

GAMS Basics

Stefan Vigerske

`stefan@gams.com`



Some of the following material is based on the GAMS lecture material by Josef Kallrath.

Outline

Basic Modeling

Dynamic Models

More GAMS

Outline

Basic Modeling

Dynamic Models

More GAMS

Cows & Pigs Example

Variables:

x_1 the number of cows to purchase

x_2 the number of pigs to purchase

Objective:

$$\text{maximize } z = 3x_1 + 2x_2$$

Constraints:

$$x_1 \in \{0, 1, 2\}$$

$$x_2 \in \{0, 1, 2\}$$

$$x_1 + x_2 \leq 3.5$$

File: cowspigs.gms



Variables

Syntax: [var-type] variable[s] varname [text] {, varname [text]}

- ▶ var-type allows to pre-determine the **Range** of a variable:

Variable type	Range
free (default)	\mathbb{R}
positive	$\mathbb{R}_{\geq 0}$
negative	$\mathbb{R}_{\leq 0}$
binary	$\{0, 1\}$
integer	$\{0, 1, \dots, 100\}$ (!!)
semicont	$\{0\} \cup [\ell, u]$ (default: $\ell = 1, u = \infty$)
semiint	$\{0\} \cup \{\ell, ell + 1, \dots, u\}$ (default: $\ell = 1, u = 100$)
sos1, sos2	special ordered sets of type 1 and 2 (later ...)

- ▶ Examples:

```
variables x, y, objvar;  
positive variable x;  
integer variable z;
```

Variable Attributes

Attributes of a variable:

Attribute	Meaning
.lo	lower bound on variable range
.up	upper bound on variable range
.fx	fixed value for a variable
.l	current primal value (updated by solver)
.m	current dual value (updated by solver)
.scale	scaling factor
.prior	branching priority

► Examples:

```
x.up = 10;  
y.fx = 5.5;  
display z.l;
```

Equations

- ▶ Equations serve to define **restrictions** (constraints) and an **objective function**

Declaration:

- ▶ Syntax: `Equation[s] eqnname [text] {, eqnname [text]} ;`

- ▶ Example:

```
Equation objective    "Objective Function"  
      e1              "First constraint"
```

Equations

- ▶ Equations serve to define **restrictions** (constraints) and an **objective function**

Declaration:

- ▶ Syntax: Equation[s] eqnname [text] {, eqnname [text]} ;

- ▶ Example:

```
Equation objective      "Objective Function"
      e1                "First constraint"
```

Definition:

- ▶ Syntax: eqnname(domainlist).. expression eqn_type expression;

eqn_type	meaning
=e=	=
=g=	≥
=l=	≤
=n=	no relation between left and right side
=x=	for external functions
=c=	for conic constraints
=b=	for logic constraints

- ▶ Example:

```
objective.. objvar =e= 2 * x + 3 * y*y - y + 5 * z ;
e1..          x + y  =l= z;
```


Equation Attributes

Attributes of an equation:

Attribute	Meaning
.l	activity (updated by solver)
.m	current dual value (updated by solver)
.scale	scaling factor

Model statement

- ▶ Model = a collection of equations

- ▶ Syntax:

```
model[s] model_name [text] [/ all | eqn_name {, eqn_name}]  
        {,model_name [text] [/ all | eqn_name {, eqn_name}] };
```

- ▶ Example:

```
model m / all /;  
model m / objective, e1 /;
```

Model statement

- ▶ Model = a collection of equations

- ▶ Syntax:

```
model[s] model_name [text] [/ all | eqn_name {, eqn_name}]  
        {,model_name [text] [/ all | eqn_name {, eqn_name}] };
```

- ▶ Example:

```
model m / all /;  
model m / objective, e1 /;
```

Attributes:

set by user		set by solver	
iterlim	iteration limit	iterusd	number of iterations
reslim	time limit in seconds	resusd	solving time
optcr	relative gap tolerance	modelstat	model status
optfile	number of solver options file	solvestat	solver status
...		...	

Example:

```
m.reslim = 60;      m.optcr = 0;  
solve m minimize objvar using MINLP;  
display m.resusd;
```

Solving a model

- ▶ Passing a model to a solver and evaluation of results
- ▶ Specification of **one free variable** to be minimized or maximized
- ▶ Syntax:

```
solve modelname using modeltyp maximizing|minimizing varname|;  
solve modelname maximizing|minimizing varname using modeltyp ;
```

- ▶ the **model type** defines the problem class to be used for the model:

LP	a linear problem
QCP	quadratically constraint problem (only linear and quadratic terms)
NLP	a nonlinear problem with continuous functions
DNLP	a nonlinear problem with discontinuous functions
MIP	a mixed-integer linear problem
MIQCP	a mixed-integer quadratically constraint problem
MINLP	a mixed-integer nonlinear problem
CNS	a nonlinear constraint satisfaction problem (no objective function)
RMIP,...	a mixed-integer problem with relaxed integrality restrictions

- ▶ Example:

```
solve m using MINLP minimizing objvar;  
solve m using RMINLP min          objvar;
```

GAMS command line call

Calling GAMS from the command line:

```
$ gams <modelfile> { [-]key=value | key value }
```

Examples:

- ▶ `gams trnsport.gms`
- ▶ `gams trnsport`
- ▶ `gams trnsport.gms LP=CBC`
- ▶ `gams trnsport LP CBC`
- ▶ `gams trnsport -LP CBC`

Listing File

Running a GAMS model generates a listing file (.lst file).

