Duke University Human Capital / Synthetic Data Project Server Performance Comparison 1/24/2018, T. Balmat

## BACKGROUND

In December of 2016, while testing new servers pap36 and pap46 before being placed into service, it was observed that certain R scripts that had been in use required longer to complete on pap46 than on pap1 (pap46 is intended to replace pap1). Table 1 lists completion times of select algorithms executed 12/4/2017 on pap1 and pap46 using randomly generated data sets of varying size that resemble authentic data used in research. Figure 1 plots completion times by number of observations in a data set. Since December, various execution time comparisons have been made between pap1, pap2, pap36, and pap46 with concentration on pap1 and pap46, since long periods of dedicated access are possible with these. In general, identical algorithms with similar data sets have tended to complete more quickly on pap1 than on pap46. Pap36 is intended to replace pap2 and is shared concurrently by researches and an active SQL Server instance. It is important to note that aspects of current research to be published, particularly with the Synthetic Data Project, compare and report computational efficiency of various algorithms, making consistency of results important.

Table 1: Comparison of pap1 and pap46 execution times using research models. December 2017. n indicates observations, Method indicates algorithm, and the "t" columns contain time to completion (in seconds) by server. Servers were dedicated during execution.

-	n	Method	t.pap1	t.pap46
1	10000	feXTX	1.50	1.79
2	25000	feXTX	1.50	2.06
3	50000	feXTX	1.75	2.39
4	100000	feXTX	2.34	2.90
5	150000	feXTX	2.68	3.50
6	250000	feXTX	3.77	5.25
7	500000	feXTX	5.63	7.78
8	1000000	feXTX	13.25	17.64
9	1500000	feXTX	22.94	26.67
10	2000000	feXTX	47.56	54.87
11	5000000	feXTX	241.93	332.27
12	10000000	feXTX	1396.29	1725.81
13	25000000	feXTX	5928.08	8024.80
14	10000	Matrix1	0.05	0.11
15	25000	Matrix1	0.12	0.20
16	50000	Matrix1	0.27	0.35
17	100000	Matrix1	0.56	0.92
18	150000	Matrix1	1.04	1.58
19	250000	Matrix1	1.92	3.13
20	500000	Matrix1	3.83	6.31
21	1000000	Matrix1	8.62	13.38
22	1500000	Matrix1	14.65	18.54
23	2000000	Matrix1	23.99	33.57
24	5000000	Matrix1	362.98	433.91
25	10000000	Matrix1	5251.48	5981.92
26	25000000	Matrix1	9411.06	10303.39
27	10000	Matrix2	0.08	0.11
28	25000	Matrix2	0.15	0.20
29	50000	Matrix2	0.30	0.32
30	100000	Matrix2	0.67	0.87
31	150000	Matrix2	0.86	1.16
32	250000	Matrix2	1.42	2.16
33	500000	Matrix2	2.69	4.10
34	1000000	Matrix2	5.68	8.80
35	1500000	Matrix2	9.30	12.31
36	2000000	Matrix2	14.10	19.86
37	5000000	Matrix2	63.07	73.23
38	10000000	Matrix2	375.82	480.18
39	25000000	Matrix2	2092.43	2932.28

# Duke University Human Capital / Synthetic Data Project Server Performance Comparison Parallel R with Sparse Matrix Algorithms

