

# Testing, cont., Equality and Identity

Thanks to Michael Ernst,  
University of Washington

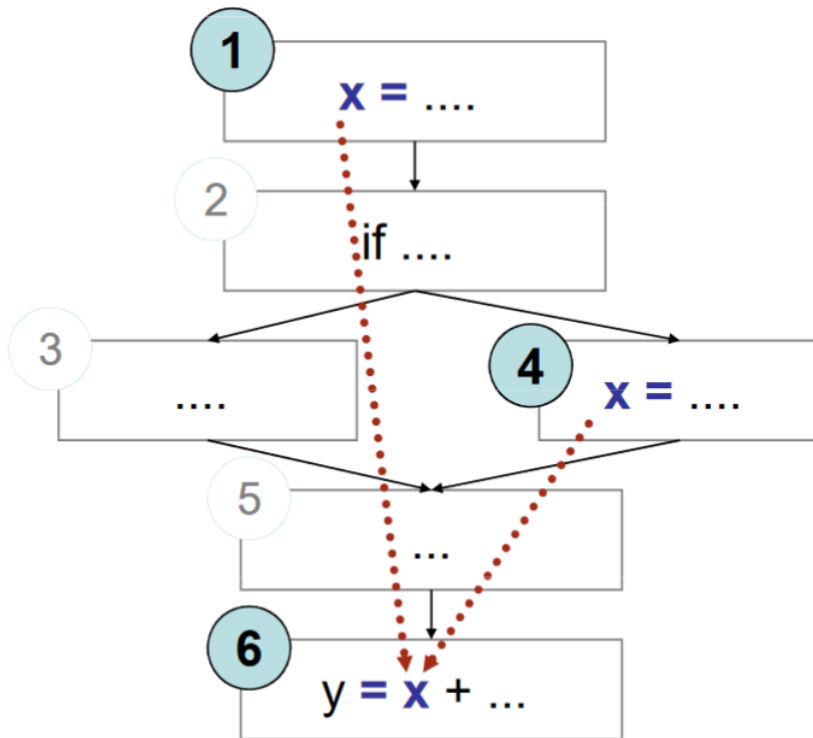
# Outline

- Testing
  - Strategies for choosing tests
    - Black box testing
    - White box testing
    - Definition-usage
- Equality and identity

# Other White Box Heuristics

- White box equivalence partitioning and boundary value analysis
- Loop testing
  - Skip loop
  - Run loop once
  - Run loop twice
  - Run loop with typical value
  - Run loop with max number of iterations
  - Run with boundary values near loop exit condition
- Branch testing
  - Run with values at the boundaries of branch condition

# Difficulties



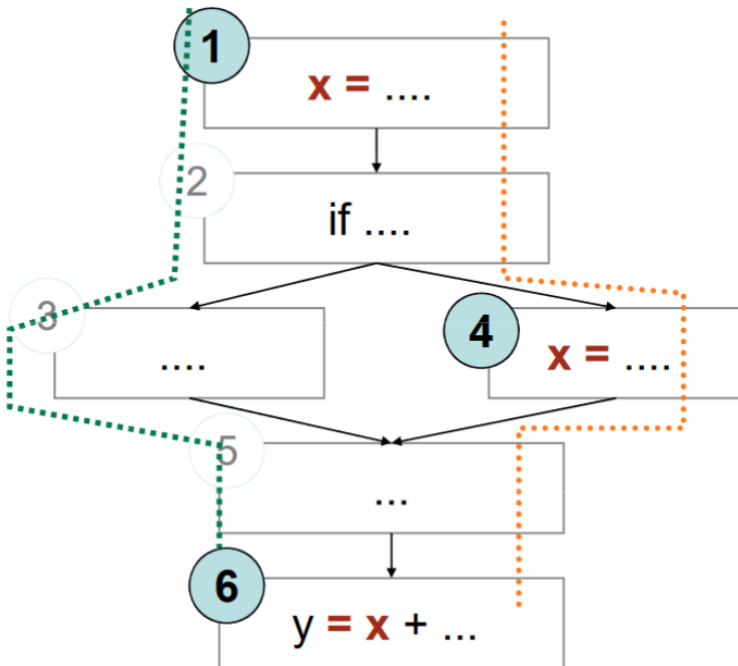
- Value of  $x$  at 6 could be computed at 1 or at 4
- Bad computation at 1 or 4 could be revealed only if they are used at 6
- (1,6) and (4,6) are *def-use (DU) pairs*
  - defs at 1,4
  - use at 6