Compilation Errors:

- ▶ are indicated by ****
- ▶ contain a '\$' directly below the point at which the compiler thinks the error occurred
- ▶ are explained near the end of the line-numbered listing part
- ▶ in the IDE, they are also indicated by red lines in the process (log) window (can be double-clicked)
- ▶ check carefully for the cause of the first error, fix it, and try again
- ▶ usual causes: undefined / undeclared symbols (parameters, variables, equations), unmatched brackets, missing semi-colons

Listing File: Equation and Column Listing

Equation Listing:

- ▶ listing of generated equations with **sets unrolled**, **parameters removed**, ...
- ▶ useful for **model debugging**: is the intended model generated?
- ▶ for nonlinear equations, a **linearization in the starting point** is shown

```
AcidDef..  AcidDilut*AcidErr  =e= 35.82-22.2*F4Perf;  
-> AcidDef..  (1)*AcidDilut + 22.2*F4Perf + (3.6)*aciderr =E=  
35.82 ; (LHS = 35.79, INFES = 0.03 ****)
```

- ▶ **activity and violation** of constraint in starting point also shown

Listing File: Equation and Column Listing

Equation Listing:

- ▶ listing of generated equations with **sets unrolled**, **parameters removed**, ...
- ▶ useful for **model debugging**: is the intended model generated?
- ▶ for nonlinear equations, a **linearization in the starting point** is shown

```
AcidDef..  AcidDilut*AcidErr  =e= 35.82-22.2*F4Perf;  
-> AcidDef..  (1)*AcidDilut + 22.2*F4Perf + (3.6)*aciderr =E=  
35.82 ; (LHS = 35.79, INFES = 0.03 ****)
```

- ▶ **activity and violation** of constraint in starting point also shown

Column Listing:

- ▶ shows coefficients, bounds, starting values for generated variables

```
-- F4Perf  F4 Performance Number
```

F4Perf

```
                (.LO, .L, .UP, .M = 1.45, 1.45, 1.62, 0)  
22.2            AcidDef  
(1)            F4Def
```


Listing File: Solve Summary

- ▶ generated for each solve command
- ▶ reporting status and result of solve

S O L V E S U M M A R Y

MODEL	m	OBJECTIVE	F
TYPE	NLP	DIRECTION	MINIMIZE
SOLVER	CONOPT	FROM LINE	85

```
**** SOLVER STATUS      1 Normal Completion
**** MODEL STATUS      2 Locally Optimal
**** OBJECTIVE VALUE   -1.7650
```

RESOURCE USAGE, LIMIT	0.006	1000.000
ITERATION COUNT, LIMIT	16	2000000000
EVALUATION ERRORS	0	0

Listing File: Solution Listing

- ▶ equation and variable **primal and dual values and bounds**
- ▶ **marking** of infeasibilities, “non-optimality”, and unboundedness
- ▶ ‘.’ = zero

	LOWER	LEVEL	UPPER	MARGINAL	
-- EQU Objective	.	.	.	1.0000	
-- EQU AlkylShrnk	.	.	.	-4.6116	
-- EQU AcidBal	.	-0.0020	.	11.8406	INFES
-- EQU IsobutBal	.	0.0952	.	0.0563	INFES
-- EQU AlkylDef	.	0.0127	.	-1.0763	INFES
-- EQU OctDef	0.5743	0.5747	0.5743	-25.9326	INFES
-- EQU AcidDef	35.8200	35.8533	35.8200	0.2131	INFES
-- EQU F4Def	-1.3300	-1.3300	-1.3300	-4.1992	
	LOWER	LEVEL	UPPER	MARGINAL	
-- VAR F	-INF	-1.4143	+INF	.	
-- VAR OlefinFeed	.	1.6198	2.0000	-0.1269	NOPT
-- VAR IsobutRec	.	1.3617	1.6000	-0.2133	NOPT
-- VAR AcidFeed	.	0.7185	1.2000	-0.0411	NOPT
-- VAR AlkylYld	.	2.8790	5.0000	-0.0076	NOPT
-- VAR IsobutMak	.	1.8926	2.0000	-0.4764	NOPT
-- VAR AcidStren	0.8500	0.8998	0.9300	0.5273	NOPT

Cows & Pigs Continued

Define:

- ▶ a set of animals (i)
- ▶ a parameter with profit for each animal ($p(i)$)
- ▶ a parameter with maximal number for each animal ($x_{\max}(i)$)
- ▶ a parameter for the max number of all animals (maxanimal)
- ▶ an integer variable to count how many of each animal to buy ($x(i)$)
- ▶ a real variable to hold the profit (profit)
- ▶ an equation to define the objective
- ▶ an equation to limit the total number of purchased animals by maxanimal

Fill sets and parameters with the data from the original example:

- ▶ 2 animals: cow and pig
- ▶ profit for cow: 3 profit for pig: 2
- ▶ maximal number of cows: 2 maximal number of pigs: 2
- ▶ maximal number of animals: 3.5

File: cowspigs2.gms

Sets

- ▶ Basic elements of a model
- ▶ Syntax:

```
set set_name ["text"] [/element ["text"] {,element ["text"]} /]  
    {,set_name ["text"] [/element ["text"] {,element ["text"]} /]} ;
```

Sets

- ▶ Basic elements of a model

- ▶ Syntax:

```
set set_name ["text"] [/element ["text"] {,element ["text"]} /]  
    {,set_name ["text"] [/element ["text"] {,element ["text"]} /]} ;
```

- ▶ Name set_name is identifier

- ▶ Elements have up to 63 characters, start with letter or digit or are quoted:

```
A    Phos-Acid    September    1986    1952-53    Line-1  
'*TOTAL*'    '10%incr'    '12"/foot'    "Line 1"
```

- ▶ Elements have **no value** (!), that is, '1986' does not have the numerical value 1986 and '01' \neq '1'
- ▶ Text has up to 254 characters, all in one line

Sets

- ▶ Basic elements of a model

- ▶ Syntax:

```
set set_name ["text"] [/element ["text"] {,element ["text"]} /]  
    {,set_name ["text"] [/element ["text"] {,element ["text"]} /]} ;
```

- ▶ Name set_name is identifier

- ▶ Elements have up to 63 characters, start with letter or digit or are quoted:

```
A    Phos-Acid    September    1986    1952-53    Line-1  
'*TOTAL*'    '10%incr'    '12"/foot'    "Line 1"
```

- ▶ Elements have **no value** (!), that is, '1986' does not have the numerical value 1986 and '01' \neq '1'

