☐ 1 ☐ 2 ☐ 3 ☐ 4 ☐ 5 ☐ 6

## Q1. Searching with Heuristics

Consider the A\* searching process on the connected undirected graph, with starting node S and the goal node G. Suppose the

ost for each connection edge is <b>always positive</b> . We define $h^*$	(X) as the shortest (optimal) distance to G from a node X.
nswer Questions (a), (b) and (c). You may want to solve Que	stions (a) and (b) at the same time.
(a) Suppose h is an <b>admissible</b> heuristic, and we conduct A C be the cost of the found path (directed by h', defined i	* <b>tree search</b> using heuristic $h'$ and finally find a solution. Let n part (a)) from S to G
(i) Choose <b>one best</b> answer for each condition below.	
1. If $h'(X) = \frac{1}{2}h(X)$ for all Node X, then	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
2. If $h'(X) = \frac{h(X) + h^*(X)}{2}$ for all Node X, then	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
3. If $h'(X) = h(X) + h^*(X)$ for all Node X, ther	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
4. If we define the set $K(X)$ for a node $X$ as all it always holds	s neighbor nodes Y satisfying $h^*(X) > h^*(Y)$ , and the following
$h'(X) \le \begin{cases} \min_{Y \in K(X)} h(X) \end{cases}$	$h'(Y) - h(Y) + h(X)$ if $K(X) \neq \emptyset$ if $K(X) = \emptyset$
then,	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
5. If $K$ is the same as above, we have	
$h'(X) = \begin{cases} \min_{Y \in K} h(X) \end{cases}$	$h(X) h(Y) + cost(X, Y)$ if $K(X) \neq \emptyset$ if $K(X) = \emptyset$
where $cost(X, Y)$ is the cost of the edge conne	
then,	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
6. If $h'(X) = \min_{Y \in K(X) + \{X\}} h(Y)$ ( <i>K</i> is the same	the as above), $\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
(ii) In which of the conditions above, $h'$ is still <b>admissi</b> we say $h_1$ dominates $h_2$ when $h_1(X) \ge h_2(X)$ hold	<b>ble</b> and for sure to dominate $h$ ? Check all that apply. Remember ls for all $X$ . $1  2  3  4  5  6$
<b>(b)</b> Suppose <i>h</i> is a <b>consistent</b> heuristic, and we conduct A*	
(i) Answer exactly the same questions for each condition	ons in Question (a)(i).
1. $\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$	$S)   2.   C = h^*(S)   C > h^*(S)   C \ge h^*(S)$ $4.   C = h^*(S)   C > h^*(S)   C \ge h^*(S)$ $6.   C = h^*(S)   C > h^*(S)   C \ge h^*(S)$
3. $\bigcup C = h^*(S) \bigcup C > h^*(S) \bigcup C \ge h^*(S)$	$4. \cup C = h^*(S) \cup C > h^*(S) \cup C \ge h^*(S)$
(ii) In which of the conditions above, $h'$ is still <b>consist</b>	ent and for sure to dominate $h$ ? Check all that apply.

(c) Suppose h is an **admissible** heuristic, and we conduct  $A^*$  **tree search** using heuristic h' and finally find a solution.

If  $\epsilon > 0$ , and  $X_0$  is a node in the graph, and h' is a heuristic such that

$$h'(X) = \begin{cases} h(X) & \text{if } X = X_0 \\ h(X) + \epsilon & \text{otherwise} \end{cases}$$

- Alice claims h' can be inadmissible, and hence  $C = h^*(S)$  does not always hold.
- Bob instead thinks the node expansion order directed by h' is the same as the heuristic h'', where

$$h''(X) = \begin{cases} h(X) - \epsilon & \text{if } X = X_0 \\ h(X) & \text{if otherwise} \end{cases}$$

Since h'' is admissible and will lead to  $C = h^*(S)$ , and so does h'. Hence,  $C = h^*(S)$  always holds.

The two conclusions (<u>underlined</u>) apparently contradict with each other, and **only exactly one of them are correct and the other is wrong**. Choose the **best** explanation from below - which student's conclusion is wrong, and why are they wrong?

0	Alice's conclusion is wrong, because the heuristic $h'$ is always admissible.
	Alice's conclusion is wrong, because an inadmissible heuristics does not necessarily always lead to the failure of the hality when conducting $A^*$ tree search.
0	Alice's conclusion is wrong, because of another reason that is not listed above.
	Bob's conclusion is wrong, because the node visiting expansion ordering of $h''$ during searching might not be the as $h'$ .
O 1	Bob's conclusion is wrong, because the heuristic $h''$ might lead to an incomplete search, regardless of its optimally rty.
$\bigcirc$ 1	Bob's conclusion is wrong, because of another reason that is not listed above.