<http://www.inf.ed.ac.uk/teaching/courses/st/2015-16/Ch13.pdf>

# Definition-use Pairs

- A def-use (DU) pair
  - A pair of a definition and use of a variable such that at least one path exists from the definition to the use
  - `x = 1; // definition`
  - `y = x + 3 // use`
- DU path
  - A path from the definition of a variable to a use of the same variable with no other definition of the variable on the path
  - Loops can create infinite DU paths

# Definition-clear path



- 1,2,3,5,6 is a definition-clear path from 1 to 6
  - x is not re-assigned between 1 and 6
- 1,2,4,5,6 is not a definition-clear path from 1 to 6
  - the value of x is “killed” (reassigned) at node 4
- (1,6) is a DU pair because 1,2,3,5,6 is a definition-clear path

<http://www.inf.ed.ac.uk/teaching/courses/st/2015-16/Ch13.pdf>

# Adequacy

- We want to test:
- All DU pairs
  - Each DU pair tested at least once
- All DU paths
  - Each path is tested at least once
- All definitions
  - For each definition, there is at least one test that exercises a DU path containing it
  - Every computed value is used at least once

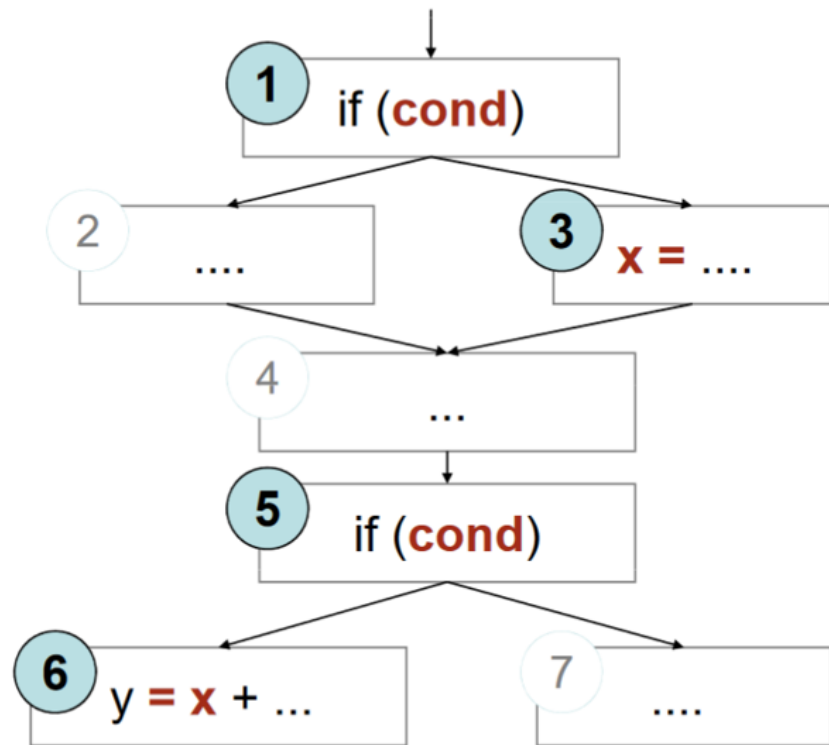
# Difficulties

- `x[i] = some_value; y = x[j];`
  - DU pair only if `i == j`
- `Obj x = new Obj(); x = some_value; y = x;`
  - `y` is an alias of `x`
  - What happens when `x` or `y` is used?
- `m.putFoo(); y = n.getFoo();`
  - Are `m` and `n` the same object?
  - Do `m` and `n` share a `foo`?
- Aliases can be a problem



# Infeasibility

- Suppose cond doesn't change between 1 and 5
  - Or conditions could be different, but 1 implies 5
- (3, 6) is not a **feasible** DU path
- It is very difficult to find infeasible paths
- Infeasible paths are a problem
  - Difficult to find
  - Difficult to test



# Infeasibility

- Detecting infeasibility can be difficult
  - Combination of elements matter
  - No general way to detect infeasible paths
- In practice the goal is **reasonable** coverage
  - Number of paths can be large
  - Doing all DU paths might be impractical
- Problems
  - Aliases
  - Infeasible paths
  - Worst case is bad
    - Exponential number of paths
    - Undecidable properties
  - Be pragmatic

