## ECON2300 - Introductory Econometrics

Tutorial 11: Experiments and Quasi-Experiments

Tutor: Francisco Tavares Garcia



Quiz 10 is available!

Quiz 10 is now available under the Assessment folder.

The due date is Thursday, 23th October, 16:00.



#### Assessment summary

| Category    | Assessment task                                 | Weight                  | Due date   |
|-------------|---|-------------------------|--|
| Quiz        | Problem Solving, Data Analysis and Short Report | 25% 7 best<br>out of 10 | Weeks 3,4,5,6,7,8,9,10,11,12                                 |
|             | □ Online  |                         | Online Periodic Assessments Throughout the Semester          |
| Project     | Project: Assignment and Brief Research Report   | 25%                     | 29/04/2025 4:00 pm   |
|             | □ Online  |                         | The project can be submitted at anytime before the due date. |
| Examination | <u>Final Exam</u>                               | 50%                     | End of Semester Exam Period                                  |
|             | ⚠ Hurdle ☐ Identity Verified ☐ In-person        |                         | 7/06/2025 - 21/06/2025                                       |



Semester One Examinations, 2024

ECON2300

Part A: (30 Marks Total) Answer ALL Questions on the Gradescope Bubble Sheet. Each Question has only ONE correct answer and is worth 2 marks:

 A researcher has estimated a linear model to study the e →ect of weekly household income x<sub>i</sub> (in \$100) on weekly household expenditure on food y<sub>i</sub> (in \$). Using a sample of size N = 40, she found that

$$y_i = 83.42 + 10.21x_i$$
,  $R^2 = 0.384$   
(43.41) (2.09)

and  $P_{i=1}^{N}(y_i - y_i^*)^2 = 500,000$  and the sample mean of  $x_i$  is 19.605. Consider a hypothesis testing against

 $H_0$ : the slope coefficient is 3.94.

Therefore we, at 5% significance level,

- (a) reject H<sub>0</sub>.
- (b) do not reject Ho.
- (c) accept H1.
- (d) cannot do anything unless the significance level is 10%.
- (e) re-estimate the regression model using a di-Jerent data.
- 2. Consider the following regression model,

$$u_i = .B_1 + .B_2 x_{i2} + \cdots + .B_K x_{iK} + u_i$$

where  $E[u_i|x_i] = 0$  and  $Var(u_i|x_i)$  depends on the value of  $x_i$ , i.e.,  $Var(u_i|x_i) \notin 0^{*2}$ . Choose the <u>correct</u> statement.

- (a) To get around the problem, we often assume that  $u_i$  is normally distributed.
- (b) To fix the problem, we need to have an instrumental variable.
- (c) This problem implies that errors are correlated with one of  $(x_{i2},...,x_{iK})$ .
- (d) If we assume Var(ui|xi) = 0<sup>12</sup>, the confidence interval is not valid.
- (e) None of the above is correct.
- A researcher has estimated a linear model to study the e →ect of weekly household income x<sub>i</sub> (in \$100) on weekly household expenditure on food y<sub>i</sub> (in \$). Using a sample of size N = 40, she found that

$$b_i = 83.42 + 10.21x_i$$
,  $R^2 = 0.384$ 

and  $P_{i=(y_i-y^*)^2}^N = 500,000$  and the sample mean of  $x_i$  is 19.605. Choose the <u>wrong</u> statement.

(a) The estimated variance of the slope estimator is (2.09)2.

#### EXAMINATION CONTINUES ON THE NEXT PAGE.

# Exam Sample

PART B: Short Response Questions. (20 Marks Total) Answer Q1-Q2 in this answer booklet.

ONLY write answers in the space provided for each question. Ample space is provided in case you need to cross out and re-write the answer. Working outside the designated space will NOT BE MARKED. Marks are as indicated. Formulas and F table are on page page 14.

Q1 Table 1 below presents estimated models where the dependent variable is ln(Price) of a house that has been sold.

