# Homework 1. Fixpoints and grammar filters

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## Introduction

You are a reader for Computer Science 181, which asks students to submit grammars that solve various problems. However, many of the submitted grammars are trivially wrong, in several ways. Here is one. Some grammars contain unreachable rules, that is, rules that can never be reached from the start symbol by applying zero or more rules. Unreachable rules do not affect the language or parse trees generated by a grammar, so in some sense they don't make the answers wrong, but they're noise and they make grading harder. You'd like to filter out the noise, and just grade the useful parts of each grammar.

You've heard that OCaml is a good language for writing compilers and whatnot, so you decide to give it a try for this application. While you're at it, you have a background in <u>fixed</u> <u>point</u> and <u>periodic point</u> theory, so you decide to give it a try too.

## **Definitions**

### fixed point

(of a function f) A point x such that f(x) = x. In this description we are using OCaml notation, in which functions always have one argument and parentheses are not needed around arguments.

### computed fixed point

(of a function f with respect to an initial point x) A fixed point of f computed by calculating x, f x, f (f x), f (f (f x)), etc., stopping when a fixed point is found for f. If no fixed point is ever found by this procedure, the computed fixed point is not defined for f and x.

### periodic point

(of a function f with period p) A point x such that f(f(x)) = x, where there are p occurrences of f in the call. That is, a periodic point is like a fixed point, except the function returns to the point after p iterations instead of 1 iteration. Every point is a periodic point for p=0. A fixed point is a periodic point for p=1.

### computed periodic point

(of a function f with respect to a period p and an initial point x) A periodic point of f with period p, computed by calculating x, f x, f (f x), f (f (f x)), etc., stopping when a periodic point with period p is found for f. The computed periodic point need

not be equal to x. If no periodic point is ever found by this procedure, the computed periodic point is not defined for f, p, and x.

#### symbol

A symbol used in a grammar. It can be either a nonterminal symbol or a terminal symbol; each kind of symbol has a value, whose type is arbitrary. A symbol has the following OCaml type:

#### right hand side

A list of symbols. It corresponds to the right hand side of a single grammar rule. A right hand side can be empty.

#### rule

A pair, consisting of (1) a nonterminal value (the left hand side of the grammar rule) and (2) a right hand side.

#### grammar

A pair, consisting of a start symbol and a list of rules. The start symbol is a nonterminal value.

# **Assignment**

Let's warm up by modeling sets using OCaml lists. The empty list represents the empty set, and if the list t represents the set t, then the list t represents the set t. Although sets by definition do not contain duplicates, the lists that represent sets can contain duplicates. Another set of warmup exercises will compute fixed points. Finally, you can write a function that filters unreachable rules.

- 1. Write a function subset a b that returns true iff  $a \subseteq b$ , i.e., if the set represented by the list a is a subset of the set represented by the list b. Every set is a subset of itself. This function should be generic to lists of any type: that is, the type of subset should be a generalization of 'a list -> 'a list -> bool.
- 2. Write a function equal\_sets a b that returns true iff the represented sets are equal.
- 3. Write a function set\_union a b that returns a list representing a∪b.
- 4. Write a function set\_intersection a b that returns a list representing a∩b.
- 5. Write a function  $set\_diff$  a b that returns a list representing a-b, that is, the set of all members of a that are not also members of b.
- 6. Write a function computed\_fixed\_point eq f x that returns the computed fixed point for f with respect to x, assuming that eq is the equality predicate for f's domain. A common case is that eq will be (=), that is, the builtin equality predicate of OCaml; but any predicate can be used. If there is no computed fixed point, your implementation can do whatever it wants: for example, it can print a diagnostic, or go into a loop, or send nasty email messages to the user's relatives.

- 7. OK, now for the real work. Write a function filter\_reachable g that returns a copy of the grammar g with all unreachable rules removed. This function should preserve the order of rules: that is, all rules that are returned should be in the same order as the rules in g.
- 8. Supply at least one test case for each of the above functions in the style shown in the sample test cases below. When testing the function F call the test cases my\_F\_test0, my\_F\_test1, etc. For example, for subset your first test case should be called my\_subset\_test0. Your test cases should exercise all the above functions, even though the sample test cases do not.

#### Your code should follow these guidelines:

- 1. Your code may use the <u>Pervasives</u> and <u>List</u> modules, but it should use no other modules other than your own code.
- 2. It is OK (and indeed encouraged) for your solutions to be based on one another; for example, it is fine for filter\_reachable to use equal\_sets and computed fixed point.
- 3. Your code should prefer pattern matching to conditionals when pattern matching is natural.
- 4. Your code should be free of <u>side effects</u> such as loops, assignment, input/output, incr, and decr. Use recursion instead of loops.
- 5. Simplicity is more important than efficiency, but your code should avoid using unnecessary time and space when it is easy to do so. For example, instead of repeating a expression, compute its value once and reuse the computed value.
- 6. The test cases below should work with your program. You are unlikely to get credit for it otherwise.

