ECON2300 - Introductory Econometrics

Tutorial 2: Linear Regression with a Single Regressor

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Do you have the latest versions of R and RStudio?

Install R – 4.4.3

https://cran.r-project.org/

Install RStudio – 2024.12.1+563

https://posit.co/download/rstudiodesktop/

Update all packages –

In RStudio >>

Tools >>

Check for Package Updates >>

Select All >>

Install Updates



Quiz 1 is available!

Quiz 1 Now Available



Dear ECON2300 Students,

Quiz 1 is now available in the Quizzes folder, which you can access via the Assessment tab.

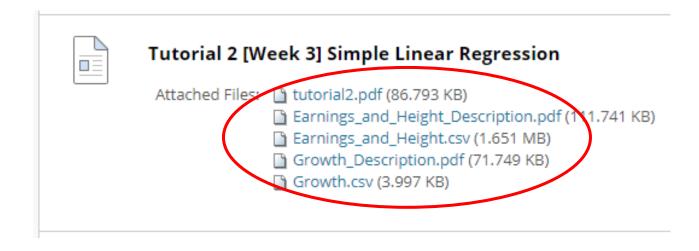
The due date for Quiz 1 is Friday, March 14, 2025, 4pm. If there is any change of the due date, we'll let you know.

Please read all instructions carefully before commencing the quiz.

Stay Safe.



- Download the files for tutorial 02 from Blackboard,
- save them into a folder for this tutorial.





Now, let's download the script for the tutorial.

- Copy the code from Github,
 - https://github.com/tavaresgarcia/teaching
- Save the scripts in the same folder as the data.



E4.1 The file Growth.csv contains data on average growth rates from 1960 through 1995 for 65 countries, along with variables that are potentially related to growth. A detailed description is given in Growth_Description.pdf. You will investigate the relationship between growth and trade.

_ A	В	С	D	E	F	G	Н
1 country_n	growth	oil	rgdp60	tradeshar	yearsscho	rev_coups	assasinatio
2 India	1.915168	0	765.9998	0.140502	1.45	0.133333	0.866667
3 Argentina	0.617645	0	4462.002	0.156623	4.99	0.933333	1.933333
4 Japan	4.304759	0	2954	0.157703	6.71	0	0.2
5 Brazil	2.930097	0	1784	0.160405	2.89	0.1	0.1
6 United Sta	1.712265	0	9895.004	0.160815	8.66	0	0.433333
7 Banglades	0.708263	0	951.9998	0.221458	0.79	0.306481	0.175
8 Spain	2.880327	0	3123.002	0.299406	3.8	0.066667	1.433333
9 Colombia	2.227014	0	1684	0.313073	2.97	0.1	0.766667
10 Peru	0.060206	0	2019	0.324613	3.02	0.266667	0.566667
11 Haiti	-0.65793	0	923.9999	0.324746	0.7	0.374074	0.2
12 Australia	1.975147	0	7782.002	0.329479	9.03	0	0.066667
13 Italy	2.932982	0	4564.001	0.330022	4.56	0.033333	1.2
14 Greece	3.22405	0	2093	0.337879	4.37	0.166667	0.166667
15 France	2.431281	0	5823.001	0.339706	4.65	0	0.3
16 Zaire	-2.81194	0	488.9999	0.352318	0.54	0.148148	0.055556
17 Uruguay	1.025309	0	3968	0.358857	5.07	0	0.166667

Variable Definitions

Variable	Definition			
Country_name	Name of country			
growth	Average annual percentage growth of real Gross Domestic Product (GDP)* from 1960 to 1995.			
rgdp60	The value of GDP* per capita in 1960, converted to 1960 US dollars			
tradehare	The average share of trade in the economy from 1960 to 1995, measured as the sum of exports plus imports, divided by GDP; that is, the average value of $(X + M)/GDP$ from 1960 to 1995, where $X =$ exports and $M =$ imports (both X and M are positive).			
yearsshcool	Average number of years of schooling of adult residents in that country in 1960			
rev_coups	Average annual number of revolutions, insurrections (successful or not) and coup d'etats in that country from 1960 to 1995			
assasinations	Average annual number of political assassinations in that country from 1960 to 1995 (per million population)			
oil	= 1 if oil accounted for at least half of exports in 1960			
	= 0 otherwise			