# Outline

- Reference equality
- “Value” equality with **.equals**
- Equality and inheritance
- **equals** and **hashCode**
- Equality and mutation
- Implementing **equals** and **hashCode** efficiently
- Equality in ADTs

# Equality

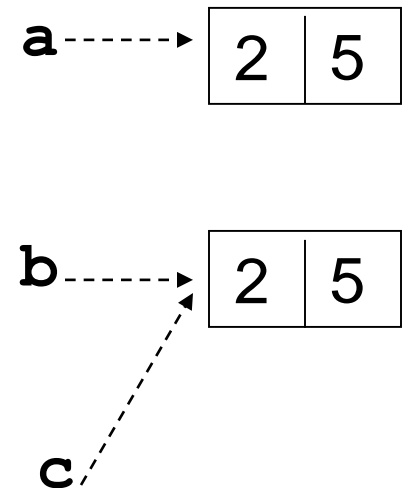
- Simple idea:
  - 2 objects are equal if they have the same value
  - 2 objects are equal if they are the same object
- Many subtleties
  - Same reference, or same value?
  - Same rep or same abstract value?
  - Equality in the presence of inheritance?
  - Does equality hold **just now** or is it **eternal**?
  - How can we implement equality efficiently?

# Equality: `==` and `equals`

- Java uses the reference model for class types

```
class Point {  
    int x; // x-coordinate  
    int y; // y-coordinate  
    Point(int x, int y) {  
        this.x = x;  
        this.y = y;  
    }  
}
```

```
a = new Point(2,5);  
b = new Point(2,5);  
c = b;
```



true or false? `a == b` ?

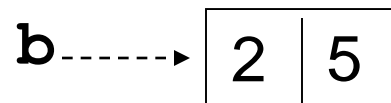
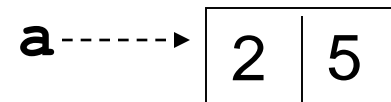
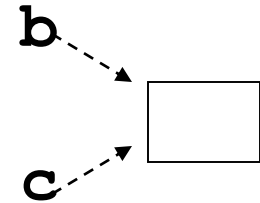
true or false? `b == c` ?

true or false? `a.equals(b)` ?

true or false? `b.equals(c)` ?

# Equality: `==` and `equals`

- In Java, `==` tests for **reference equality**. This is the strongest form of equality
- Often we need a weaker form of equality, **value equality**
- In our **Point** example, we want **a** to be “equal” to **b** because the **a** and **b** objects hold the same value
  - Need to override `Object.equals()`



# Properties of Equality

- Equality is an **equivalence relation**

- **Reflexive**      `a.equals(a)`

- **Symmetric**      `a.equals(b) ⇔ b.equals(a)`

- **Transitive**      `a.equals(b) ∧ b.equals(c) ⇒ a.equals(c)`

- Is reference equality an equivalence relation?

- Yes

# Object.equals method

- **Object.equals** is very simple:
  - Point extends Object
  - all objects extend Object, implicitly

```
public class Object {  
    public boolean equals(Object obj) {  
        return this == obj;  
    }  
}
```



# Object.equals Javadoc spec

Indicates whether some other object is "equal to" this one. The **equals** method implements an equivalence relation:

- It is *reflexive*: for any non-null reference value **x**, **x.equals(x)** should return true.
- It is *symmetric*: for any non-null reference values **x** and **y**, **x.equals(y)** should return true if and only if **y.equals(x)** returns true.
- It is *transitive*: for any non-null reference values **x**, **y**, and **z**, if **x.equals(y)** returns true and **y.equals(z)** returns true, then **x.equals(z)** should return true.
- It is *consistent*: for any non-null reference values **x** and **y**, multiple invocations of **x.equals(y)** consistently return true or consistently return false, provided no information used in equals comparisons on the objects is modified.

# Object.equals Javadoc spec

For any non-null reference value **x**, **x.equals(null)** should return false.

The **equals** method for class Object implements **the most discriminating possible** (i.e., the **strongest**) *equivalence* relation on objects; that is, for any non-null reference values **x** and **y**, this method returns true if and only if **x** and **y** refer to the same object (**x == y** has the value true)...

Parameters:

**obj** - the reference object with which to compare.

Returns:

true if this object is the same as the **obj** argument;  
false otherwise.