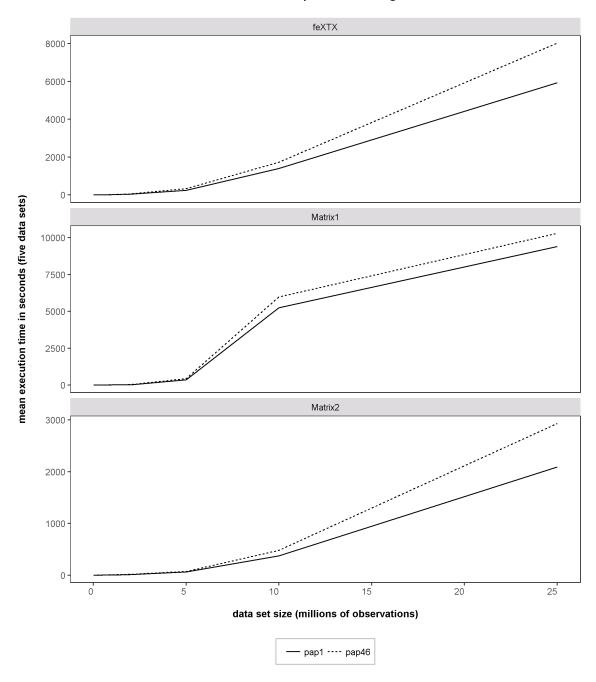


Figure 1: Comparison of pap1 and pap46 execution times using research models. December 2017. Servers were dedicated during execution.

## CURRENT TESTING

Beginning around 1/15/2018 additional testing was begun using algorithms with similar computations, but different implementation from those used in December. While conducting tests, total CPU utilization generally appeared lower on pap1 and pap2 than on pap36 and pap46. Variability in CPU utilization also appeared greater on pap1 and pap2, with a 20% inter-day deviation observed on pap1 while executing identical algorithms with similar data. Observations were made after confirming that no other user processes were active. Table 2 compares execution time by server and figure 2 plots execution time by observation count. In these results, pap46 appears to out perform pap1. The data used in January are similar to that used in December and, although solution methods differ, the computational load is very similar, making the change in pap46 performance relative to pap1 unexpected.

Table 2: Comparison of pap1, pap2, pap36, and pap46 execution times using research models. January 2018. n indicates observations, Problem indicates the problem and algorithm used, and the "t" columns contain time to completion (in seconds) by server. Servers were dedicated during execution.

	n	Problem	t.pap1	t.pap46	t.pap2	t.pap36
1	1000000	tData	3.44	2.65	2.63	3.01
2	5000000	tData	14.80	13.11	12.65	14.56
3	10000000	tData	32.99	26.31	25.90	27.49
4	25000000	tData	79.14	71.33	72.06	79.28
5	1000000	tXTX	0.36	0.35	0.35	0.39
6	5000000	tXTX	1.85	1.76	1.71	1.91
7	10000000	tXTX	4.97	4.41	4.41	4.99
8	25000000	tXTX	31.91	26.04	27.61	32.45
9	1000000	tChol	0.48	0.27	0.28	0.27
10	5000000	tChol	0.81	0.59	0.65	0.62
11	10000000	tChol	2.08	1.35	1.49	1.45
12	25000000	tChol	108.22	71.58	86.96	77.46
13	1000000	$_{ m tBeta}$	0.01	0.01	0.01	0.01
14	5000000	$_{ m tBeta}$	0.12	0.09	0.04	0.13
15	10000000	$_{ m tBeta}$	0.58	0.49	0.28	0.59
16	25000000	$_{ m tBeta}$	15.68	13.31	10.83	16.06
17	1000000	tvBeta	0.51	0.37	0.36	0.34
18	5000000	tvBeta	1.34	0.98	1.01	0.98
19	10000000	tvBeta	4.21	2.46	2.66	2.69
_20	25000000	tvBeta	207.83	133.06	155.83	151.22