Table 1: Residential Housing Models

| Regressor          | (1)                   | (2)              | (3)               | (4)              | (5)              |
|--------------------|-----------------------|------------------|-------------------|------------------|------------------|
| Size               | 0.00042<br>(0.000038) |                  |                   |                  |                  |
| ln(Size)           |                       | 0.69<br>(0.054)  | 0.68<br>(0.087)   | 0.57<br>(2.03)   | 0.69<br>(0.055)  |
| $ln(Size)^2$       |                       |                  |                   | 0.0078<br>(0.14) |                  |
| Bedrooms           |                       |                  | 0.0036<br>(0.037) |                  |                  |
| Pool               | 0.082<br>(0.032)      | 0.071<br>(0.034) | 0.071<br>(0.034)  | 0.071<br>(0.036) | 0.071<br>(0.035) |
| View               | 0.037<br>(0.029)      | 0.027<br>(0.028) | 0.026<br>(0.026)  | 0.027<br>(0.029) | 0.027<br>(0.030) |
| Pool × View        |                       |                  |                   |                  | 0.0022<br>(0.10) |
| Condition          | 0.13<br>(0.045)       | 0.12<br>(0.035)  | 0.12<br>(0.035)   | 0.12<br>(0.036)  | 0.12<br>(0.035)  |
| Intercept          | 10.97<br>(0.069)      | 6.60<br>(0.39)   | 6.63<br>(0.53)    | 7.02<br>(7.50)   | 6.60<br>(0.40)   |
| Summary Statistics |                       |                  |                   |                  |                  |
| SER                | 0.102                 | 0.098            | 0.099             | 0.099            | 0.099            |
| $\overline{R}^2$   | 0.72                  | 0.74             | 0.73              | 0.73             | 0.73             |

Variable definitions: Price = sale price (\$); Size = house size (in square feet); Redrooms = number of bedrooms; Pool = binary variable (1 if house has a swimming pool, 0 otherwise); View = binary variable (1 if house has a nice view, 0 otherwise); Condition = binary variable (1 if real estate agent reports house is in excellent condition, 0 otherwise).

(a) A family purchases a 2000 square foot home and plans to make extensions totaling 500 square feet. The house currently has a pool, and a real estate agent has reported that the house is in excellent condition. However, the house does not have a view, and this will not change as a result of the extensions. According to the results from Model 1 (column (1) of Table 1), what is the expected DOLLAR increase in the price of the home due to the planned extensions? (4 marks)



#### SETutor is available!

If you found these tutorials helpful, please answer the survey.

(If you didn't, please let me know how to improve them through the survey too ②)

This is very valuable for us tutors!

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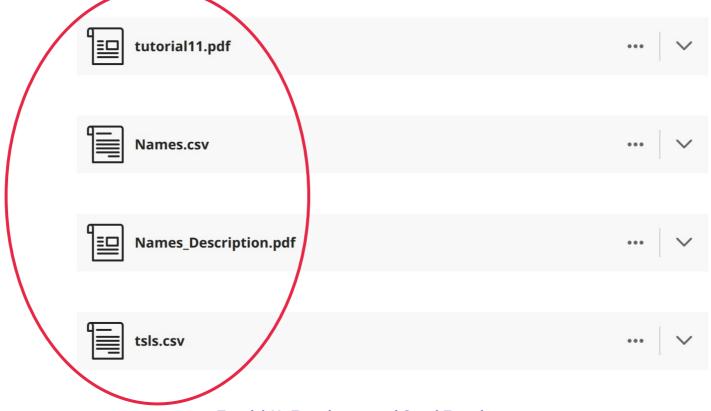


# **Introductory Econometrics**

**Students** 



- Download the files for tutorial 11 from Blackboard,
- save them into a folder for this tutorial.





## Now, let's download the script for the tutorial.

- Copy the code from Github,
  - https://github.com/tavaresgarcia/teaching
- Save the scripts in the same folder as the data.