- ▶ Text has up to 254 characters, all in one line

- ▶ Example:

```
Set n    Nutrients  
/ Prot   "Protein (mg)"  
    VitA  "Vitamine A",    VitC    'Vitamine C',  
    Calc  Calcium  
/;
```

Sequences, Alias

Sequences in Sets: *-Notation

- ▶ `set t "time" / 2000*2008 /;`
corresponds to
`set t "time" / 2000,2001,2002,2003,2004,2005,2006,2007,2008 /;`
- ▶ `a1bc*a20bc` is different from `a01bc*a20bc`
- ▶ the following are **wrong**: `a1x1*a9x9`, `a1*b9`

Sequences, Alias

Sequences in Sets: *-Notation

- ▶ `set t "time" / 2000*2008 /;`
corresponds to
`set t "time" / 2000,2001,2002,2003,2004,2005,2006,2007,2008 /;`
- ▶ `a1bc*a20bc` is different from `a01bc*a20bc`
- ▶ the following are **wrong**: `a1x1*a9x9`, `a1*b9`

Several names for one set: alias command

- ▶ Syntax: `alias(set_name, set_name \{, set_name\})`
- ▶ Example:
`set ice / chocolate, strawberry, cherry, vanilla /;`
`alias(ice, icecreme, gelado, sorvete);`

Data

- ▶ data in GAMS consists always of **real numbers** (no strings)
- ▶ uninitialized data has the **default value 0**
- ▶ 3 forms to declare data:
 - ▶ **Scalar**: a single (scalar) data
 - ▶ **Parameter**: list oriented data
 - ▶ **Table**: table oriented data (at least 2 dimensions)

Data

- ▶ data in GAMS consists always of **real numbers** (no strings)
- ▶ uninitialized data has the **default value 0**
- ▶ 3 forms to declare data:
 - ▶ **Scalar**: a single (scalar) data
 - ▶ **Parameter**: list oriented data
 - ▶ **Table**: table oriented data (at least 2 dimensions)

Scalar Data:

- ▶ Syntax:

```
scalar[s] scalar_name [text] [/signed_num/]  
        { scalar_name [text] [/signed_num/] };
```
- ▶ Example:

```
Scalars rho Discountfactor / .15 /  
        izf internal rate of return;
```

Data: Parameters

Parameter:

- ▶ can be indexed over a one or several sets
- ▶ Syntax:

```
parameter[s] param_name [text] [/ element [=] signed_num  
                                {,element [=] signed_num} /]  
    {,param_name [text] [/ element [=] signed_num  
                                {,element [=] signed_num} /] } ;
```

- ▶ Example:

```
set ice icecreams / chocolate, strawberry, cherry, vanilla /;  
parameter demand(ice) / chocolate 50, strawberry = 30  
                                vanilla    20 /
```

- ▶ Example:

```
set c 'countries' / jamaica, haiti, guyana, brazil /;  
parameter demand(c,ice) "Demand of icecream per country (t)"  
    / Jamaica.Chocolate 300, Jamaica.Strawberry 50, Jamaica.Cherry 5  
    Haiti.(Chocolate,Vanilla,Strawberry) = 30,  
    (Guyana,Brazil).Chocolate 100 /
```

Data: Tables

Tables:

- Syntax:

```
table table_name [text] EOL
      element    { element }
      element signed_num { signed_num } EOL
      {element signed_num { signed_num } EOL} ;
```

- Example:

```
table demand(c,ice) "Demand of icecream per country (t)"
      Chocolate Strawberry Cherry Vanilla
Jamaica          300          50          5
Haiti            30          30          30
(Guyana,Brazilien) 100          ;
```

- no “free form”: **position** of elements is of importance
- tables with more than 2 dimensions are also possible

Data: Assignments

► Scalar Assignment:

```
scalar x / 1.5 /;  
x = 1.2;  
x = x + 2;
```

► Indexed Assignment:

```
Set row          / r1*r10 /  
    col          / c1*c10 /  
    subrow(row) / r7*r10 /;  
Parameter a(row,col), r(row), c(col);  
a(row,col)      = 13.2 + r(row)*c(col);  
a('r7','c4')    = -2.36;  
  
a(subrow,'c10') = 2.44 - 33*r(subrow);  
  
a(row,row)      = 7.7 - r(row);  
alias(row,rowp);  
a(row,rowp)     = 7.7 - r(row) + r(rowp);
```

Data: Expressions

Expression: an arbitrarily complex calculation instruction

Arithmetic operators: `**` (exponentiate), `+`, `-`, `*`, `/`

- ▶ `x = 5 + 4*3**2;`
`x = 5 + 4*(3**2);`
- ▶ `x**n` corresponds to $\exp(n \cdot \log(x)) \Rightarrow$ only allowed for $x > 0$
- ▶ `population(t) = 56*(1.015**(ord(t)-1))`

Data: Expressions

Expression: an arbitrarily complex calculation instruction

Arithmetic operators: ** (exponentiate), +, -, *, /

- ▶ `x = 5 + 4*3**2;`
`x = 5 + 4*(3**2);`
- ▶ `x**n` corresponds to $\exp(n \cdot \log(x)) \Rightarrow$ only allowed for $x > 0$
- ▶ `population(t) = 56*(1.015**(ord(t)-1))`

Indexed Operations:

- ▶ Syntax: `indexed_op((controlling_indices), expressions)`
- ▶ `indexed_op` can be: `sum`, `prod`, `smin`, `smax`

```
parameter demand(c,ice) "demand (t)"
        totaldemand(c) "totaler demand per country (t)"
        completedemand "totaler demand for all countries (t)"
        mindemand(ice) "minimal demand per icecream";

totaldemand(c) = sum(ice,      demand(c,ice));
completedemand = sum((ice,c), demand(c,ice));
mindemand(ice) = smin(c,      demand(c,ice));
```

Data: Expressions

Expression: an arbitrarily complex calculation instruction

Arithmetic operators: `**` (exponentiate), `+`, `-`, `*`, `/`

- ▶ `x = 5 + 4*3**2;`
`x = 5 + 4*(3**2);`
- ▶ `x**n` corresponds to $\exp(n \cdot \log(x)) \Rightarrow$ only allowed for $x > 0$
- ▶ `population(t) = 56*(1.015**(ord(t)-1))` (+ - 1)