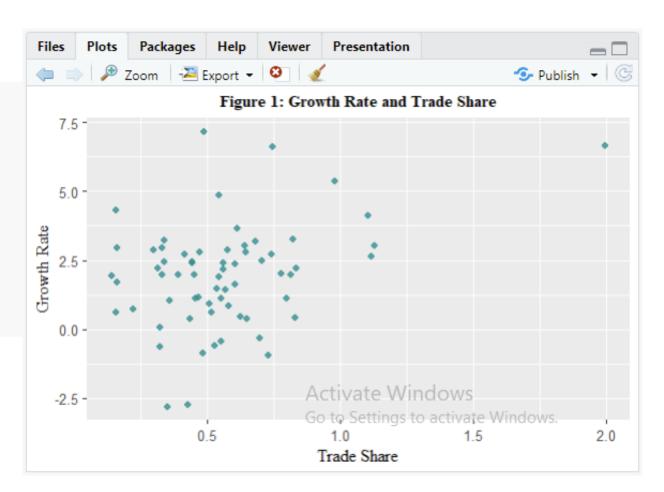
E4.1 The file Growth.csv contains data on average growth rates from 1960 through 1995 for 65 countries, along with variables that are potentially related to growth. A detailed description is given in Growth_Description.pdf. You will investigate the relationship between growth and trade.

```
8 # load non-built-in R packages (you should install them first!)
10 install.packages("readr")
11 install.packages("dplyr")
   install.packages("ggplot2")
13 install.packages("estimatr")
   install.packages("Hmisc")
15
16 library(readr)
                     # package for fast read rectangular data
17 library(dplyr) # package for data manipulation
18 library(ggplot2) # package for elegant data visualisation
   library(estimatr) # package for commonly used estimators with robust SE
   library(Hmisc) # package for statistics functions
21
   ### SW E4.1
24
25 # Set working directory (make sure you edit to your own WD)
26 # Ex Win: setwd("G:/My Drive/BEcon/TUTOR/ECON2300/02")
   # Ex Mac: setwd("/Users/ugdkim7/Dropbox/Teaching/R tutorials/Tutorial02")
28
   # To use the following line:
31 # save this file in the same directory as the data files
   # install.packages("rstudioapi")
   |setwd(dirname(rstudioapi::getSourceEditorContext()$path))
34
35 # Clean Working Environment
   rm(list = ls())
37
  # load csv data
39 Growth <- read_csv("Growth.csv")</pre>
```



(a) Construct a scatterplot of average annual growth rate, growth, on the average trade share, tradeshare. Does there appear to be a relationship between the variables?

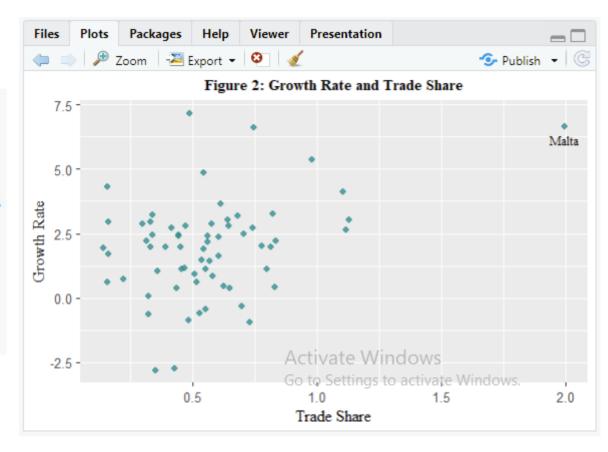
See Figure 1. Yes, there appears to be a weak positive relationship.