E13.1 A prospective employer receives two resumes: a resume from a white job applicant and a similar resume from an African American applicant. Is the employer more likely to call back the white applicant to arrange an interview? Marianne Bertrand and Sendhil Mullainathan carried out a randomized controlled experiment to answer this question. Because race is not typically included on a resume, they differentiated resumes on the basis of "white-sounding names" (such as Emily Walsh or Gregory Baker) and "African American-sounding names" (such as Lakisha Washington or Jamal Jones). A large collection of fictitious resumes was created, and the presupposed "race" (based on the "sound" of the name) was randomly assigned to each resume. These resumes were sent to prospective employers to see which resumes generated a phone call (a "call back") from the prospective employer. Use the data file Names.csv to answer the following questions. See Names\_Description.pdf for more details

about the data.



**Tutorial 11: Experiments and Quasi-Experiments** 



#### **Variable Descriptions**

| Description  |
|--|
| Key Variables  |
| applicant's first name                                 |
| 1 = female   |
| 1 = black  |
| 1= high quality resume                                 |
| 1= applicant was called back                           |
| 1 = data from Chicago                                  |
|  |
| Detailed Information on Resume                         |
| number of jobs listed on resume                        |
| number of years of work experience on the resume       |
| 1=resume mentions some honors                          |
| 1=resume mentions some volunteering experience         |
| 1=applicant has some military experience               |
| 1=resume has some employment holes                     |
| 1=resume mentions some work experience while at school |
| 1=email address on applicant's resume                  |
| 1=resume mentions some computer skills                 |
| 1=resume mentions some special skills                  |
| applicant has college degree or more                   |
|  |



(a) Define the "call-back rate" as the fraction of resumes that generate a phone call from the prospective employer. What was the call-back rate for whites? For African Americans? Construct a 95% confidence interval for the difference in the call-back rates. Is the difference statistically significant? Is it large in a real-world sense?

| > summary(reg1)   |
|---|
| <pre>Call: lm_robust(formula = call_back ~ black, se_type = "stata")</pre>  |
| Standard error type: HC1  |
| Coefficients:  Estimate Std. Error t value Pr(> t ) CI Lower CI Upper DF  |
| (Intercept) 0.09651 0.005985 16.124 5.045e-57 0.08478 0.10824 4868  |
| black -0.03203 0.007785 -4.115 3.941e-05 -0.04729 -0.01677 4868   |
| Multiple R-squared: 0.003466 , Adjusted R-squared: 0.003261 F-statistic: 16.93 on 1 and 4868 DF, p-value: 3.941e-05 |

|                     | (1)        | (2)       | (3)       | (4)       |
|---------------------|------------|-----------|-----------|-----------|
| (Intercept)         | 0.0965***  | 0.0965*** | 0.0734*** | 0.0850*** |
|                     | (0.0060)   | (0.0060)  | (0.0053)  | (0.0080)  |
| black               | -0.0320*** | -0.0382** |           | -0.0231*  |
|                     | (0.0078)   | (0.0117)  |           | (0.0106)  |
| female.black        |            | 0.0080    |           |           |
|                     |            | (0.0115)  |           |           |
| high                |            |           | 0.0141    | 0.0229    |
|                     |            |           | (0.0078)  | (0.0120)  |
| high.black          |            |           |           | -0.0178   |
|                     |            |           |           | (0.0156)  |
| $\mathbb{R}^2$      | 0.0035     | 0.0035    | 0.0007    | 0.0044    |
| Adj. R <sup>2</sup> | 0.0033     | 0.0031    | 0.0005    | 0.0038    |
| Num. obs.           | 4870       | 4870      | 4870      | 4870      |
| RMSE                | 0.2716     | 0.2717    | 0.2720    | 0.2716    |

<sup>\*\*\*</sup>p < 0.001; \*\*p < 0.01; \*p < 0.05

From (1) in the table, the call-back rate for whites is 0.0965 and the call-back rate for blacks is 0.0965-0.032 = 0.0645. The difference is -0.032 is statistically significant at the 1% level (t-statistic = -4.11). This result implies that 9.65% of resumes with white-sounding names generated a call back. Only 6.45% of resumes with black-sounding names generated a call back. The difference is large in both statistical and economic sense.



