

Taylor Rembos  
EEL 3135  
Lab 3 Part 2

### Lab 3: Music Synthesis with Sinusoidal Signals

#### Lab Part Two

#### 2.1 Construction of the Bach Fugue

**'Bach\_fugue\_3voices.wav' file**

The MATLAB data file `bach_fugue.mat` is of the same structure as `barukh_fugue.mat`, also containing a `theVoices` array of structures. Add the three voices from the `theVoices` in `bach_fugue.mat`, together to [produce the Bach Fugue](#). Have your TA [check this off](#). (Alternately, if you can't finish this in time, submit as a `.wav` file on Canvas.)

##### **function playsong2.m**

```
function song = playSong(theVoices)
% PLAYSONG Produce a sinusoidal waveform containing the combination
of the different notes in theVoices
% usage: song = playSong ( )
% song = the output sinusoidal waveform
load('bach_fugue.mat')
fs = 8000;
spp = 0.25 %%% seconds per pulse, theVoices is measured in pulses with
4 pulses per beat

% Create a vector of zeros with length equal to the total number
of samples in the entire song
song =
zeros(1,4*spp*fs*(theVoices(3).durations(length(theVoices(3).durations)
) + (theVoices(3).startPulses(length(theVoices(3).durations))))); %%%
vector of zeros

% Then add in the notes
for i = 1:length(theVoices) % Cycle through each set of notes
    % Convert data arrays to appropriate units
    for j = 1:length(theVoices(i).noteNumbers) % Cycle through each
note in aset
        keynum = theVoices(i).noteNumbers(j);
        note = key2note(1,keynum,theVoices(i).durations(j).*spp);
%%% create sinusoid of correct length to represent a single note
        locstart = theVoices(i).startPulses(j)*(fs/4)+1; %%% index
of where note starts
        locend = locstart + length(note) - 1; %%%
        % index of where note ends
        song(locstart:locend) = song(locstart:locend) + note;
    end
end
song = song/(max(abs(song))); % anti clipping xx
soundsc(song,fs);
audiowrite('Bach_fugue_3voices.wav',song,fs);
% Use audiowrite() to generate WAV file
end
```

## 2.2 Musical Tweaks - Enveloping

'bach\_envelope.wav' file

Your job here is to [improve the sound quality](#).

Hint 1: The function `interp1()` may be useful in this section.

Hint 2: You'll want to make sure that your note and E are the same length.

Hint 3: Previous generations of students have found the Hanning Window to be an effective envelope.

[Implement an envelope to improve the sound of your Bach Fugue](#). Save it as *bach\_envelope.wav* and submit it on Canvas.

### script key2noteReal.m

```
function xx = key2noteReal(X, keynum, dur)
    % KEY2NOTE Produce a sinusoidal waveform corresponding to a given
    piano key number
    % usage: xx = key2note (X, keynum, dur)
    % xx = the output sinusoidal waveform
    % X = complex amplitude for the sinusoid, X = A*exp(j*phi).
    % keynum = the piano keyboard number of the desired note
    % dur = the duration (in seconds) of the output note
    % Hint 1: The function interp1() may be useful in this section.?
    % Hint 2: You'll want to make sure that your note and E are the same
    length.
    % Hint 3: Previous generations of students have found the Hanning
    Window to be an effective envelope.

    fs = 8000;
    tt = (1/fs):(1/fs):dur;
    freq = 440*(2^((keynum-49)/12));
    a = 50;
    b = 20;
    c = 1.4285;
    e = interp1([0,dur/a,dur/b,dur/c,dur], [0,1,0.8,0.02,0], tt, 'spline');
    % interp1 interpolation interp1(X,V,Xq), X vector (X=N), V vector
    (length
    % N), Xq array of size M
    % interpolates to find Vq, the values of the underlying function V=F(X)
    at
    % query points Xq
    xx = e.*real(X*exp(j*2*pi*freq*tt));
```

### function playSong2.m

```
function song = playSong(theVoices)
    % PLAYSONG Produce a sinusoidal waveform containing the combination
    of the different notes in theVoices
    % usage: song = playSong ()
    % song = the output sinusoidal waveform
    load('bach_fugue.mat')
    fs = 8000;
    spp = 0.25 %%% seconds per pulse, theVoices is measured in pulses with
    4 pulses per beat
```

```

% Create a vector of zeros with length equal to the total number
ofsamples in the entire song
song =
zeros(1,4*spp*fs*(theVoices(3).durations(length(theVoices(3).durations)
) + (theVoices(3).startPulses(length(theVoices(3).durations))))); %%%
vector of zeros

% Then add in the notes
for i = 1:length(theVoices) % Cycle through each set of notes
    % Convert data arrays to appropriate units
    for j = 1:length(theVoices(i).noteNumbers) % Cycle through each
note in aset
        keynum = theVoices(i).noteNumbers(j);
        note =
key2noteReal(1,keynum,theVoices(i).durations(j).*spp); %%% create
sinusoid of correct length to represent a single note
        locstart = theVoices(i).startPulses(j)*(fs/4)+1; %%% index
of where note starts
        locend = locstart + length(note) - 1; %%%
        % index of where note ends
        song(locstart:locend) = song(locstart:locend) + note;
    end
end
song = song/(max (abs (song))); %% anti clipping xx
soundsc(song,fs);
audiowrite('Bach_envelope.wav',song,fs);
% Use audiowrite() to generate WAV file
end