(b) One country, Malta, has a trade share much larger than the other countries. Find Malta on the scatterplot. Does Malta look like an outlier?

See Figure 2. Malta is the "outlying" observation with a trade share of 2.





(c) Using all observations, run a regression of growth on tradeshare. What is the estimated slope? What is the estimated intercept? Use the regression to predict the growth rate for a country with a trade share of 0.5 and with a trade equal to 1.0

```
# regression with robust standard errors
reg1 = lm_robust(growth ~ tradeshare, data = Growth, se_type = "stata")
# present output table
summary(reg1)
call:
lm_robust(formula = growth ~ tradeshare, data = Growth, se_type = "stata")
Standard error type: HC1
                                                                  # prediction based on regression model
Coefficients:
          Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper DF
                                                                  predict(reg1, newdata = data.frame(tradeshare = c(0.5, 1)))
            0.6403
                                                       1.558 63
(Intercept)
                      0.4591 1.394 0.1680736 -0.2773
tradeshare
            2.3064
                      0.6633 3.477 0.0009235 0.9810
                                                        3.632 63
                                                                    > predict(reg1, newdata = data.frame(tradeshare = c(0.5, 1)))
Multiple R-squared: 0.1237 , Adjusted R-squared: 0.1098
                                                                   1.793482 2.946699
F-statistic: 12.09 on 1 and 63 DF, p-value: 0.0009235
```

The fitted regression line is

$$\widehat{\mathtt{growth}} = 0.64 + 2.31 \times \mathtt{tradeshare}$$

where the estimated slope and intercept are 2.31 and 0.64, respectively. Moreover, the predicted growth, growth, at tradeshare = $1 \text{ is } 0.64 + 2.31 \times 1 = 2.95$. Similarly, the predicted growth, growth, at tradeshare = $0.5 \text{ is } 0.64 + 2.31 \times 0.5 = 1.80$.



(d) Estimate the same regression, excluding the data from Malta. Answer the same questions in (c).

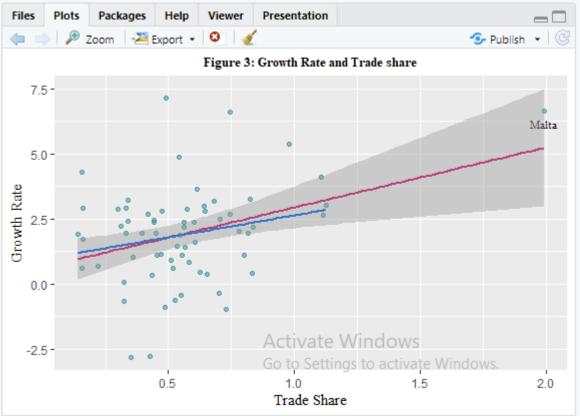
```
reg2 = lm_robust(growth ~ tradeshare, data = subset(Growth, country_name != "Malta"),
                    se type = "stata")
summary(reg2)
 call:
lm_robust(formula = growth ~ tradeshare, data = subset(Growth,
    country_name != "Malta"), se_type = "stata")
Standard error type: HC1
 Coefficients:
           Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper DF
                       0.5361 1.786 0.07899 -0.11415
 (Intercept) 0.9574
                                                         2.029 62
                       0.8656 1.942 0.05670 -0.04944
 tradeshare
             1.6809
                                                         3.411 62
Multiple R-squared: 0.04466 , Adjusted R-squared: 0.02925
F-statistic: 3.771 on 1 and 62 DF, p-value: 0.0567
                                                                   predict(reg2, newdata = data.frame(tradeshare = c(0.5, 1)))
                                                                    > predict(reg2, newdata = data.frame(tradeshare = c(0.5, 1)))
                                                                    1.797863 2.638315
```

The estimated slope and intercept are 1.68 and 0.96, respectively. Moreover, the predicted growth, growth, at tradeshare = 1 is $0.96 + 1.68 \times 1 = 2.64$. Similarly, the predicted growth, growth, at tradeshare = 0.5 is $0.96 + 1.68 \times 0.50 = 1.80$.



