P(X>1) = P(X>=2) = 0.096 + 0.008 = 0.104$$



ECON1310 Tutorial 4 – Week 5

PROBABILITY II

At the end of this tutorial you should be able to

- Construct a discrete probability distribution.
- Calculate the mean and variance for a discrete probability distribution.
- Describe the characteristics of a binomial distribution.
- Calculate the probability of a particular outcome of a binomial distribution using a calculator.



Thank you

Francisco Tavares Garcia

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Reference

Black et al. (2016), Australasian Business Statistics, 4th Edition, Wiley Australia.

CRICOS code 00025B