See Also:

**hashCode()** , **HashMap**

# The **Object.equals** Spec

- Why this complex specification? Why not just
  - **returns:** true if `obj == this`, false otherwise
- Object is the superclass for all Java classes
  - The specification of **Object.equals** must be as weak (i.e., general) as possible
- Subclasses must be **substitutable** for Object
  - Thus, subclasses need to provide stronger **equals**!
  - No subclass can weaken **equals** and still be **substitutable** for Object!
  - Javadoc spec lists the properties of equality, the weakest possible specification of **equals**

## Adding **equals**

```
public class Duration {  
    private final int min;  
    private final int sec;  
    public Duration(int min, int sec) {  
        this.min = min;  
        this.sec = sec;  
    }  
}  
  
Duration d1 = new Duration(10,5);  
Duration d2 = new Duration(10,5);  
System.out.println(d1.equals(d2)); // prints?
```

## First Attempt to Add **equals**

```
public class Duration {  
    public boolean equals(Duration d) {  
        return  
            this.min == d.min && this.sec == d.sec;  
    }  
}
```

```
Duration d1 = new Duration(10,5);
```

```
Duration d2 = new Duration(10,5);
```

```
System.out.println(d1.equals(d2));
```

 Yields what?

- Is **equals** reflexive, symmetric and transitive?
- This **equals** is not quite correct. Why?

# Overriding vs. Overloading

- Method **overloading** is when two or more methods in the same class have the exact same name but different parameters
  - When overloading, one must change either the type or the number of parameters for a method that belongs to the same class. Overriding means that a method inherited from a parent class will be changed.
- Method **overriding** is when a derived class requires a different definition for an inherited method,
  - The method can be redefined in the derived class.
  - *In overriding* a method, everything remains exactly the same except the method definition – what the method does is changed slightly to fit in with the needs of the child class.
  - the method name, the number and types of parameters, and the return type will all remain the same.
  - Happens at runtime

## What About This?

```
public class Duration {  
    public boolean equals(Duration d) {  
        return  
            this.min == d.min && this.sec == d.sec;  
    }  
}
```

d1's compile-time type is `Object`.  
d1's runtime type is `Duration`.

```
Object d1 = new Duration(10,5);
```

```
Object d2 = new Duration(10,5);
```

```
System.out.println(d1.equals(d2)) ; Yields what?
```

Compiler looks at d1's compile-time type.  
Chooses signature `equals(Object)`.

## A More Correct **equals**

```
@Override
```

```
public boolean equals(Object o) {  
    if (! (o instanceof Duration) )  
        return false;  
    Duration d = (Duration) o;  
    return this.min == d.min && this.sec == d.sec;  
}
```

```
Object d1 = new Duration(10,5);
```

```
Object d2 = new Duration(10,5);
```

```
System.out.println(d1.equals(d2)) ; Yields what?
```



# Outline

- Reference equality
- “Value” equality with **.equals**
- **Equality and inheritance**
- **equals** and **hashCode**
- Equality and mutation
- Implementing **equals** and **hashCode** efficiently
- Equality and ADTs

## Add a Nano-second Field

```
public class NanoDuration extends Duration {  
    private final int nano;  
    public NanoDuration(int min,  
                        int sec,  
                        int nano) {  
        super(min, sec) ; // initializes min&sec  
        this.nano = nano;  
    }  
}
```

- What if we don't add `NanoDuration.equals`?  
(Assume `Duration.equals` as in slide 24)

## First Attempt at `NanoDuration.equals`

```
public boolean equals(Object o) {  
    if (! (o instanceof NanoDuration) )  
        return false;  
    NanoDuration nd = (NanoDuration) o;  
    return super.equals(nd) && nd.nano == nano;  
}
```

`Duration d1 = new NanoDuration(5,10,15);`

`Duration d2 = new Duration(5,10);`

`d1.equals(d2);` Yields what?

`d2.equals(d1);` Yields what?

## Possible Fix for `NanoDuration.equals`

```
public boolean equals(Object o) {  
    if (! (o instanceof Duration) )  
        return false;  
    if (! (o instanceof NanoDuration) )  
        return super.equals(o) ; //compare without nano  
                                   // Is this what we want?  
    NanoDuration nd = (NanoDuration) o;  
    return super.equals(o) && nd.nano == nano;  
}
```

- Does it fix the symmetry bug?
- What can go wrong?