(e) Plot the estimated regression functions from (c) and (d). Using the scatterplot in (a), explain why the regression function that includes Malta is steeper than the regression function that excludes

Malta.



The data point of Malta is far away from the cloud of other points with very high trade share and growth rate. As the sample size is small, such an outlier (influential point) can greatly affect the slope of the regression line. In this case, as the growth rate of Malta is higher than most other countries, including Malta makes the regression line steeper.



(f) Where is Malta? Why is the Malta trade share so large? Should Malta be included or excluded from the analysis?

Malta is an island nation in the Mediterranean Sea, south of Sicily. Malta is a freight transport site, which explains its large "trade share." Many goods coming into Malta (imports into Malta) are immediately transported to other countries (as exports from Malta). Thus, Malta's imports and exports are unlike the imports and exports of most other countries. Malta should not be included in the analysis.



Tutorial 2 - Linear Regression with a Single Regressor



E4.2 The file Earnings_and_Height.csv contains data on earnings, height, and other characteristics of a random sample of U.S. workers. See Earnings_and_Height_Description.pdf for a detailed description of the data. You will investigate the relationship between earnings and height.

	Α	В	С	D	Е	F	G	Н	1	J	K
1	sex	age	mrd	educ	cworker	region	race	earnings	height	weight	occupation
2	0:female	48	1:Married	13	1:Private	3:South	non-hispa	84054.75	65	133	1
3	0:female	41	6:Never N	12	1:Private	2:Midwes	non-hispa	14021.4	65	155	1
4	0:female	26	1:Married	16	1:Private	1:Northea	non-hispa	84054.75	60	108	1
5	0:female	37	1:Married	16	1:Private	2:Midwes	non-hispa	84054.75	67	150	1
6	0:female	35	6:Never N	16	1:Private	1:Northea	non-hispa	28560.39	68	180	1
7	0:female	25	6:Never N	15	1:Private	4:West	non-hispa	23362.87	63	101	1
8	0:female	29	1:Married	16	1:Private	2:Midwes	non-hispa	38925.34	67	150	1
9	0:female	44	3:Divorce	18	3:State Go	4:West	non-hispa	84054.75	65	125	1
10	0:female	50	6:Never N	14	2:Fed Gov	3:South	non-hispa	84054.75	67	129	1
11	0:female	38	1:Married	12	4:Local Go	3:South	non-hispa	84054.75	66	110	1
12	0:female	30	1:Married	12	1:Private	4:West	non-hispa	84054.75	65	110	1
13	0:female	29	3:Divorce	18	2:Fed Gov	3:South	non-hispa	38925.34	68	135	1
14	0:female	26	1:Married	16	1:Private	1:Northea	non-hispa	84054.75	65	123	1
15	0:female	50	1:Married	12	1:Private	1:Northea	non-hispa	49430.11	63	132	1
16	0:female	65	3:Divorce	16	4:Local Go	4:West	hispanic	16081.59	65	110	1
17	0:female	45	6:Never N	17	2:Fed Gov	4:West	non-hispa	84054.75	71	202	1
18	0:female	26	6:Never N	16	1:Private	3:South	non-hispa	23362.87	66	130	1
19	0:female	57	3:Divorce	12	2:Fed Gov	3:South	non-hispa	44152.16	68	220	1
20	0:female	40	3:Divorce	16	1:Private	4:West	non-hispa	84054.75	66	195	1
21	0:female	36	1:Married	12	1:Private	3:South	non-hispa	49430.11	68	135	1
22	0:female	60	1:Married	15	4:Local Go	3:South	non-hispa	84054.75	64	160	1
23	0:female	32	1:Married	12	1:Private	2:Midwes	non-hispa	33712.97	65	115	1
24	0:female	33	1:Married	12	1:Private	1:Northea	non-hispa	44152.16	61	125	1