(b) Is the African American/white call-back rate differential different for men than for women?

| > summary(reg2)   |
|---|
| <pre>Call: lm_robust(formula = call_back ~ black + female.black, se_type = "stata")</pre>                           |
| Standard error type: HC1  |
| Coefficients:   |
| Estimate Std. Error t value Pr(> t ) CI Lower CI Upper DF   |
| (Intercept) 0.09651 0.005986 16.1227 5.178e-57 0.08477 0.10824 4867   |
| black -0.03822 0.011657 -3.2790 1.049e-03 -0.06107 -0.01537 4867  |
| female.black 0.00799 0.011527 0.6931 4.883e-01 -0.01461 0.03059 4867  |
| Multiple R-squared: 0.003541 , Adjusted R-squared: 0.003132 F-statistic: 8.805 on 2 and 4867 DF, p-value: 0.0001524 |

| Comment of the comment of | (1)        | (2)       | (3)       | (4)       |
|---------------------------|------------|-----------|-----------|-----------|
| (Intercept)               | 0.0965***  | 0.0965*** | 0.0734*** | 0.0850*** |
|                           | (0.0060)   | (0.0060)  | (0.0053)  | (0.0080)  |
| black                     | -0.0320*** | -0.0382** |           | -0.0231   |
|                           | (0.0078)   | (0.0117)  |           | (0.0106)  |
| female.black              |            | 0.0080    |           |           |
|                           |            | (0.0115)  |           |           |
| high                      |            |           | 0.0141    | 0.0229    |
|                           |            |           | (0.0078)  | (0.0120)  |
| high.black                |            |           |           | -0.0178   |
|                           |            |           |           | (0.0156)  |
| $\mathbb{R}^2$            | 0.0035     | 0.0035    | 0.0007    | 0.0044    |
| Adj. R <sup>2</sup>       | 0.0033     | 0.0031    | 0.0005    | 0.0038    |
| Num. obs.                 | 4870       | 4870      | 4870      | 4870      |
| RMSE                      | 0.2716     | 0.2717    | 0.2720    | 0.2716    |

<sup>\*\*\*</sup>p < 0.001; \*\*p < 0.01; \*p < 0.05

From (2) in the table, the call-back rate for male blacks 0.0965 - 0.0382 = 0.0583, and for female blacks is 0.0965 - 0.0382 + 0.008 = 0.0663. The difference is 0.008, which is not significant at the 5% level (t-statistic = 0.69).



(c) What is the difference in call-back rates for high-quality versus low-quality resumes? What is the high-quality/low-quality difference for white applicants? For African American applicants? Is there a significant difference in this high-quality/low-quality difference for whites versus African Americans?

```
Call:
lm_robust(formula = call_back ~ high, se_type = "stata")
Standard error type: HC1
Coefficients:
           Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper
                      0.005299 13.857 7.404e-43 0.063044 0.08382 4868
high
                      0.007793 1.804 7.132e-02 -0.001221 0.02934 4868
Multiple R-squared: 0.0006675,
                                      Adjusted R-squared: 0.0004622
F-statistic: 3.254 on 1 and 4868 DF, p-value: 0.07132
> summary(reg4)
Call:
lm_robust(formula = call_back ~ black + high + high.black, se_type = "stata")
Standard error type: HC1
Coefficients:
           Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper
(Intercept) 0.08498
                      0.008013 10.605 5.397e-26 0.069274 0.100693 4866
black
            -0.02310
                      0.010590 -2.182 2.919e-02 -0.043864 -0.002341
hiah
            0.02295
                      0.011958
                               1.919 5.505e-02 -0.000496 0.046392 4866
high.black -0.01778
                      0.015561 -1.143 2.532e-01 -0.048286 0.012725 4866
Multiple R-squared: 0.0044, Adjusted R-squared: 0.003787
F-statistic: 6.613 on 3 and 4866 DF, p-value: 0.0001868
```