# Duke University Human Capital / Synthetic Data Project Server Performance Comparison feXTX OMP C Algorithms

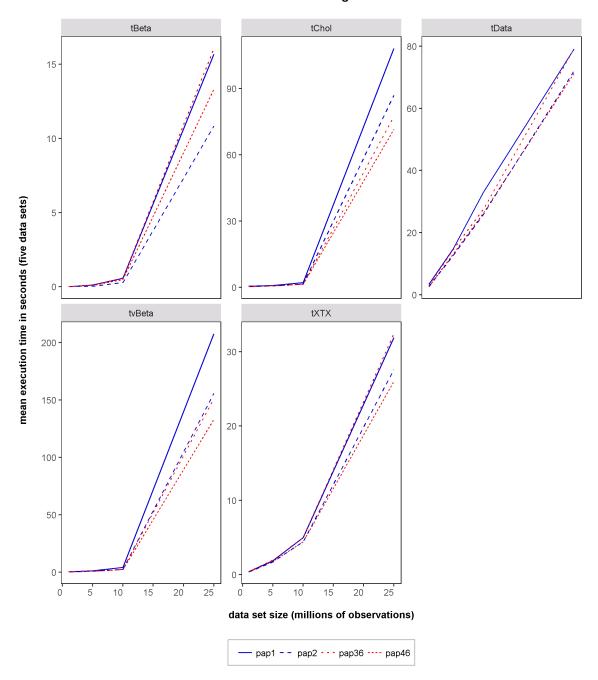


Figure 2: Comparison of pap1, pap2, pap36, and pap46 execution times using research models. January 2018. Servers were dedicated during execution.

The scripts used for the previous test involve custom, parallelize C functions using the open MP library. It should be noted that C functions were compiled on a separate Windows host (none of the servers evaluated here) and shared copies of the executable are used by all servers. To test performance of more standard R functions, models were solved using compatible algorithms from the Matrix and MatrixModels packages. Table 3 and figure 3 compare execution time between servers. As with other January results, pap46 appears to outperform pap1.

Table 3: Comparison of pap1 and pap46 execution times using Matrix package. January 2018. n indicates observations, Problem indicates the problem and algorithm used, and the "t" columns contain time to completion (in seconds) by server. Servers were dedicated during execution.

	n	Problem	t.pap1	t.pap46
1	1000000	tData	3.08	2.95
2	5000000	tData	14.79	13.01
3	10000000	tData	33.02	25.89
4	25000000	tData	83.56	71.40
5	1000000	tX	4.06	2.77
6	5000000	tX	25.19	17.22
7	10000000	tX	65.29	43.03
8	25000000	tX	218.94	154.93
9	1000000	tXTX	2.16	1.53
10	5000000	tXTX	19.00	10.73
11	10000000	tXTX	44.93	28.23
12	25000000	tXTX	183.27	114.02
13	1000000	tChol	0.24	0.18
14	5000000	tChol	1.66	1.11
15	10000000	tChol	14.64	10.10
16	25000000	tChol	1270.49	1089.93

# Duke University Human Capital / Synthetic Data Project Server Performance Comparison Sparse Matrix Algorithms

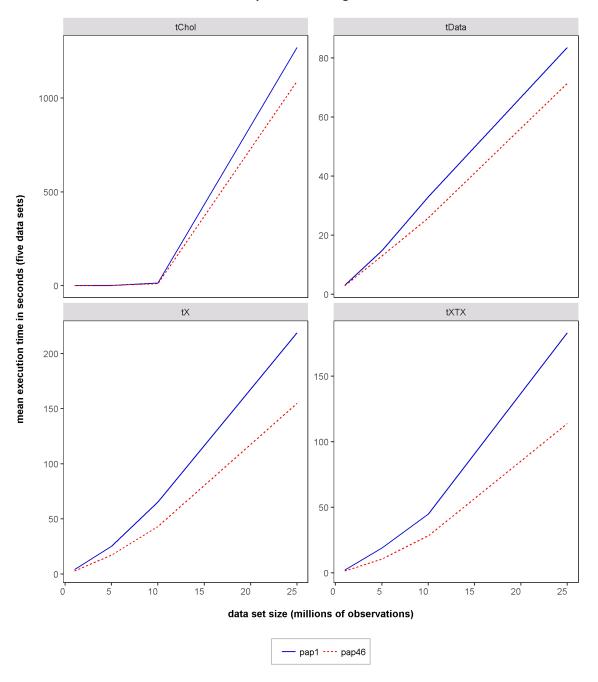


Figure 3: Comparison of pap1 and pap46 execution times using Matrix package. January 2018. Servers were dedicated during execution.