# Possible Fix for **NanoDuration.equals**

```
Duration d1 = new NanoDuration(10,5,15);
```

```
Duration d2 = new Duration(10,5);
```

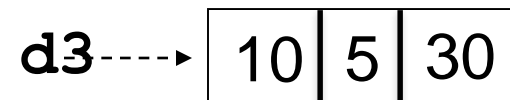
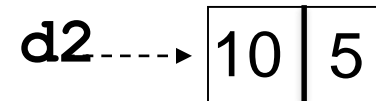
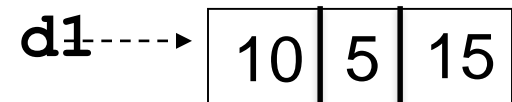
```
Duration d3 = new NanoDuration(10,5,30);
```

`d1.equals(d2)` ; Yields what?

`d2.equals(d3)` ; Yields what?

`d1.equals(d3)` ; Yields what?

**equals** is not transitive!



## One Solution: Checking Exact Class, Instead of **instanceof**

```
class Duration {  
    public boolean equals(Object o) {  
        if (o == null) return false;  
        if ( !o.getClass().equals(getClass()) )  
            return false;  
        Duration d = (Duration) o;  
        return d.min == min && d.sec == sec;  
    }  
}
```

- Problem: every subclass must implement **equals**;  
sometimes, we want to compare distinct classes!

## Another Solution: Composition

```
public class NanoDuration {  
    private final Duration duration;  
    private final int nano;  
    ...  
}
```

Composition does solve the **equals** problem: **Duration** and **NanoDuration** are now unrelated, so we'll never compare a **Duration** to a **NanoDuration**

Problem: Can't use **NanoDuration** instead of **Duration**. Can't reuse code written for **Duration**.

# A Reason to Avoid Subclassing Concrete Classes. More later

- In the JDK, subclassing of concrete classes is rare. When it happens, there are problems
- One example: **Timestamp extends Date**
  - Extends **Date** with a nanosecond value
  - But **Timestamp** spec lists several caveats
    - E.g., **Timestamp.equals(Object)** method is not symmetric with respect to **Date.equals(Object)**
      - (the symmetry problem we saw on the previous slide)



# Abstract Classes

- Prefer subclassing abstract classes
  - “Superclasses” cannot be instantiated
- There is no equality problem if superclass cannot be instantiated!
  - E.g., if **Duration** were abstract, the issue of comparing **Duration** and **NanoDuration** never arises

# Outline

- Reference equality
- “Value” equality with **.equals**
- Equality and inheritance
- **equals** and **hashCode**
- Equality and mutation
- Implementing **equals** and **hashCode** efficiently
- Equality and ADTs

# The **int hashCode** Method

- **hashCode** computes an index for the object (to be used in hashtables)
- Javadoc for **Object.hashCode()** :
  - “Returns a hash code value of the object. This method is supported for the benefit of hashtables such as those provided by **HashMap**.”
  - Self-consistent: **o.hashCode() == o.hashCode()**  
... as long as **o** does not change between the calls
  - Consistent with **equals()** method: **a.equals(b) => a.hashCode() == b.hashCode()**
  - Collections such as **HashMap** calculate *unicity* using **.equals** and **.hashCode**

# The **Object.hashCode** Method

- **Object.hashCode**'s implementation returns a **distinct integer** for each **distinct object**, typically by converting the object's address into an integer
- **hashCode** must be consistent with equality
  - **equals** and **hashCode** are used in hashtables
  - If **hashCode** is inconsistent with **equals**, the hashtable behaves incorrectly
  - Rule: if you override **equals**, override **hashCode**; must be consistent with **equals**

# Implementations of **hashCode**

Remember, we defined `Duration.equals(Object)`

```
public class Duration {
```

Choice 1: don't override, inherit **hashCode** from Object

Choice 2: `public int hashCode() { return 1; }`

Choice 3: `public int hashCode() { return min; }`

Choice 4: `public int hashCode() { return min+sec; }`  
`}`

## **hashCode** Must Be Consistent with **equals**

- Suppose we change **Duration.equals**

// Returns true if **o** and **this** represent the same number of  
// seconds

```
public boolean equals(Object o) {  
    if (!(o instanceof Duration)) return false;  
    Duration d = (Duration) o;  
    return 60*min+sec == 60*d.min+d.sec;  
}
```

- Will **min+sec** for **hashCode** still work?