| C.                  | (1)        | (2)       | (3)       | (4)       |
|---------------------|------------|-----------|-----------|-----------|
| (Intercept)         | 0.0965***  | 0.0965*** | 0.0734*** | 0.0850*** |
|                     | (0.0060)   | (0.0060)  | (0.0053)  | (0.0080)  |
| black               | -0.0320*** | -0.0382** |           | -0.0231*  |
|                     | (0.0078)   | (0.0117)  |           | (0.0106)  |
| female.black        |            | 0.0080    |           |           |
|                     |            | (0.0115)  |           |           |
| high                |            |           | 0.0141    | 0.0229    |
|                     |            |           | (0.0078)  | (0.0120)  |
| high.black          |            |           |           | -0.0178   |
|                     |            |           |           | (0.0156)  |
| $\mathbb{R}^2$      | 0.0035     | 0.0035    | 0.0007    | 0.0044    |
| Adj. R <sup>2</sup> | 0.0033     | 0.0031    | 0.0005    | 0.0038    |
| Num. obs.           | 4870       | 4870      | 4870      | 4870      |
| RMSE                | 0.2716     | 0.2717    | 0.2720    | 0.2716    |

From (3) in the table, the call-back rate for low-quality resumes is 0.0734 and the call-back rate for high-quality resumes is 0.0734 + 0.0141 = 0.0875. The difference is 0.0141, which is not significant at the 5% level, but is at the 10% level (p-value = 0.071). From (4) the (high-quality)-(low-quality) difference for whites is 0.0229and for blacks is 0.0229 - 0.0178 = 0.0051; the black-white difference is -0.0178 which is not statistically significant at the 5% level (t-statistic = -1.14).



(d) The authors of the study claim that race was assigned randomly to the resumes. Is there any evidence of nonrandom assignment?

```
> Tests = lm_robust(cbind(ofjobs, yearsexp, honors, volunteer, military, empholes,
                 workinschool, email, computerskills, specialskills, eoe, manager,
                 supervisor, secretary, offsupport, salesrep,
                 retailsales, req, expreq, comreq, educreq, compreq, orgreq,
                 manuf, transcom, bankreal, trade, busservice, othservice,
                 missind, chicago, high, female, college, call_back) ~ black,
              se_type = "stata")
  > tidv(Tests)
                               std.error
                                              statistic
                                                                          conf.low
                                                                                      conf.high
                      estimate
                                                              p.value
                                                                                                            outcome
            term
                                                                                                       workinschool
                5.581109e-01 0.010065993
                                          5.544519e+01
                                                        0.000000e+00 0.538376993
                                                                                    0.577844773 4868
13 (Intercept)
14
         black
                2.874743e-03 0.014230522
                                          2.020125e-01
                                                        8.399154e-01 -0.025023504
                                                                                    0.030772990 4868
                                                                                                       workinschool
   (Intercept)
                4.788501e-01 0.010125602
                                          4.729103e+01
                                                        0.000000e+00 0.458999353
                                                                                   0.498700853 4868
                                                                                                              email
         black 8.213552e-04 0.014320252
                                          5.735620e-02
16
                                                        9.542638e-01 -0.027252803
                                                                                   0.028895513 4868
                                                                                                              email
                8.086242e-01 0.007973639
                                          1.014122e+02
                                                                                   0.824256162 4868 computerskills
   (Intercept)
                                                        0.000000e+00 0.792992298
18
         black 2.381930e-02 0.010994740
                                          2.166427e+00
                                                        3.032693e-02
                                                                      0.002264649
                                                                                   0.045373955 4868 computerskills
                                          3.463868e+01 3.283966e-235
                                                                                                      specialskills
  (Intercept)
                3.301848e-01 0.009532257
                                                                      0.311497278
                                                                                   0.348872332 4868
         black -2.874743e-03 0.013465635 -2.134874e-01 8.309558e-01 -0.029273467
                                                                                    0.023523980 4868
                                                                                                      specialskills
21 (Intercept) 2.911704e-01 0.009208402 3.162008e+01 9.531045e-200
                                                                                    0.309223056 4868
                                                                      0.273117807
                                                                                                                eoe
         black -2.163638e-16 0.013022647 -1.661443e-14 1.000000e+00 -0.025530266
                                                                                    0.025530266 4868
                                                                                                                eoe
```