Assess your work by writing a brief after-action report that summarizes why you solved the problem the way you did, other approaches that you considered and rejected (and why you rejected them), and any weaknesses in your solution in the context of its intended application. This report should be a <u>plain text</u> file that is no more than 2000 bytes long. See <u>Resources for oral presentations and written reports</u> for advice on how to write assessments; admittedly much of the advice there is overkill for the simple kind of report we're looking for here.

## **Submit**

Submit three files via CourseWeb. The file hw1.ml should implement the abovementioned functions, along with any auxiliary types and functions; in particular, it should define the symbol type as shown above. The file hw1test.ml should contain your test cases. The file hw1.txt should hold your assessment. Please do not put your name, student ID, or other personally identifying information in your files.

## Sample test cases

See <u>hw1sample.ml</u> for a copy of these tests.

```
let subset test0 = subset [] [1;2;3]
let subset test1 = subset [3;1;3] [1;2;3]
let subset_test2 = \underline{not} (subset [1;3;7] [4;1;3])
let equal_sets_test0 = equal_sets [1;3] [3;1;3]
let equal sets test1 = not (equal sets [1;3;4] [3;1;3])
let set union test0 = equal_sets (set_union [] [1;2;3]) [1;2;3]
let set union test1 = equal sets (set union [3;1;3] [1;2;3]) [1;2;3]
let set union test2 = equal sets (set union [] []) []
let set intersection test0 =
  equal sets (set intersection [] [1;2;3]) []
let set intersection test1 =
  equal sets (set intersection [3;1;3] [1;2;3]) [1;3]
let set intersection test2 =
  equal sets (set intersection [1;2;3;4] [3;1;2;4]) [4;3;2;1]
let set diff test0 = equal sets (set diff [1;3] [1;4;3;1]) []
let set diff test1 = equal sets (set diff [4;3;1;1;3] [1;3]) [4]
let set diff test2 = equal sets (set diff [4;3;1] []) [1;3;4]
let set diff test3 = equal sets (set_diff [] [4;3;1]) []
let computed fixed point test0 =
  computed fixed point (=) (fun x \rightarrow x \angle 2) 1000000000 = 0
let computed fixed point test1 =
  computed fixed point (=) (fun x -> x \star. 2.) 1. = infinity
let computed fixed point test2 =
  computed fixed point (=) sqrt 10. = 1.
let computed fixed point test3 =
  ((computed_fixed_point (fun x y \rightarrow abs_float (x \rightarrow y) < 1.)
                          (fun x -> x /. 2.)
                          10.)
   = 1.25)
(* An example grammar for a small subset of Awk. *)
type awksub nonterminals =
  | Expr | Lvalue | Incrop | Binop | Num
let awksub rules =
   [Expr, [T"("; N Expr; T")"];
    Expr, [N Num];
    Expr, [N Expr; N Binop; N Expr];
    Expr, [N Lvalue];
    Expr, [N Incrop; N Lvalue];
    Expr, [N Lvalue; N Incrop];
    Lvalue, [T"$"; N Expr];
    Incrop, [T"++"];
    Incrop, [T"--"];
    Binop, [T"+"];
    Binop, [T"-"];
```

```
Num, [T"0"];
    Num, [T"1"];
    Num, [T"2"];
    Num, [T"3"];
    Num, [T"4"];
    Num, [T"5"];
    Num, [T"6"];
    Num, [T"7"];
    Num, [T"8"];
    Num, [T"9"]]
let awksub grammar = Expr, awksub rules
let awksub test0 =
  filter reachable awksub grammar = awksub grammar
let awksub test1 =
  filter reachable (Expr, <u>List.tl</u> awksub rules) = (Expr, List.tl awksub rules)
let awksub test2 =
  filter_reachable (Lvalue, awksub_rules) = (Lvalue, awksub_rules)
let awksub test3 =
  filter reachable (Expr, List.tl (List.tl awksub rules)) =
    (Expr,
     [Expr, [N Expr; N Binop; N Expr];
      Expr, [N Lvalue];
      Expr, [N Incrop; N Lvalue];
      Expr, [N Lvalue; N Incrop];
      Lvalue, [T "$"; N Expr];
      Incrop, [T "++"];
      Incrop, [T "--"];
      Binop, [T "+"];
      Binop, [T "-"]])
let awksub test4 =
  filter reachable (Expr, List.tl (List.tl awksub rules))) =
    (Expr,
     [Expr, [N Lvalue];
      Expr, [N Incrop; N Lvalue];
      Expr, [N Lvalue; N Incrop];
      Lvalue, [T "$"; N Expr];
      Incrop, [T "++"];
      Incrop, [T "--"]])
type giant nonterminals =
  | Conversation | Sentence | Grunt | Snore | Shout | Quiet
let giant grammar =
 Conversation,
  [Snore, [T"ZZZ"];
  Quiet, [];
   Grunt, [T"khrgh"];
   Shout, [T"aooogah!"];
```

```
Sentence, [N Quiet];
Sentence, [N Grunt];
Sentence, [N Shout];
Conversation, [N Snore];
Conversation, [N Sentence; T","; N Conversation]]

let giant_test0 =
   filter_reachable giant_grammar = giant_grammar

let giant_test1 =
   filter_reachable (Sentence, List.tl (snd giant_grammar)) =
        (Sentence,
        [Quiet, []; Grunt, [T "khrgh"]; Shout, [T "aooogah!"];
        Sentence, [N Quiet]; Sentence, [N Grunt]; Sentence, [N Shout]])

let giant_test2 =
   filter_reachable (Quiet, snd giant_grammar) = (Quiet, [Quiet, []])
```