```

### 2.3 Musical Tweaks – Fourier Series of a Trumpet

Suppose the maximum frequency in the Bach Fugue is 1200 Hz. What is the minimum sampling frequency needed to synthesize, without aliasing, a trumpet sound containing nine harmonics?

$$2 \times 1200 \text{ Hz} = 2400 \text{ Hz}$$

Using a sampling frequency of 44100 Hz, construct your Bach Fugue in trumpet. Submit this as a .wav file on Canvas.

**'bach\_trumpet.wav' file**

#### script key2noteReal.m

```
function xx = key2noteReal(X, keynum, dur)
    % KEY2NOTE Produce a sinusoidal waveform corresponding to a given
    piano key number
    % usage: xx = key2note (X, keynum, dur)
    % xx = the output sinusoidal waveform
    % X = complex amplitude for the sinusoid, X = A*exp(j*phi).
    % keynum = the piano keyboard number of the desired note
    % dur = the duration (in seconds) of the output note
    % Hint 1: The function interp1() may be useful in this section.?
    % Hint 2: You'll want to make sure that your note and E are the same
    length.
    % Hint 3: Previous generations of students have found the Hanning
    Window to be an effective envelope.

    fs = 44100;
    tt = (1/fs):(1/fs):dur;
    freq = 440*(2^((keynum-49)/12));
    a = 50;
    b = 20;
    c = 10/7;
    e = interp1([0,dur/a,dur/b,dur/c,dur], [0,1,0.8,0.02,0], tt, 'spline');
    % interp1 interpolation interp1(X,V,Xq), X vector (X=N), V vector
    (length
    % N), Xq array of size M
    % interpolates to find Vq, the values of the underlying function V=F(X)
    at
    % query points Xq
    % s = spline( x , y , xq ) returns a vector of interpolated values s
    corresponding to the query points in xq
    har1 = 0.1155*real(X*exp(j*1*2*pi*freq*tt)*exp(j*(-2.199)));
    har2 = 0.3417*real(X*exp(j*2*2*pi*freq*tt)*exp(j*1.6727));
    har3 = 0.1789*real(X*exp(j*3*2*pi*freq*tt)*exp(j*(-2.5454)));
    har4 = 0.1232*real(X*exp(j*4*2*pi*freq*tt)*exp(j*0.6607));
    har5 = 0.0678*real(X*exp(j*5*2*pi*freq*tt)*exp(j*(-2.0390)));
    har6 = 0.0473*real(X*exp(j*6*2*pi*freq*tt)*exp(j*2.1597));
    har7 = 0.0260*real(X*exp(j*7*2*pi*freq*tt)*exp(j*(-1.0467)));
    har8 = 0.0045*real(X*exp(j*8*2*pi*freq*tt)*exp(j*1.8581));
    har9 = 0.0020*real(X*exp(j*9*2*pi*freq*tt)*exp(j*(-2.3925)));
    xx = e.*(har1+har2+har3+har4+har5+har6+har7+har8+har9);
```

### **function playSong2.m**

```
function song = playSong(theVoices)
% PLAYSONG Produce a sinusoidal waveform containing the combination
of the different notes in theVoices
% usage: song = playSong ()
% song = the output sinusoidal waveform
load('bach_fugue.mat')
fs = 44100;
spp = 0.25 %%% seconds per pulse, theVoices is measured in pulses with
4 pulses per beat

% Create a vector of zeros with length equal to the total number
of samples in the entire song
song =
zeros(1,4*spp*fs*(theVoices(3).durations(length(theVoices(3).durations)
) + (theVoices(3).startPulses(length(theVoices(3).durations))))); %%%
vector of zeros

% Then add in the notes
for i = 1:length(theVoices) % Cycle through each set of notes
    % Convert data arrays to appropriate units
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note in aset
        keynum = theVoices(i).noteNumbers(j);
        note =
key2noteReal(1,keynum,theVoices(i).durations(j).*spp); %%% create
sinusoid of correct length to represent a single note
        locstart = theVoices(i).startPulses(j)*(fs/4)+1; %%% index
of where note starts
        locend = locstart + length(note) - 1; %%%
        % index of where note ends
        song(locstart:locend) = song(locstart:locend) + note;
    end
end
    song = song/(max(abs(song))); %% anti clipping xx
    soundsc(song,fs);
    audiowrite('Bach_trumpet.wav',song,fs);
% Use audiowrite() to generate WAV file
end
```

***Extra Credit is coming...***