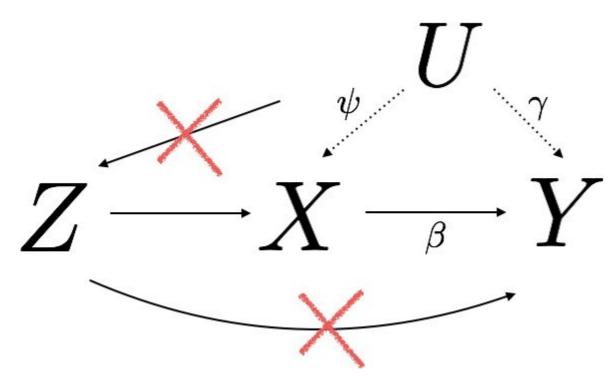
Results of a series of t-tests (via linear regressions, see the log-file) shows estimated means of other characteristics for black and white sounding names. There are only two significant differences in the mean values: the call-back rate (the variable of interest) and computer skills (for which black-named resumes had a slightly higher fraction than white-named resumes). Thus, there is no evidence of non-random assignment.



TSLS In this question, we fit the following regression model to the data tsls.csv

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + u \tag{1}$$

We are interested in studying the causal effect of  $X_2$  on Y, i.e.,  $\beta_2$ .



DOI: https://doi.org/10.1145/3178876.3186151



TSLS In this question, we fit the following regression model to the data tsls.csv

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + u \tag{1}$$

We are interested in studying the causal effect of  $X_2$  on Y, i.e.,  $\beta_2$ .



(a) Estimate (1) using OLS. Write out the estimated regression equation along with standard errors and one measure of fit in a standard form.

#### > summary(reg1) Call: $lm_robust(formula = y \sim x1 + x2, se_type = "stata")$ Standard error type: HC1 Coefficients: Estimate Std. Error t value Pr(>|t|) CI Lower CI Upper DF 1.0445 0.1154 9.051 1.499e-14 0.81550 1.2736 97 (Intercept) 0.3034 0.1759 1.725 8.770e-02 -0.04567 0.6525 97 x1 x2 -0.5430 0.0561 -9.679 6.616e-16 -0.65434 -0.4317 97 Multiple R-squared: 0.505, Adjusted R-squared: 0.4948 F-statistic: 49.34 on 2 and 97 DF. p-value: 1.651e-15

|                | (1)        | 2: TSLS<br>(2)  | (3)        |
|----------------|------------|-----------------|------------|
| (Intercept)    | 1.0445***  | 1.0244***       | 1.0174***  |
| 110            | (0.1154)   | (0.1383)        | (0.1551)   |
| x1             | 0.3034     | 0.8307**        | 1.0123***  |
|                | (0.1759)   | (0.3126)        | (0.2888)   |
| x2             | -0.5430*** | $-0.9289^{***}$ | -1.0618*** |
|                | (0.0561)   | (0.1775)        | (0.1357)   |
| $\mathbb{R}^2$ | 0.5050     | 0.2688          | 0.0781     |
| $Adj. R^2$     | 0.4948     | 0.2537          | 0.0591     |
| Num. obs.      | 100        | 100             | 100        |
| RMSE           | 0.8109     |                 |            |

