

1  
Data Matrix:  $D$   $m \times n$   $m > n$

Covariance  $D^T D$

eigen functions, eigen values:

$$[e, \lambda] = \text{eig}(D^T D);$$

$$D^T D e = e \lambda$$

$$D^T D = e \lambda e^T$$

$$A = D e; \quad \text{PCs}$$

Singular Value Decomposition

$$D = U S V^T$$

$$D^T D = V S^T U^T U S V^T$$

$$= V S^T S V^T$$

$$= V S^2 V^T$$

$\left\{ \begin{array}{l} V \text{ is equivalent to } e \\ S^2 \text{ " " " to } \lambda. \end{array} \right.$

$$A = U S; \quad \text{PCS}$$