s and nei	gnt.					
Variable Name	Description					
age	Age, in years					
cworker	Class of Worker:					
	1 = Private company Employee					
	2 = Federal Government Employee					
	3 = State Government Employee					
	4 = Local Government Employee					
	5 = Incorporated Business Employee					
	6 = Self Employed					
earnings	annual labor earnings, expressed in \$2012 (see Table notes)					
educ	years of education					
height	height without shoes (in inches)					
mrd	Marital Status					
	1 = Married, Spouse in household					
	2 = Married, Spouse not in household					
	3 = Widowed					
	4 = Divorced					
	5 = Separated					
	6 = Never Married					
occupation	Occupations in 15 categories:					
	1 = Exec/Manager					
	2 = Professionals					
	3 = Technicians					
	4 = Sales					
	5 = Administrat					
	6 = Household service					
	7 = Protective service					
	8 = Other Service					
	9 = Farming					
	10 = Mechanics					
	11 = Construction/Mining					
	12 = Precision production					
	13 = Machine Operator					
	14 = Transport 15 = Laborer					
F0.00	race/ethnicity					
race						
	1 = non-Hispanic white 2 = non-Hispanic black					
	3 = Hispanic					
	4 = other					
ragion	Region of the U.S.	_				
region	1 = Northeast					
	2 = Midwest					
	3 = South					
	4 = West					
sex	Sex, 1=Male, 0 = Female					
weight	weight without shoes (in pounds)	_				
	neight malout shoes (in pounds)					

Tutorial 2 - Linear Regression with a Single Regressor s



(a) What is the median value of height in the sample?

```
rm(list = ls())
setwd("/Users/uqdkim7/Dropbox/Teaching/R tutorials/Tutorial02")
EH <- read_csv("Earnings_and_Height.csv")

(a)
The median height in the sample is 67 inches.
# descriptive/summary statistics
describe(EH$height, descript = "height")</pre>
```

```
> describe(EH$height, descript = "height")
height
      n missing distinct
                               Info
                                                  Gmd
                                                            .05
                                                                     .10
                                                                              . 25
                                                                                                .75
                                                                                                                   .95
                                        Mean
  17870
                              0.995
                                       66.96
                                                4.518
                                                                      62
                                                                               64
                                                                                                 70
                                                                                                          72
                                                                                                                   74
lowest: 48 49 51 52 53, highest: 79 80 81 83 84
```

> describe(EH\$earnings[EH\$height <= 67], descript = "earnings for height <= 67")</pre>

essentially zero).