\*\*\* p < 0.001; \*\* p < 0.01; \* p < 0.05

The estimated model is

$$\hat{Y} = 1.045 + 0.303 X_1 - 0.543 X_2, \ \bar{R}^2 = 0.495$$

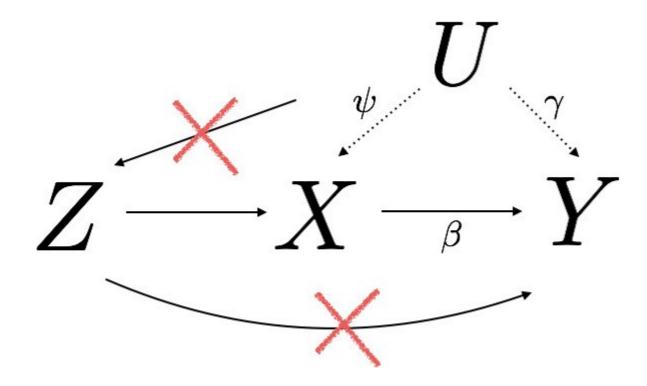
(b) If  $X_2$  were endogenous, which least squares assumption would be violated? What could be wrong with OLS if this assumption is indeed invalid?

The exogeneity assumption  $(E[u|X_1, X_2] = 0)$  would be violated. If this were the case, OLS would be biased and inconsistent.



(c) Estimate  $\beta_2$  using two-stage least squares (TSLS), instead of OLS.  $Z_1$  is one of our candidate instrumental variables (IV). What conditions must hold for  $Z_1$  to be a valid IV for  $X_2$ ?

Two conditions must hold: (1)  $C(u, Z_1) = 0$  (exogeneity), and (2)  $C(X_2, Z_1) \neq 0$  (relevance).





(d) Suppose  $Z_1$  is a valid IV for  $X_2$ . Run a TSLS regression using  $Z_1$ . Write out the estimated regression equations for the second-stage estimation. Are  $(\beta_0, \beta_1, \beta_2)$  exactly identified, over-identified, or under-identified? What could be wrong if we run TSLS "manually" (i.e., use the regress command twice to replicate the TSLS procedure)?

| > summary(re |             |           |                    |          |         |       | - |
|--------------|-------------|-----------|--------------------|----------|---------|-------|---|
| Call:        | 2 - V V1    | . v2   v1 | -11                |          |         |       | - |
| ivreg(formul | a = y ~ XI  | T X2   X1 | . <del>+</del> 21) |          |         |       |   |
| Residuals:   |             |           |                    |          |         |       |   |
| Min          | 1Q Mediar   | 1 3Q      | Max                |          |         |       |   |
| -2.3753 -0.7 | 670 0.0596  | 0.5884    | 2.0363             |          |         |       |   |
| c cc:        | _           |           |                    |          |         |       |   |
| Coefficients |             |           |                    |          |         |       |   |
|              | Estimate S1 |           |                    |          |         |       | 7 |
| (Intercept)  | 1.0244      | 0.1383    | 7.407              | 4.79e-11 | ***     |       |   |
| x1           | 0.8307      | 0.3126    | 2.658              | 0.0092   | **      |       |   |
| x2           | -0.9289     | 0.1775    | -5.233             | 9.64e-07 | ***     |       |   |
|              |             |           |                    |          |         |       |   |
| Signif. code | s: 0 '***   | 0.001 '*  | *' 0.01            | '*' 0.05 | ·.' 0.1 | ' ' 1 | _ |
| - · g 2040   |             |           | 0.01               | 0.00     |         | -     |   |

|                | Table 2    | 2: TSLS         |            |
|----------------|------------|-----------------|------------|
|                | (1)        | (2)             | (3)        |
| (Intercept)    | 1.0445***  | 1.0244***       | 1.0174***  |
|                | (0.1154)   | (0.1383)        | (0.1551)   |
| x1             | 0.3034     | 0.8307**        | 1.0123***  |
|                | (0.1759)   | (0.3126)        | (0.2888)   |
| x2             | -0.5430*** | $-0.9289^{***}$ | -1.0618*** |
|                | (0.0561)   | (0.1775)        | (0.1357)   |
| $\mathbb{R}^2$ | 0.5050     | 0.2688          | 0.0781     |
| $Adj. R^2$     | 0.4948     | 0.2537          | 0.0591     |
| Num. obs.      | 100        | 100             | 100        |
| RMSE           | 0.8109     |                 |            |