## Q2. Iterative Deepening Search

Pacman is performing search in a maze again! The search graph has a branching factor of b, a solution of depth d, a maximum depth of m, and edge costs that may not be integers. Although he knows breadth first search returns the solution with the smallest depth, it takes up too much space, so he decides to try using iterative deepening. As a reminder, in standard depth-first iterative deepening we start by performing a depth first search terminated at a maximum depth of one. If no solution is found, we start over and perform a depth first search to depth two and so on. This way we obtain the shallowest solution, but use only O(bd) space.

But Pacman decides to use a variant of iterative deepening called **iterative deepening A\***, where instead of limiting the depth-first search by depth as in standard iterative deepening search, we can limit the depth-first search by the f value as defined in A\* search. As a reminder f[node] = g[node] + h[node] where g[node] is the cost of the path from the start state and h[node] is a heuristic value estimating the cost to the closest goal state.

In this question, all searches are tree searches and **not** graph searches.

(a) Complete the pseudocode outlining how to perform iterative deepening A\* by choosing the option from the next page that fills in each of these blanks. Iterative deepening A\* should return the solution with the lowest cost when given a consistent heuristic. Note that cutoff is a boolean and new-limit is a number.

function ITERA	TIVE-DEEPENIN	G-Tree-Search( $p$	problem)					
$start-node \leftarrow$	- Make-Node(	INITIAL-STATE[ <i>pro</i>	oblem])					
$limit \leftarrow f[stace]$	ırt-node]							
loop								
$fringe \leftarrow$	$fringe \leftarrow MAKE-STACK(start-node)$							
new-limi	<i>t</i> ←	(i)						
$\textit{cutoff} \leftarrow$		(ii)						
while fri	nge is not empty	do do						
node	$\leftarrow$ Remove-Fr	ONT(fringe)						
<b>if</b> Go	OAL-TEST(proble	em, STATE[node])	then					
r	eturn node							
end i	f							
for c	<i>hild-node</i> in Ex	PAND(STATE[node	], problem) <b>do</b>					
if	$f[child-node] \leq$	≤ limit <b>then</b>						
	$fringe \leftarrow Insi$	ERT( <i>child-node</i> , fri	inge)					
	$new$ - $limit \leftarrow [$	(iii)						
	$cutoff \leftarrow$	(iv)						
e	lse							
	$new$ - $limit \leftarrow [$	(v)						
	cutoff ←	(vi)						
e	nd if							
end f	for							
end whi	le							
<b>if</b> not cu	toff then							
retui	<b>n</b> failure							
end if								
$limit \leftarrow $	(v	rii)						
end loop	ζ.	· /						

$A_1$	-∞	$\mathbf{A_2} \boxed{0}$		A <sub>3</sub>	∞	] A <sub>4</sub>	limit
$B_1$	True	B <sub>2</sub> False		$\mathbf{B}_3$	cutoff	B <sub>4</sub>	not cutoff
$C_1$	new-limit	C <sub>2</sub> new	-limit + 1	C <sub>3</sub>	new- $limit + f[node]$	$C_4$	new-limit + f[child-node]
$C_5$	MIN(new-limit, f[node])	~	(new-limit, ild-node])	C <sub>7</sub>	$\begin{array}{c} \text{MAX}(\textit{new-limit},\\ f[\textit{node}]) \end{array}$	C <sub>8</sub>	MAX(new-limit, f[child-node])
(i)	$\bigcirc A_1$	$\bigcirc A_2$	$\bigcirc A_3$	$\bigcirc \mathbf{A}$	4		
(ii)	$\bigcirc B_1$	$\bigcirc B_2$	$\bigcirc B_3$	$\bigcirc \mathbf{B}$	4		
(iii)		$\bigcirc C_2 \\ \bigcirc C_6$	$\bigcirc C_3 \\ \bigcirc C_7$	$\bigcirc$ C			
(iv)	$\bigcirc B_1$	$\bigcirc B_2$	$\bigcirc B_3$	$\bigcirc \mathbf{B}$	4		
(v)			$\bigcirc C_3 \\ \bigcirc C_7$	$\bigcirc$ C	•		
(vi)	$\bigcirc B_1$	$\bigcirc B_2$	$\bigcirc B_3$	$\bigcirc \mathbf{B}$	4		
(vii)		$\bigcirc C_2 \\ \bigcirc C_6$	$\bigcirc C_3 \\ \bigcirc C_7$	$\bigcirc$ C			

- **(b)** Assuming there are no ties in *f* value between nodes, which of the following statements about the number of nodes that iterative deepening A\* expands is True? If the same node is expanded multiple times, count all of the times that it is expanded. If none of the options are correct, mark None of the above.
  - $\bigcirc$  The number of times that iterative deepening A\* expands a node is greater than or equal to the number of times A\* will expand a node.
  - $\bigcirc$  The number of times that iterative deepening A\* expands a node is less than or equal to the number of times A\* will expand a node.
  - $\bigcirc$  We don't know if the number of times iterative deepening A\* expands a node is more or less than the number of times A\* will expand a node.
  - O None of the above