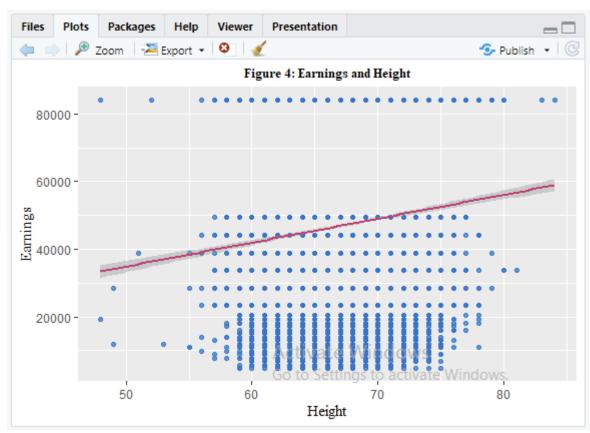


- (b) i. Estimate average earnings for workers whose height is at most 67 inches.
 - ii. Estimate average earnings for workers whose height is greater than 67 inches.
 - iii. On average, do taller workers earn more than shorter workers? How much more? What is a 95% confidence interval for the difference in average earnings?

```
earnings for height <= 67
      n missing distinct
                               Info
                                                                              . 25
                                                                                                                  .95
                                                  Gmd
                                                                                                .75
                                                                                                         . 90
                                        Mean
                                                                  15082
   10114
                        23
                              0.974
                                       44488
                                                29337
                                                         10865
                                                                            23363
                                                                                     38925
                                                                                              84055
                                                                                                       84055
                                                                                                                84055
lowest: 4726.391 5675.895 6711.288 7782.854 8826.651, highest: 33712.969 38925.336 44152.160 49430.109 84054.750
> describe(EH$earnings[EH$height > 67], descript = "earnings for height > 67")
earnings for height > 67
      n missing distinct
                               Info
                                                           .05
                                                                     .10
                                                                              . 25
                                                                                       .50
                                                                                                .75
                                                                                                         .90
                                                                                                                  .95
                                                  Gmd
                                        Mean
    7756
                        23
                              0.952
                                       49988
                                                29682
                                                         14021
                                                                  18169
                                                                            28560
                                                                                     44152
                                                                                              84055
                                                                                                       84055
                                                                                                                84055
                0
lowest: 4726.391 5675.895 6711.288 7782.854 8826.651, highest: 33712.969 38925.336 44152.160 49430.109 84054.750
> # unpair two-Samples t-test
> t.test(EH$earnings[EH$height <= 67], EH$earnings[EH$height > 67])
        Welch Two Sample t-test
data: EH$earnings[EH$height <= 67] and EH$earnings[EH$height > 67]
t = -13.59, df = 16624, p-value < 2.2e-16
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -6292.643 -4706.237
sample estimates:
                                  The estimated average annual earnings for shorter workers is $44,488, is $49,988 for taller workers, for a
mean of x mean of y
                                  difference of $5,499. The 95% confidence interval is $4,706 to $6,293. The difference is large (more than
 44488.44 49987.88
                                  10% of average earnings), precisely estimated and statistically significantly different from zero (p-value is
```



(c) Construct a scatterplot of annual earnings, earnings, on height, height. Notice that the points on the plot fall along horizontal lines. (There are only 23 distinct values of earnings). Why? (Hint: Carefully read the detailed data description.)



The data documentation reports that individual earnings were reported in 23 brackets, and a single average value is reported for earnings in the same bracket. Thus, the dataset contains 23 distinct values of earnings.



- (d) Run a regression of earnings on height.
 - i. What is the estimated slope?
 - ii. Use the estimated regression to predict earnings for a worker who is 67 inches tall, for a worker who is 70 inches tall, and for a worker who is 65 inches tall.

```
> reg3 <- lm_robust(earnings ~ height, data = EH, se_type = "stata")</pre>
> summary(reg3)
Call:
lm_robust(formula = earnings ~ height, data = EH, se_type = "stata")
Standard error type: HC1
Coefficients:
            Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper
                         3379.9 -0.1517 8.794e-01 -7137.6
(Intercept)
              -512.7
                                                             6112.1 17868
                           50.4 14.0425 1.478e-44
height
               707.7
                                                     608.9
                                                              806.5 17868
Multiple R-squared: 0.01088 , Adjusted R-squared: 0.01082
F-statistic: 197.2 on 1 and 17868 DF, p-value: < 2.2e-16
> predict(reg3, newdata = data.frame(height = c(65, 67, 70)))
                                                                           earnings = -512.7 + 707.7 \times \text{height}, R^2 = 0.011
45485.92 46901.26 49024.28
```

The estimated slope is 707.7 (\$ per year). The estimated earnings are

Height in inches	earnings in \$ per year
65	45,486
67	46,901
70	49,024



- (e) Suppose height were measured in centimeters instead of inches. Answer the following questions about the earnings on height (in cm) regression.
 - i. What is the estimated slope of the regression?
 - ii. What is he estimated intercept?
 - iii. What is the R^2 ?
 - iv. What is the standard error of the regression?