## CPU UTILIZATION

Two algorithms with high computational demand are the Cholesky decomposition and computation of a matrix inverse using a computed Cholesky decomposition. Custom parallelized C functions for these operations, using the open MP library, were executed on each server using a large random data set generated on each server using identical seed values. Figure 4 contains screen shots of the task manager performance tab for each server while computing the Cholesky decomposition. Although snapshots, images were taken at moments of customary utilization. Scripts were executed on 1/25/2018. Table 4 lists CPU utilization and time to compute the Cholesky decomposition. Figure 5 and table 5 show CPU utilization and time to compute the inverse of a large matrix using its Cholesky decomposition. From the tables and graphs, it appears that computation time is dependent on CPU utilization and, at the time of this test, pap46 experienced better CPU utilization than did the other servers.

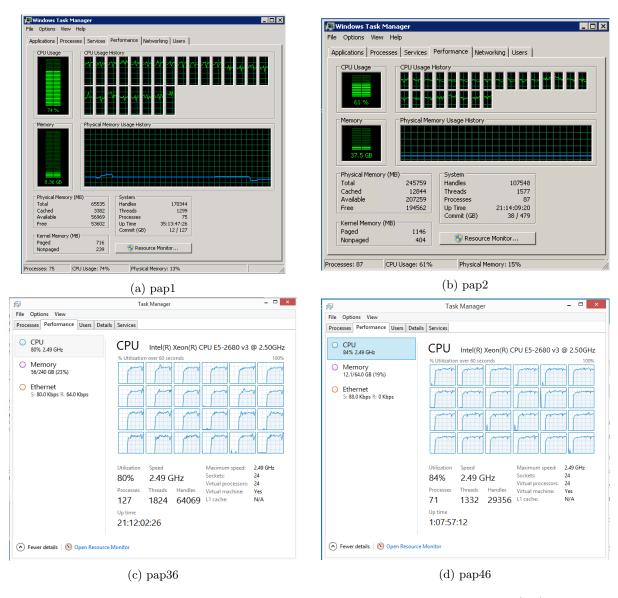


Figure 4: CPU utilization while computing Cholesky decomposition of a large matrix. 1/25/2018. Servers were dedicated during execution.

Table 4: CPU utilization and time to compute Cholesky decomposition of a large matrix. 1/25/2018. Servers were dedicated during execution.

Server	CPU Utilization	Computation Time (sec)
pap1	74%	74.94
pap2	61%	105.09
pap36	80%	80.06
pap46	84%	70.20

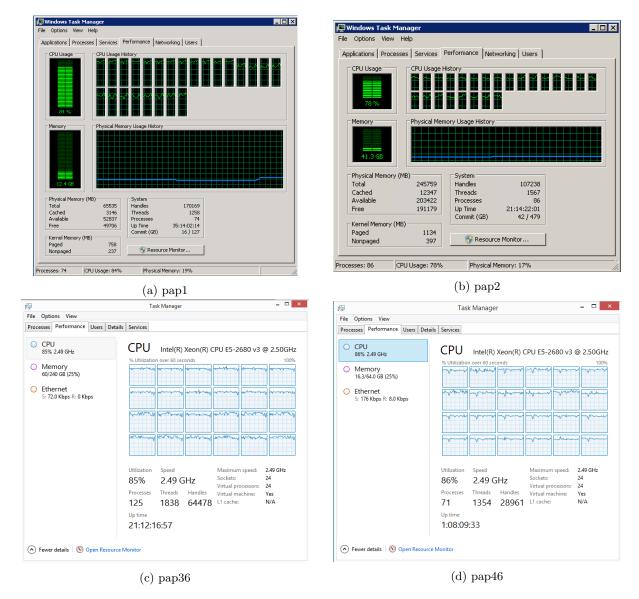


Figure 5: CPU utilization while computing matrix inverse using Cholesky decomposition. 1/25/2018. Servers were dedicated during execution.

Table 5: CPU utilization and time to compute inverse of matrix using Cholesky decomposition. 1/25/2018. Servers were dedicated during execution.

Server	CPU Utilization	Computation Time (sec)
pap1	84%	150.20
pap2	78%	152.32
pap36	85%	147.39
pap46	86%	128.77

# QUESTIONS

- Has something changed in the configurations of pap1 and pap46 since December 2017?
- Why does pap46 appear to outperform the other three servers? Whatever the cause, and if it is robust to operating conditions and reboot, we want to capitalize on it!