Indexed Operations:

- ▶ Syntax: `indexed_op((controlling_indices), expressions)`
- ▶ `indexed_op` can be: `sum`, `prod`, `smin`, `smax`

```
parameter demand(c,ice) "demand (t)"
      totaldemand(c) "totaler demand per country (t)"
      completedemand "totaler demand for all countries (t)"
      mindemand(ice) "minimal demand per icecream";

totaldemand(c) = sum(ice,      demand(c,ice));
completedemand = sum((ice,c), demand(c,ice));
mindemand(ice) = smin(c,      demand(c,ice));
```

Functions: `errorf(x)`, `exp(x)`, `power(x,n)`, `sqr(x)`, `uniform(a,b)`,
`normal(mean,sdev)`, ...

What the Solve Statement is doing

At each **Solve** statement, the following happens...

1. The model (= list of (indexed) equations) is compiled into a **model instance**, that is, a scalar (= no indices) list of constraints and those variables, that appear in at least one constraint.
(The **Equation Listing** and **Column Listing** shows in the listing file shows parts of this model.)
2. Instance statistics are written to the log:

```
--- Generating NLP model m  
--- alkyl.gms(85) 5 Mb  
--- 8 rows 15 columns 32 non-zeroes  
--- 54 nl-code 19 nl-non-zeroes
```
3. Some error check is performed.
4. The instance is passed on to a solver and processed there.

```
--- Executing IPOPT: elapsed 0:00:00.093  
[solver log]  
--- Restarting execution
```
5. The result (model and solution status, solution, statistical information) is passed back to GAMS and reported in the listing file.

Solver Status

Solver status: state of the solver program

- | | |
|------------|--|
| 1 | Normal Completion |
| 2 | Iteration Interrupt |
| 3 | Resource Interrupt (timelimit reached) |
| 4 | Terminated by Solver |
| 5 | Evaluation Error Limit |
| 6 | Capability Problems |
| 7 | Licensing Problems |
| 8 | User Interrupt |
| 9, ..., 13 | setup, solver, system errors |

Model Status

Model status: what the solution looks like

1	Optimal (global optimality)
2, 8	Locally Optimal
3, 18	Unbounded
4, 10, 19	Infeasible (proven to be infeasible)
5	Locally Infeasible
6	Intermediate Infeasible
7	Intermediate Nonoptimal (feasible for continuous models)
9	Intermediate Non-integer
11	License Problem
12, 13	Error
14	No Solution (but expected so)
15, 16, 17	Solved for CNS models

Option command

- ▶ specification of [systemwide parameters](#) to control output, solving process, ...
- ▶ Syntax:
option keyword1 [= value1] { ,|EOL keyword2 = [value2] }
- ▶ some important parameters:

keyword	meaning	default
iterlim	iteration limit	2000000000
reslim	time limit	1000 (!!)
optca	absolute gap tolerance	0.0
optcr	relative gap tolerance	0.1 (!!)
LP	choice of LP solver	CPLEX
NLP	choice of NLP solver	CONOPT
...		

- ▶ Example:
option iterlim = 100, optcr = 0;
solve icesale using mip min kosten;
option mip = cbc;
solve icesale using mip min kosten;
- ▶ options can also be set on the [command line](#):
> gams icesale.gms mip=cbc optcr=0

Display command

- ▶ display sets, data, variable/equation/model attributes in the listing file

- ▶ Examples:

```
display ice, sorbet;  
display x.l, x.m;  
display demand;  
display satdemand.m;
```

- ▶ only non-zero values are displayed
- ▶ control number of digits after the decimal point for all displayed values
option decimals = 1 ;
- ▶ number of digits after the decimal point for variable x:
option x:6 ;

Outline

Basic Modeling

Dynamic Models

More GAMS

Cows & Pigs by Complete Enumeration (!) in GAMS

x_1 the number of cows to purchase ($x_1 \in \{0, 1, 2\}$)

x_2 the number of pigs to purchase ($x_2 \in \{0, 1, 2\}$)

maximize $z = 3x_1 + 2x_2$

such that $x_1 + x_2 \leq 3.5$

Cows & Pigs by Complete Enumeration (!) in GAMS

x_1 the number of cows to purchase ($x_1 \in \{0, 1, 2\}$)

x_2 the number of pigs to purchase ($x_2 \in \{0, 1, 2\}$)

maximize $z = 3x_1 + 2x_2$

such that $x_1 + x_2 \leq 3.5$

```
scalar x1, x2, obj;  
scalar objbest, x1best, x2best;  
objbest = 0;  
for( x1 = 0 to 2,  
    for( x2 = 0 to 2,  
        if( x1 + x2 le 3,  
            obj = 3*x1 + 2*x2;  
            if( obj > objbest,  
                x1best = x1;  
                x2best = x2;  
                objbest = obj;  
            ) )) )  
display x1best, x2best, objbest;
```

File: cowspigsenum.gms

Finding a good local optimum to a NLP: Multistart

- ▶ Starting an NLP solver from different starting points and pick the best solution.
- ▶ If we don't know how to pick a good point, let's pick one randomly.

Finding a good local optimum to a NLP: Multistart

- ▶ Starting an NLP solver from different starting points and pick the best solution.
- ▶ If we don't know how to pick a good point, let's pick one randomly.
- ▶ **Multistart algorithm:**
 1. $f^U = \infty$
 2. for $k = 1$ to N , do
 - 2.1 Generate starting point x uniformly at random over $[\underline{x}, \overline{x}]$.
 - 2.2 Run NLP solver from x and obtain solution x^* .
 - 2.3 if $f(x^*) < f^U$: $f^U = f(x^*)$ and $x^U = x^*$
 3. Return x^U and f^U .
- ▶ The GAMS solver **MSNLP** implements such an algorithm.