# Sample use of test cases

When testing on SEASnet, use one of the machines lnxsrv06.seas.ucla.edu, lnxsrv07.seas.ucla.edu, lnxsrv09.seas.ucla.edu, and lnxsrv10.seas.ucla.edu. Make sure /usr/local/cs/bin is at the start of your path, so that you get the proper version of OCaml. To do this, append the following lines to your \$HOME/.profile file if you use bash or ksh:

```
export PATH=/usr/local/cs/bin:$PATH

or the following line to your $HOME/.login file if you use tcsh or csh:

set path=(/usr/local/cs/bin $path)
```

The command ocaml should output the version number 4.07.1.

If you put the <u>sample test cases</u> into a file hwlsample.ml, you should be able to use it as follows to test your hwl.ml solution on the SEASnet implementation of OCaml. Similarly, the command #use "hwltest.ml";; should run your own test cases on your solution.

```
val set union test0 : bool = true
val set_union_test1 : bool = true
val set_union_test2 : bool = true
val set_intersection_test0 : bool = true
val set_intersection_test1 : bool = true
val set_intersection_test2 : bool = true
val computed_fixed_point_test0 : bool = true
val computed fixed point test1 : bool = true
val computed fixed point test2 : bool = true
val computed_fixed_point_test3 : bool = true
type awksub_nonterminals = Expr | Lvalue | Incrop | Binop | Num
val awksub rules :
  (awksub nonterminals * (awksub nonterminals, string) symbol list) list =
  [(Expr, [T "("; N Expr; T ")"]); (Expr, [N Num]);
   (Expr, [N Expr; N Binop; N Expr]); (Expr, [N Lvalue]);
   (Expr, [N Incrop; N Lvalue]); (Expr, [N Lvalue; N Incrop]);
   (Lvalue, [T "$"; N Expr]); (Incrop, [T "++"]); (Incrop, [T "--"]);
   (Binop, [T "+"]); (Binop, [T "-"]); (Num, [T "0"]); (Num, [T "1"]);
   (Num, [T "2"]); (Num, [T "3"]); (Num, [T "4"]); (Num, [T "5"]);
   (Num, [T "6"]); (Num, [T "7"]); (Num, [T "8"]); (Num, [T "9"])]
val awksub_grammar :
  awksub_nonterminals *
  (awksub nonterminals * (awksub nonterminals, string) symbol list) list =
  (Expr,
   [(Expr, [T "("; N Expr; T ")"]); (Expr, [N Num]);
    (Expr, [N Expr; N Binop; N Expr]); (Expr, [N Lvalue]);
    (Expr, [N Incrop; N Lvalue]); (Expr, [N Lvalue; N Incrop]);
    (Lvalue, [T "$"; N Expr]); (Incrop, [T "++"]); (Incrop, [T "--"]);
    (Binop, [T "+"]); (Binop, [T "-"]); (Num, [T "0"]); (Num, [T "1"]);
    (Num, [T "2"]); (Num, [T "3"]); (Num, [T "4"]); (Num, [T "5"]);
    (Num, [T "6"]); (Num, [T "7"]); (Num, [T "8"]); (Num, [T "9"])])
val awksub test0 : bool = true
val awksub test1 : bool = true
val awksub_test2 : bool = true
val awksub_test3 : bool = true
val awksub_test4 : bool = true
type giant nonterminals =
    Conversation
    Sentence
    Grunt
    Snore
    Shout
   Quiet
val giant grammar :
  giant_nonterminals *
  (giant nonterminals * (giant nonterminals, string) symbol list) list =
  (Conversation,
   [(Snore, [T "ZZZ"]); (Quiet, []); (Grunt, [T "khrgh"]);
    (Shout, [T "aooogah!"]); (Sentence, [N Quiet]); (Sentence, [N Grunt]);
    (Sentence, [N Shout]); (Conversation, [N Snore]);
    (Conversation, [N Sentence; T ","; N Conversation])])
val giant test0 : bool = true
val giant test1 : bool = true
```

```
val giant_test2 : bool = true
#
```

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