## FURTHER STEPS IN EVALUATING PERFORMANCE

- Repeat evaluation of December 2017 tests (parallel R and Sparse Matrix methods). Objective is to determine whether pap1 continues to outperform pap46. January results would suggest not.
- Repeat CPU utilization comparison, monitoring inter-day variation, especially after server reboot.

# SERVER CONFIGURATION AS REPORTED BY R

Server: pap1 (configured in 2012)

```
R version 3.2.1 (2015-06-18)
```

Platform: x86\_64-w64-mingw32/x64 (64-bit)

Running under: Windows Server 2008 R2 x64 (build 7601) Service Pack 1

### locale:

- [1] LC\_COLLATE=English\_United States.1252
- [2] LC\_CTYPE=English\_United States.1252
- [3] LC\_MONETARY=English\_United States.1252
- [4] LC\_NUMERIC=C
- [5] LC\_TIME=English\_United States.1252

### attached base packages:

- [1] parallel stats graphics grDevices utils datasets methods
- [8] base

# other attached packages:

[1] MatrixModels\_0.4-1 Matrix\_1.2-1

loaded via a namespace (and not attached):

[1] grid\_3.2.1 lattice\_0.20-31

Server: pap2 (configured in 2012)

```
R version 3.2.1 (2015-06-18)
```

Platform: x86\_64-w64-mingw32/x64 (64-bit)

Running under: Windows Server 2008 R2 x64 (build 7601) Service Pack 1

#### locale:

- [1] LC\_COLLATE=English\_United States.1252
- [2] LC\_CTYPE=English\_United States.1252
- [3] LC\_MONETARY=English\_United States.1252
- [4] LC\_NUMERIC=C
- [5] LC\_TIME=English\_United States.1252

# attached base packages:

- [1] parallel stats graphics grDevices utils datasets methods
- [8] base

## other attached packages:

[1] MatrixModels\_0.4-1 Matrix\_1.2-1

loaded via a namespace (and not attached):

[1] Rcpp\_0.12.0 grid\_3.2.1 lattice\_0.20-31

## Server: pap46 (replacement for pap1, configured in 2017)

R version 3.4.1 (2017-06-30)

Platform: x86\_64-w64-mingw32/x64 (64-bit)

Running under: Windows Server 2012 R2 x64 (build 9600)

Matrix products: default

### locale:

- [1] LC\_COLLATE=English\_United States.1252
- [2] LC\_CTYPE=English\_United States.1252
- [3] LC\_MONETARY=English\_United States.1252
- [4] LC\_NUMERIC=C
- [5] LC\_TIME=English\_United States.1252

### attached base packages:

- [1] parallel stats graphics grDevices utils datasets methods
- [8] base

# other attached packages:

[1] MatrixModels\_0.4-1 Matrix\_1.2-10

loaded via a namespace (and not attached):

[1] compiler\_3.4.1 Rcpp\_0.12.11 lattice\_0.20-35 grid\_3.4.1

# Server: pap36 (replacement for pap2, configured in 2017)

R version 3.4.1 (2017-06-30)

Platform: x86\_64-w64-mingw32/x64 (64-bit)

Running under: Windows Server 2012 R2 x64 (build 9600)

Matrix products: default

### locale:

- [1] LC\_COLLATE=English\_United States.1252
- [2] LC\_CTYPE=English\_United States.1252
- [3] LC\_MONETARY=English\_United States.1252

```
[4] LC_NUMERIC=C
```

[5] LC\_TIME=English\_United States.1252

attached base packages:

- [1] parallel stats graphics grDevices utils datasets methods
- [8] base

other attached packages:

[1] MatrixModels\_0.4-1 Matrix\_1.2-10

loaded via a namespace (and not attached):

[1] compiler\_3.4.1 Rcpp\_0.12.11 grid\_3.4.1 lattice\_0.20-35}

# R SCRIPTS USED FOR TESTING

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