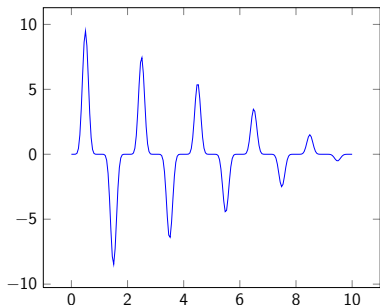
Finding a good local optimum to a NLP: Multistart

- ▶ Starting an NLP solver from different starting points and pick the best solution.
- ▶ If we don't know how to pick a good point, let's pick one randomly.
- ▶ **Multistart algorithm:**
 1. $f^U = \infty$
 2. for $k = 1$ to N , do
 - 2.1 Generate starting point x uniformly at random over $[x, \bar{x}]$.
 - 2.2 Run NLP solver from x and obtain solution x^* .
 - 2.3 if $f(x^*) < f^U$: $f^U = f(x^*)$ and $x^U = x^*$
 3. Return x^U and f^U .
- ▶ The GAMS solver **MSNLP** implements such an algorithm.

- ▶ Example:

$$\begin{aligned} \max_{x \in [0,10]} \phi(x), \\ \text{where } \phi(x) = (10 - x) \sin^9(2\pi x) \end{aligned}$$

- ▶ Optimal solution:
 $x = 0.24971128$, $\phi(x) = 9.75014433$
- ▶ File: `nlpsin.gms`



Program flow control, loop command

- ▶ controlling the execution of a GAMS program
- ▶ commands: `loop`, `if-else`, `while`, `for`
- ▶ declarations and definition of equations are not allowed inside these commands
- ▶ solve statements are allowed

Program flow control, loop command

- ▶ controlling the execution of a GAMS program
- ▶ commands: `loop`, `if-else`, `while`, `for`
- ▶ declarations and definition of equations are not allowed inside these commands
- ▶ solve statements are allowed

`loop` command:

- ▶ Syntax:

```
loop(controllingset[$(condition)],  
      statement {; statement}  
    );
```

- ▶ Example:

```
set t / 1985*1990 /;  
parameter pop(t) / 1985  3456 /  
           growth(t) / 1985  25.3,  1986  27.3,  1987  26.2,  
                      1988  27.1,  1989  26.6,  1990  26.6 /;  
loop(t, pop(t+1) = pop(t) + growth(t));
```

If-Elseif-Else command

► Syntax:

```
if( condition, statement {; statement};  
{elseif condition, statement {; statement}; }  
[else statement {; statement};]  
);
```

► Example:

```
if( (ml.modelstat eq 4),  
*      model ml was infeasible,  
*      relax bound and solve again  
  x.up(j) = 2*x.up(j);  
  solve ml using lp min z;  
elseif ml.modelstat eq 1,  
  display x.l;  
else  
  abort "Error solving the model";  
);
```

While, Repeat commands

While command:

► Syntax: `while(condition, statement \{; statement\};);`

► Example:

```
scalar count / 1 /;  
scalar globmin / inf /;  
while(count le 1000,  
    x.l(j) = uniform(x.lo(j), x.up(j));  
    solve ml using nlp min obj;  
    if ( obj.l le globmin, globmin = obj.l; );  
    count = count + 1;  
);
```

While, Repeat commands

While command:

- ▶ Syntax: `while(condition, statement \{; statement\};);`
- ▶ Example:

```
scalar count / 1 /;
scalar globmin / inf /;
while(count le 1000,
  x.l(j) = uniform(x.lo(j), x.up(j));
  solve ml using nlp min obj;
  if ( obj.l le globmin, globmin = obj.l; );
  count = count + 1;
);
```

Repeat command:

- ▶ Syntax: `repeat(statement \{; statement\}; until condition);`
- ▶ Example:

```
scalar count / 1 /; scalar globmin / inf /;
repeat( x.l(j) = uniform(x.lo(j), x.up(j));
  solve ml using nlp min obj;
  if ( obj.l le globmin, globmin = obj.l; );
  count = count + 1;
until count eq 1000 );
```


For command

```
for(i = start to|downto end [by incr], statement \{; statement\};);
```

- ▶ Note: i is a **scalar**, not a set
- ▶ start, end, and incr can be **real** numbers, but incr needs to be positive
- ▶ Example:

```
scalar count;  
scalar globmin / inf /;  
for( count = 1 to 1000,  
    x.l(j) = uniform(x.lo(j), x.up(j));  
    solve ml using nlp min obj;  
    if ( obj.l le globmin, globmin = obj.l; );  
);
```

Subsets, Cardinality

Subsets:

- ▶ Syntax for $\text{set_name1} \subseteq \text{set_name2}$: `set set_name1 (set_name2);`
- ▶ Example:
`set ice / chocolate, strawberry, cherry, vanilla /;`
`set sorbet(ice) / strawberry, cherry /;`
- ▶ Domain checking: `set sorbet(ice) / strawberry, banana /;` \Rightarrow **error**

Subsets, Cardinality

Subsets:



- ▶ Syntax for $\text{set_name1} \subseteq \text{set_name2}$: `set set_name1 (set_name2);`
- ▶ Example:

```
set ice / chocolate, strawberry, cherry, vanilla /;  
set sorbet(ice) / strawberry, cherry /;
```
- ▶ Domain checking: `set sorbet(ice) / strawberry, banana /;` \Rightarrow error

Card(set)

- ▶ gives the number of elements in a set
- ▶ Example:

```
set c      'countries' / jamaica, haiti, guyana, brazil /;  
scalar nc 'number of countries';  
nc = card(c);
```

Ordered Sets

Lag & Lead Operations:

- ▶ allow to access **neighbors** (next or further distant) of a elements in a priori explicitly specified **ordered set**
- ▶ Syntax: `setelement \pm n`
- ▶ Note: `x(setelement+n)` is **zero** if position of `setelement` $>$ `card(set)-n`
- ▶ Example:

```
Set t / 1*24 /;
```

```
Variables level(t), inflow(t), outflow(t);
```

```
Equation balance(t) couple fill levels of reservoir over time;
```

```
* implicitly assume an initial fill level of zero
```

```
balance(t).. level(t) =e= level(t-1) + inflow(t) - outflow(t);
```