Compute SER:

```
sqrt(reg3$res_var)
```

[1] 26777.24

Recall that 1 cm = 0.394 inches. The estimated regression in (d), with units shown, is

$$\widehat{\mathtt{earnings}}(\$) = -512.7(\$) + 707.7(\$/inch) \times \mathtt{height}(inch),$$

and we have $R^2 = 0.011$ which is unit free and SER = 26,777(\$), the same unit as the LHS variable. Note that

$$\begin{split} \widehat{\texttt{earnings}}(\$) &= -512.7(\$) + 707.7(\$/inch) \times \texttt{height}(inch) \\ &= -512.7(\$) + 707.7(\$/inch) \times (0.394inch/cm) \times \texttt{height}(cm) \\ &= -512.7(\$) + 278.8(\$/cm) \times \texttt{height}(cm) \end{split}$$

So the regression is

$$\widehat{\mathtt{earnings}}(\$) = -512.7(\$) + 278.8(\$/cm) \times \mathtt{height}(cm)$$

with $R^2 = 0.011$ and SER = 26,777(\$). Tutorial 2 - Linear Regression with a Single Regressor



- (f) Run a regression of earnings on height using data for female workers only.
 - i. What is the estimated slope?
 - ii. A randomly selected woman is 1 inch taller than he average woman in the sample. Would you predict her earnings to be higher or lower than the average earnings for women in the sample? By how much?

```
reg4 = lm_robust(earnings ~ height, data = subset(EH, sex == "0:female"), se_type = "stata")
summary(reg4)
          Call:
          lm_robust(formula = earnings ~ height, data = subset(EH, sex ==
              "0:female"), se_type = "stata")
          Standard error type: HC1
          Coefficients:
                     Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper
                                         2.008 4.463e-02
          (Intercept) 12650.9
                                 6299.15
                                                             303.2 24998.5 9972
          height
                        511.2
                                   97.58
                                          5.239 1.650e-07
                                                             319.9
                                                                     702.5 9972
          Multiple R-squared: 0.002672 , Adjusted R-squared: 0.002572
          F-statistic: 27.44 on 1 and 9972 DF, p-value: 1.65e-07
                        earnings = 12650 + 511.2 \times \text{height}, R^2 = 0.003
```

A women who is one inch taller than average is predicted to have earnings that are \$511.2 per year higher than average.



(f) Run a regression of earnings on height using data for female workers only.

F-statistic: 174.8 on 1 and 7894 DF, p-value: < 2.2e-16

- i. What is the estimated slope?
- ii. A randomly selected woman is 1 inch taller than he average woman in the sample. Would you predict her earnings to be higher or lower than the average earnings for women in the sample? By how much?
- (g) Repeat (f) for male workers.

```
reg5 = lm_robust(earnings ~ height, data = subset(EH, sex == "1:male"), se_type = "stata")
summary(reg5)
         Call:
         lm_robust(formula = earnings ~ height, data = subset(EH, sex ==
             "1:male"), se_type = "stata")
         Standard error type: HC1
         Coefficients:
                     Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper DF
                                6925.01 -6.228 4.960e-10
         (Intercept)
                      -43130
                                                          -56705
                                                                   -29555 7894
                        1307
                                  98.86 13.220 1.771e-39
         height
                                                            1113
                                                                     1501 7894
         Multiple R-squared: 0.02086, Adjusted R-squared: 0.02074
```

$$\widehat{\text{earnings}} = -43130 + 1307 \times \text{height}, \quad R^2 = 0.021$$

A man who is one inch taller than average is predicted to have earnings that are \$1307 per year higher than average.



(h) Do you think that height is uncorrelated with other factors that cause earning? That is, do you think that the regression error term, say u_i , has a conditional mean of zero, given height (X_i) ?

Height may be correlated with other factors that cause earnings. For example, height may be correlated with "strength," and in some occupations, stronger workers may by more productive. There are many other potential factors that may be correlated with height and cause earnings and you will investigate of these in future exercises.

Thank you

Francisco Tavares Garcia

Academic Tutor | School of Economics

tavaresgarcia.github.io

Reference

Stock, J. H., & Watson, M. W. (2019). Introduction to Econometrics, Global Edition, 4th edition. Pearson Education Limited.

CRICOS code 00025B