# Outline of today's class

- Reference equality
- “Value” equality with **.equals**
- Equality and inheritance
- **equals** and **hashCode**
- Equality and mutation
- Implementing **equals** and **hashCode** efficiently
- Equality and ADTs

# Equality, Mutation and Time

- If two objects are equal **now**, will they **always** be equal?
  - In mathematics, the answer is “yes”
    - Given that the object is not a function of time
  - In Java, the answer is “you chose”
  - The Object spec does not specify this
- For immutable objects
  - Abstract value never changes, equality is **eternal**
- For mutable objects
  - We can either compare abstract values **now**, or
  - be **eternal** (can't have both since value can change)



# StringBuffer Example

- StringBuffer is mutable, and takes the **eternal** approach

```
StringBuffer s1 = new StringBuffer("hello");
```

```
StringBuffer s2 = new StringBuffer("hello");
```

```
System.out.println(s1.equals(s1)); // true
```

```
System.out.println(s1.equals(s2)); // false
```

- **equals** is just reference equality (==). This is the only way to ensure eternal equality for mutable objects

# Date Example

- **Date** is mutable, and takes the “compare values now” approach

```
Date d1 = new Date(0) ; //Jan 1, 1970 00:00:00 GMT
Date d2 = new Date(0) ;
System.out.println(d1.equals(d2)) ; // true
d2.setTime(10000) ; //some time later
System.out.println(d1.equals(d2)) ; // false
```

# Behavioral and Observational Equivalence

- Two objects are “**behaviorally equivalent**” if there is no sequence of operations that can distinguish them
  - This is “eternal” equality
  - Two Strings with same content are behaviorally equivalent, two Dates or StringBuffers with same content are not
- Two objects are “**observationally equivalent**” if there is no sequence of observer operations that can distinguish them
  - We are excluding mutators
  - Excluding ==
  - Two Strings, Dates, or StringBuffers with same content are observationally equivalent.

# Equality and Mutation

- Date class implements observational equality
- We can **violate the rep invariant** of a Set container (rep invariant: there are no duplicates in set) by **mutating after insertion**

```
Set<Date> s = new HashSet<Date>() ;
Date d1 = new Date(0) ;
Date d2 = new Date(1) ;
s.add(d1) ;
s.add(d2) ;
d2.setTime(0) ; // mutation after d2 already in the Set!
for (Date d : s) { // prints 2 identical dates
    System.out.println(d) ;
}
```

# Equality and Mutation

- Be very careful with elements of Sets
- Ideally, elements should be immutable objects, because immutable objects guarantee behavioral equivalence
- Java spec for Sets warns about using mutable objects as set elements
- Same problem applies to [keys in maps](#)

# Equality and Mutation

- Sets assume hash codes don't change

```
Set<Date> s = new HashSet<Date>();  
Date d1 = new Date(0);  
Date d2 = new Date(1000); // later  
s.add(d1);  
s.add(d2);  
d2.setTime(10000);  
s.contains(d2); // false  
s.contains(new Date(10000)); // false  
s.contains(new Date(1000)); // false again
```

# Equality and Mutation

- Redefining **equals** and **hashCode** makes most sense for immutable, “value”, objects
  - E.g., String, RatNum
- Be careful with **equals** and **hashCode** on mutable objects
  - From spec of Object.equals: It is *consistent*: for any non-null reference values **x** and **y**, multiple invocations of **x.equals(y)** consistently return true or consistently return false, provided no information used in equals comparisons on the objects is modified.

# Equality and Mutation

- From JavaDoc
  - Note: Great care must be exercised if mutable objects are used as set elements. **The behavior of a set is not specified if the value of an object is changed in a manner that affects equals comparisons while the object is an element in the set.** A special case of this prohibition is that it is not permissible for a set to contain itself as an element.
- HashSet.contains() uses hashCode()
- HashSet.contains() method relies on hash values to stay immutable
  - There is an assumption that the hashCode() does not change
- contains() computes the hashCode() of the object it is looking for
  - It searches only the *bucket* that contains the hash value
- The moral
  - If you put mutable objects in a Set, don't modify them and expect operations like contains() to work as expected.