Ordered Sets

Lag & Lead Operations:

- ▶ allow to access **neighbors** (next or further distant) of a elements in a priori explicitly specified **ordered set**
- ▶ Syntax: `setelement \pm n`
- ▶ Note: `x(setelement+n)` is **zero** if position of `setelement` $>$ `card(set)-n`
- ▶ Example:

```
Set t / 1*24 /;  
Variables level(t), inflow(t), outflow(t);  
Equation balance(t) couple fill levels of reservoir over time;  
* implicitly assume an initial fill level of zero  
balance(t).. level(t) = level(t-1) + inflow(t) - outflow(t);
```

Ord(setelement):

- ▶ gives **position of an element** in an a priori explicitly specified **ordered sets**
- ▶ Example:

```
Set t / 1*24 /;  
Parameter hour(t);  
hour(t) = ord(t);
```

Dynamic Sets

- ▶ dynamic sets allow elements to be **added** or **removed**
- ▶ dynamic sets are usually **domain-checked**, i.e., **subsets**
- ▶ Syntax: `setname(othersetelement) = yes | no` (add/remove single element)
- ▶ Syntax: `setname(subset) = yes | no` (add/remove another subset)
- ▶ Example:

```
set ice / chocolate, strawberry, cherry, vanilla /;  
Parameter demand(ice) / chocolate 1000, strawberry 500,  
                        cherry 10, vanilla 100 /;
```

```
set sorbet(ice);  
sorbet(ice) = yes;  
sorbet('chocolate') = no;   sorbet('vanilla') = no;
```

```
Set highdemand(ice) ice creams with high demand;  
highdemand(ice) = (demand(ice) >= 500);
```

- ▶ most often used as **controlling index** in an assignment or equation definition

```
Scalar sumhighdemand;  
sumhighdemand = sum(highdemand, demand(highdemand));
```

Example: refer to first/last period of discrete-time models

Set t / 1*24 /;

Sets **tb(t)** base period

tn(t) non-base periods

tt(t) terminal period;

tb(t) = (ord(t) = 1);

tn(t) = (ord(t) > 1);

tt(t) = (ord(t) = card(t));

Variables level(t), inflow(t), outflow(t);

Equations **balance(t)** couple fill levels of reservoir over time

basebalance(t) define fill level for base period;

* only for time periods > base period

balance(tn(t)).. **level(t)** =e= **level(t-1)** + **inflow(t)** - **outflow(t)**;

* only for base period

basebalance(tb).. **level(tb)** =e= 100 + **inflow(tb)** - **outflow(tb)**;

* lower bound on fill level in terminal period

level.lo(tt) = 100;

Alternatively (but less readable):

equation **basebalance**; **basebalance**..

sum(tb, level(tb)) =e= 100 + **sum(tb, inflow(tb) - outflow(tb))**;



Outline

Basic Modeling

Dynamic Models

More GAMS

Multidimensional Sets

Multidimensional Sets:

- ▶ describing **assignments** (relations) between sets
- ▶ Example:

```
sets c  'countries'  / jamaica, haiti, guyana, brazil /  
     h  'harbors'    / kingston, s-domingo, georgetown, belem /  
set   hc(h, c)  harbor to country relation  
      / kingston.jamaica,   s-domingo.haiti  
      georgetown.guyana,   belem.brazil /;
```

sameas and diag

`sameas`(setelement, otherelement) and `sameas`(setelement, "text")

`diag`(setelement, otherelement) and `diag`(setelement, "text")

- ▶ `sameas` returns true if **identifiers** for given set elements **are the same**, or if identifier of one set element equals a given text
- ▶ `sameas` can also be **used as a set**
- ▶ `diag` is like `sameas`, but return **1 if true**, and **0 otherwise**
- ▶ Example:

```
sets ice1 / chocolate, strawberry, cherry, vanilla /  
      ice2 / strawberry, cherry, banana /;  
scalar ncommon;  
ncommon = sum((ice1, ice2), diag(ice1,ice2));  
ncommon = sum(sameas(ice1, ice2), 1);
```

Conditional expressions: \$ Operator

Boolean Operators:

- ▶ numerical operators: `lt`, `<`, `le`, `<=`, `eq`, `=`, `ne`, `<>`, `ge`, `>=`, `gt`, `>`
- ▶ logical operators: `not`, `and`, `or`, `xor`
- ▶ set membership: `a(i)` evaluates to *true* if and only if `i` is contained in the (sub)set `a`, otherwise *false*
- ▶ *true* corresponds to 1, *false* to 0

Conditional expressions: \$ Operator

Boolean Operators:

- ▶ numerical operators: `lt`, `<`, `le`, `<=`, `eq`, `=`, `ne`, `<>`, `ge`, `>=`, `gt`, `>`
- ▶ logical operators: `not`, `and`, `or`, `xor`
- ▶ set membership: `a(i)` evaluates to *true* if and only if `i` is contained in the (sub)set `a`, otherwise *false*
- ▶ *true* corresponds to 1, *false* to 0

\$-Operator:

- ▶ allows to **apply necessary conditions**
- ▶ `$(condition)` can be read as "if condition is true" **Cond.**
- ▶ Example:
"If `b > 1.5`, then let `a = 2`." $\Rightarrow a$(b > 1.5) = 2$; ✓
"If `b > 1.5`, then let `a = 2`, otherwise let `a = 0`." $\Rightarrow a = 2$(b > 1.5)$;
- ▶ \$ on **left side**: **no assignment**, if condition not satisfied
- ▶ \$ on **right side**: **always assignment**, but term with \$ **evaluates to 0**, if condition not satisfied
- ▶ cannot be used in declarations

Applications for \$ Operator

Filtering in indexed operations:

```
parameter sorbetbalance;  
set ice; set sorbet(ice);  
sorbetbalance = sum(ice$sorbet(ice), price(ice)*purchase.l(ice));  
sorbetbalance = sum(sorbet(ice), price(ice) * purchase.l(ice));
```