\*\*\*p < 0.001; \*\*p < 0.01; \*p < 0.05

The estimated model is

$$\hat{Y} = 1.024 + 0.831 X_1 - 0.929 X_2, \ \bar{R}^2 = 0.254$$

As we have one IV for one endogenous regressor,  $\beta$ 's are exactly identified. Running two OLS can replicates the TSLS estimates. However, this procedure tends to underestimate the SE of the IV estimator, which would make statistical inference (t-statistics, p-values, and confidence intervals, etc.) invalid.



(f) Is  $Z_1$  is a weak IV? Test the relevance of  $Z_1$ .

Run a regression of  $X_2$  against  $(1, X_1, Z_1)$ . Compute the F-statistic for the coefficient on  $Z_1$  being 0. The F-statistic = 17.83 > 10 and has essentially 0 p-value. Thus, we can conclude that  $Z_1$  is relevant and sufficiently strong.



(g) Suppose we have another candidate IV,  $Z_2$ . Test the exogeneity of  $Z_2$ .

```
> summary(reg3, diagnostics = TRUE)
Call:
ivreg(formula = y \sim x1 + x2 \mid x1 + z1 + z2)
Residuals:
    Min
              10 Median
                                        Max
-2.61717 -0.82661 0.07949 0.70318 2.28762
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.0174
                        0.1551 6.559 2.64e-09 ***
             1.0123
                       0.2888 3.505 0.000692 ***
x1
x2
            -1.0618
                        0.1357 -7.823 6.38e-12 ***
Diagnostic tests:
                df1 df2 statistic p-value
                2 96
                           23.136 6.30e-09 ***
Weak instruments
Wu-Hausman
                1 96
                           68.293 7.83e-13 ***
                           0.855
                                    0.355
Sargan
                  1 NA
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 1.107 on 97 degrees of freedom
Multiple R-Squared: 0.07808, Adjusted R-squared: 0.05907
Wald test: 32.56 on 2 and 97 DF, p-value: 1.519e-11
```

We conduct the overidentifying restrictions test. The resulting p-value = 0.355 is large. Hence, we do not reject the null hypothesis that  $Z_2$  is exogenous.



(h) Now suppose both  $Z_1$  and  $Z_2$  are valid IV. Estimate (1) using both  $Z_1$  and  $Z_2$ . How many IV do you want to use to estimate  $\beta_2$ ? Explain your answer.

|                | Table 2         | 2: TSLS    |            |
|----------------|-----------------|------------|------------|
|                | (1)             | (2)        | (3)        |
| (Intercept)    | 1.0445***       | 1.0244***  | 1.0174***  |
|                | (0.1154)        | (0.1383)   | (0.1551)   |
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|                | (0.1759)        | (0.3126)   | (0.2888)   |
| x2             | $-0.5430^{***}$ | -0.9289*** | -1.0618*** |
|                | (0.0561)        | (0.1775)   | (0.1357)   |
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| $Adj. R^2$     | 0.4948          | 0.2537     | 0.0591     |
| Num. obs.      | 100             | 100        | 100        |
| RMSE           | 0.8109          |            |            |

<sup>\*\*\*</sup>p < 0.001; \*\*p < 0.01; \*p < 0.05

It is better to use both  $Z_1$  and  $Z_2$ . The two TSLS estimations give similar estimates of the two slope coefficients, while the one using both  $Z_1$  and  $Z_2$  has smaller SE.



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# Introductory Econometrics

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# Thank you

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#### Reference

Stock, J. H., & Watson, M. W. (2019). Introduction to Econometrics, Global Edition, 4th edition. Pearson Education Limited.

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