# Mutation and hash codes

- Sets assume that the hash codes don't change
- Mutation can break this assumption

```
List<String> friends =  
    new LinkedList<String>(Arrays.asList("yoda", "zaphod"));  
List<String> enemies =  
    new LinkedList<String>(Arrays.asList("Darth Vader", "Joker"));  
  
Set<List<String>> h = new HashSet<List<String>>();  
h.add(friends);  
h.add(enemies);  
friends.add("Batman");  
  
System.out.println(h.contains(friends)); // probably false  
System.out.println();  
for (List<String> lst : h) {  
    System.out.println(lst.equals(friends));  
} // one "true" will be printed - inconsistent
```

# Implementing **equals** Efficiently

- **equals** can be expensive!
- How can we speed-up **equals**?

```
public boolean equals(Object o) {  
    if (this == o) return true;  
    // class-specific prefiltering (e.g.,  
    // compare file size if working with files)  
    // Lastly, compare fields (can be expensive)  
}
```

## Example: A Naive **RatPoly.equals**

```
public boolean equals(Object o) {
    if (o instanceof RatPoly) {
        RatPoly rp = (RatPoly) o;
        int i=0;
        while (i<Math.min(rp.c.length,c.length)) {
            if (rp.c[i] != c[i]) // Assume int arrays
                return false;
            i = i+1;
        }
        if (i != rp.c.length || i != c.length) return false;
        return true;
    }
    else
        return false;
}
```

## Example: Better **equals**

```
public boolean equals(Object o) {  
    if (o instanceof RatPoly) {  
        RatPoly rp = (RatPoly) o;  
        if (rp.c.length != c.length)  
            return false; // prefiltering  
        for (int i=0; i < c.length; i++) {  
            if (rp.c[i] != c[i])  
                return false;  
        }  
        return true;  
    }  
    else  
        return false;  
}
```

# Implementing **hashCode**

// returns: the **hashCode** value of this String

```
public int hashCode() {  
    int h = this.hash; // rep. field hash  
    if (h == 0) {      // caches the hashCode  
        char[] val = value;  
        int len = count;  
        for (int i = 0; i < len; i++) {  
            h = 31*h + val[i];  
        }  
        this.hash = h;  
    }  
    return h;  
}
```

This works only for immutable objects!

# Outline of today's class

- Reference equality
- “Value” equality with **.equals**
- Equality and inheritance
- **equals** and **hashCode**
- Equality and mutation
- Implementing **equals** and **hashCode** efficiently
- Equality and ADTs

# Rep Invariant, AF and Equality

- With ADTs we compare abstract values, not rep
- Usually, many valid reps map to the same abstract value
  - If Concrete Object (rep) and Concrete Object' (rep') map to the same Abstract Value, then Concrete Object and Concrete Object' must be **equal**
- A stronger rep invariant shrinks the domain of the AF and simplifies **equals**

## Example: Line Segment

```
class LineSegment {  
  // Rep invariant:  
  // !(x1=x2 && y1=y2)  
  float x1,y1;  
  float x2,y2;  
  ...  
}  
// equals must  
// return true for  
// {x1:1,y1:2,x2:4,y2:5}  
// and {4,5,1,2}
```

```
class LineSegment {  
  // Rep invariant:  
  // x1<x2 ||  
  // x1=x2 && y1<y2  
  float x1,y1;  
  float x2,y2;  
  ...  
}  
// equals is simpler:  
// {4,5,1,2} is not  
// valid rep anymore
```



# Rules for overriding equals()

- Overriding equality seems easy but many ways to get it wrong
- Obey the general contract
- Don't do it if
  - Each instance of the class is inherently unique.
  - You don't care whether the class provides a “logical equality” test
    - Random numbers
  - A superclass has already overridden equals, and the behavior inherited from the superclass is adequate for this class.
    - Set inherits its equals from AbstractSet
  - The class is private or package-private, and you are certain that its equals method will never be invoked.

# Rules for overriding equals()

- If you need to:
  - Use the == operator to check if the argument is a reference to this object
  - Use the instanceof operator to check if the argument is of the correct type
  - Cast the argument to the correct type
  - For each “significant” field in the class, check to see if that field of the argument matches the corresponding field of this object.
  - When you are finished writing your equals method, ask yourself three questions: Is it symmetric, is it transitive, and is it consistent?
  - Always override hashCode when you override equals
  - Don’t substitute another type for Object in the equals declaration.
  - Eclipse can generate Java hashCode and equals methods
    - Source->Generate hashCode() and equals()’.