Applications for \$ Operator

Filtering in indexed operations:

```
parameter sorbetbalance;  
set ice; set sorbet(ice);  
sorbetbalance = sum(ice$sorbet(ice), price(ice)*purchase.l(ice));  
sorbetbalance = sum(sorbet(ice), price(ice) * purchase.l(ice));
```

Conditioned indexed operations:

```
rho = sum(i$(sig(i) ne 0), 1/sig(i) - 1);
```

Applications for \$ Operator

Filtering in indexed operations:

```
parameter sorbetbalance;  
set ice; set sorbet(ice);  
sorbetbalance = sum(ice$sorbet(ice), price(ice)*purchase.l(ice));  
sorbetbalance = sum(sorbet(ice), price(ice) * purchase.l(ice));
```

Conditioned indexed operations:

```
rho = sum(i$(sig(i) ne 0), 1/sig(i) - 1);
```

Conditioned equations:

```
Equation satdemand(ice);  
satdemand(ice)$sorbet(ice).. purchase(ice) =g= demand(ice);
```

```
balance(t)$(ord(t)>1)..   
level(t) =e= level(t-1) + inflow(t) - outflow(t);
```

Existence of variables in constraints:

```
variables x, y;    parameter A;    equation e;  
e.. x + y$(A>2) =e= A;
```

No Variables in \$ condition

- ▶ The following **DOES NOT WORK**:

```
binary variable x; variable y; equation e1, e2;  
e1$(x = 1).. y =l= 100;  
e2 .. y$(x = 1) =l= 100;
```

- ▶ The value of **x is decided by the solver**, not by the GAMS.
- ▶ However, GAMS has to evaluate \$-operators when assembling an instance in the Solve statement.
- ▶ Instead, you have to **reformulate**:

```
e.. y =l= 100 * x + y.up * (1-x);
```

That is: $x=1 \Rightarrow y \leq 100$; $x=0 \Rightarrow y \leq y.up$.

Compilation vs. Execution

GAMS processed models in 2 phases:

Compilation Phase:

- ▶ reads the complete GAMS model and **translate** into GAMS specific byte code
- ▶ **processes declarations** (variables, equations, sets, parameters)
- ▶ execute all **compile-time commands** (next slides)
- ▶ Listing file:

```
GAMS 24.1.2 r40979 Released Jun 16, 2013 LEX-LEG x86_64/Linux
```

```
3 16:03:38 Page 1
```

```
A Transportation Problem (TRANSPORT,SEQ=1)
```

```
C o m p i l a t i o n
```

```
<echo of all processed lines>
```

```
COMPILATION TIME      =          0.002 SECONDS      3 MB  24.1.2 r4  
...
```

Execution Phase:

- ▶ **executes commands** in program: assignments, solve, loop, while, for, if, ...

Compile Time Commands

- ▶ introduced by **\$ sign in the first column** (!)
- ▶ Syntax: `$commandname argumentlist {commandname argumentlist}`
- ▶ modify **behavior of GAMS compiler**, e.g., how to process the input, customizing output
- ▶ allow **program flow control on compilation level**: call external programs, include other files, if-else, goto, ...
- ▶ modifying and reading **compile-time variables**

Examples:

- ▶ define a title for your GAMS program
`$Title A Transportation Problem`
- ▶ define a section that contains only comments
`$onText`
This problem finds a least cost shipping schedule that meets requirements at markets and supplies at factories.
`$offText`
- ▶ disable echoing of input lines in listing file
`$offListing`

Compile Time Variables

- ▶ compile-time variables hold strings
- ▶ their value is accessed via the `%variablename%` notation
- ▶ values are assigned via `$set` or `$eval` commands or on the GAMS command line via double-dash-options: `gams --variablename variablevalue`
- ▶ for `$eval`, the variable value string is interpreted as numerical expression
- ▶ Example:

```
$set  N      10  
$eval Nsqr %N% * %N%  
set i / 1 * %N% /;
```
- ▶ variants `$setLocal`, `$setGlobal`, `$evalLocal`, `$evalGlobal` allow to control the (file)scope of a variable

Compile Time Program Control: \$If

- ▶ **\$If** allows to do conditional processing
- ▶ Syntax:
\$If [not] (exist filename | string1 == string2) new_input_line
- ▶ **only one-line** clauses allowed (new_input_line can be on next line, though)
- ▶ Examples:

```
$if exist myfile.dat $log "myfile.dat exists, yeah!"
```

```
scalar a;
```

```
$if %difficulty% == easy a = 5;
```

```
$if not %difficulty% == easy a = 10;
```

Compile Time Program Control: \$If

- ▶ **\$If** allows to do conditional processing
- ▶ Syntax:
`$If [not] (exist filename | string1 == string2) new_input_line`
- ▶ **only one-line** clauses allowed (`new_input_line` can be on next line, though)
- ▶ Examples:

```
$if exist myfile.dat $log "myfile.dat exists, yeah!"
```

```
scalar a;  
$if %difficulty% == easy a = 5;  
$if not %difficulty% == easy a = 10;
```

- ▶ **\$IfThen-\$ElseIf-\$Else-\$Endif** allows to control activity for a set of statements; Example:

```
scalar a;  
$ifthen %difficulty% == easy  
a = 5;  
$else  
a = 10;  
$endif
```

Compile Time Program Control: \$Goto

- ▶ **\$Goto-\$Label** allows to skip over or repeat sections of the input
- ▶ Example:

```
scalar a / 5 /;  
$if %difficulty% == easy $goto easy  
a = 10;  
$label easy
```

Executing Shell Commands

- ▶ `$call` passes a following string to the current shell and waits for the command to be completed
- ▶ if the string starts with a '=', the operating system is called directly, i.e., no shell is invoked

- ▶ Example:

```
$call "gamslib trnsport"
```

```
$call "=gams trnsport"
```

```
$if exist myfile.dat $call cp myfile.dat mycopy.dat
```

- ▶ the `errorlevel` function allows to check whether a previous command (e.g., `$call`) executed without error:

```
$call "gamslib trnsport"
```

```
$call "gams trnsport"
```

```
$if errorlevel 1 $abort "ouch! - solving trnsport failed"
```

Writing text files

- ▶ `$Echo` and `$onEcho-$offEcho` allows to write to text files

- ▶ Example:

```
$Echo "hello, world!" > myfile.txt
```

```
$OnEcho >> myfile.txt
```

```
ahoy-hoy!
```

```
$OffEcho
```

- ▶ `> myfile.txt` creates a new file `myfile.txt`, thereby overwriting a possibly existing one of the same name
- ▶ `>> myfile.txt` appends to an existing file `myfile.txt`
- ▶ Recall: These are **compilation-time commands**! Not usable to write solve outcomes or similar; use display command or put-facility (later) for this.

Including text files

- ▶ **\$Include** allows to include ASCII files into a GAMS program
- ▶ compilation is then continued for the included file
- ▶ Example:

```
Parameter d(i,j) distance in thousands of miles;  
$include dist.inc
```

where dist.inc contains

```
Table d(i,j) distance in thousands of miles  
           new-york      chicago      topeka  
seattle    2.5           1.7           1.8  
san-diego  2.5           1.8           1.4 ;
```

Including csv files

- ▶ **\$OnDelim** enables **comma separated value** (csv) format for data in table or parameter statements

Examples:

```
Table d(i,j)  distance
$ondelim
$include dist.csv
$offdelim
;
```

where dist.csv is

```
,new-york,chicago,topeka
seattle,2.5,1.7,1.8
san-diego,2.5,1.8,1.4
```

```
Parameter d(i,j)  distance /
$ondelim
$include dist.txt
$offdelim
/;
```

where dist.txt is

```
SEATTLE,NEW-YORK,2.5
SAN-DIEGO,NEW-YORK,2.5
SEATTLE,CHICAGO,1.7
SAN-DIEGO,CHICAGO,1.8
SEATTLE,TOPEKA,1.8
SAN-DIEGO,TOPEKA,1.4
```

Put Command

- ▶ writing text files at execution time
- ▶ associating an identifier `fileid` with a file: `file fileid / myfile.txt /;`
- ▶ select a stream (and thus a file) to write to: `put fileid;`
- ▶ writing some items (text, labels, numbers): `put item {, item};`
- ▶ write a `linebreak`: `put /;`
- ▶ close a stream: `putclose;`

Put Command

- ▶ writing text files at execution time
- ▶ associating an identifier fileid with a file: file fileid / myfile.txt /;
- ▶ select a stream (and thus a file) to write to: put fileid;
- ▶ writing some items (text, labels, numbers): put item {, item};
- ▶ write a linebreak: put /;
- ▶ close a stream: putclose;
- ▶ Example:

```
file fx /result.txt/;
put fx 'Shipped quantities between plants and markets' /;
put    '-----' /;
loop((i,j)$x.l(i,j),
      put 'Shipment from ', i.te(i):10, ' to ', j.te(j):10,
          ' in cases:', x.l(i,j) /;
); putclose;
```

gives

Shipped quantities between plants and markets

```
-----
Shipment from seattle    to new-york    in cases:   50.00
Shipment from seattle    to chicago     in cases:  300.00
Shipment from san-diego   to new-york    in cases:  275.00
Shipment from san-diego   to topeka      in cases:  275.00
```

Text Items, Formatted Output

Label names and explanatory texts can be accessed via attributes:

- ▶ `ident.ts`: text associated with identifier
- ▶ `element.tl`: label associated with set element
- ▶ `set.te(element)`: text associated with element of set

Text Items, Formatted Output

Label names and explanatory texts can be accessed via attributes:

- ▶ `ident.ts`: text associated with identifier
- ▶ `element.tl`: label associated with set element
- ▶ `set.te(element)`: text associated with element of set

Local Item Formatting:

- ▶ Syntax for formatting item output: `item:{<>}width:decimals`
- ▶ `{<>}` specifies whether justified left (<), right (>), or centered (<>)
- ▶ `width` is the field width
- ▶ `decimals` is the number of decimals for numeric output
- ▶ each can be omitted, e.g., `x.1::5`

Text Items, Formatted Output

Label names and explanatory texts can be accessed via attributes:

- ▶ `ident.ts`: text associated with identifier
- ▶ `element.tl`: label associated with set element
- ▶ `set.te(element)`: text associated with element of set

Local Item Formatting:

- ▶ Syntax for formatting item output: `item:{<>}width:decimals`
- ▶ `{<>}` specifies whether justified left (<), right (>), or centered (<>)
- ▶ `width` is the field width
- ▶ `decimals` is the number of decimals for numeric output
- ▶ each can be omitted, e.g., `x.l::5`

Global Item Formatting:

- ▶ change field justification and width for all items of a type
- ▶ `.lj`, `.nj`, `.sj`, `.tj`, `.lw`, `.nw`, `.sw`, `.tw` attributes of stream identifier
- ▶ see GAMS User's Guide Section 15.10

Text Items, Formatted Output

Label names and explanatory texts can be accessed via attributes:

- ▶ `ident.ts`: text associated with identifier
- ▶ `element.tl`: label associated with set element
- ▶ `set.te(element)`: text associated with element of set

Local Item Formatting:

- ▶ Syntax for formatting item output: `item:{<>}width:decimals`
- ▶ `{<>}` specifies whether justified left (<), right (>), or centered (<>)
- ▶ `width` is the field width
- ▶ `decimals` is the number of decimals for numeric output
- ▶ each can be omitted, e.g., `x.l::5`

Global Item Formatting:

- ▶ change field justification and width for all items of a type
- ▶ `.lj`, `.nj`, `.sj`, `.tj`, `.lw`, `.nw`, `.sw`, `.tw` attributes of stream identifier
- ▶ see GAMS User's Guide Section 15.10

Cursor Positioning:

- ▶ `put @n`; moves cursor to column `n` of current line