

CSCI3240 Exam 1 Study Guide Answers

Spring 2023

Exam 1 Question Format

1. Multiple choice
2. Fill in the blanks
3. True or False

Chapter 2: Practice Problems

- I. Assume we are running code on a 8-bit machine using two's complement arithmetic for signed integers. A "short" integer is encoded using 4 bits. Fill in the empty boxes in the table below. The following definitions are used in the table:

```
short sy = -3;
```

```
int y = sy;
```

```
int x = -17;
```

```
unsigned ux = x
```

Note: You need not fill in entries marked with "–"

Only accepted format for binary representation (use 8-bits): 00000000, 11111111

Only accepted format for hexadecimal representation: 4D, EF, FF

Expression	Decimal	Binary	Hexadecimal
Zero	0	00000000	00
-	-3	11111101	FD
-	50	00110010	32
ux	239	11101111	EF
y	-3	11111101	FD
x >> 2	-5	11111011	FB
Tmax	127	01111111	7F
Tmax+Tmin	-1	11111111	FF
Tmin - 1	127	01111111	7F

- II. Assume we are running code on a 10-bit machine using two's complement arithmetic for signed integers. Fill in the empty boxes in the table below. The following definitions are used in the table:

`int y = -9;`

`unsigned z = y;`

Note: You need not fill in entries marked with “–”

Only accepted format for binary representation (use 10-bits): 0000000000, 1111111111

Only accepted format for hexadecimal representation: 2FD, 1EF, 3FF

Expression	Decimal	Binary	Hexadecimal
Zero	0	0000000000	000
-	-5	1111111011	3FB (FFB also accepted)
–	18	0000010010	012
y	-9	1111110111	3F7 (FF7 also accepted)
z	1015	1111110111	3F7
y-z	0	0000000000	000
-Tmax	-511	1000000001	201 (E01 also accepted)
-Tmin	-512	1000000000	200 (E00 also accepted)
Tmax +1	-512	1000000000	200 (E00 also accepted)

III. Integer puzzles

Check if the statements are always true?

Initialization

```
int x = foo();
int y = bar();
unsigned ux = x;
unsigned uy = y;
```

1. $x < 0 \Rightarrow ((x*2) < 0)$
2. $ux \geq 0$
3. $x \& 7 == 7 \Rightarrow (x < 30) < 0$
4. $ux > -1$
5. $x > y \Rightarrow -x < -y$
6. $x * x \geq 0$
7. $x > 0 \&\& y > 0 \Rightarrow x + y > 0$
8. $x \geq 0 \Rightarrow -x \leq 0$
9. $x \leq 0 \Rightarrow -x \geq 0$
10. $(x|-x) >> 31 == -1$
11. $ux >> 3 == ux/8$
12. $x >> 3 == x/8$
13. $x \& (x-1) != 0$

IV. What is the output of the following code?

Assume that int is 32 bits, short is 16 bits, and the representation is two's complement.

```
unsigned int x = 0xDEADBEEF;
unsigned short y = 0xFFFF;
signed int z = -1;
if (x > (signed short) y)
    printf("Hello");
if (x > z)
    printf("World");
```

- (a) Prints nothing.
- (b) Prints "Hello"
- (c) Prints "World"
- (d) Prints "HelloWorld"

V. After executing the following code, which of the variables are equal to 0?

```
unsigned int a = 0xffffffff;
unsigned int b = 1;
unsigned int c = a + b;
unsigned long d = a + b;
unsigned long e = (unsigned long)a + b;
(Assume ints are 32 bits wide and longs are 64 bits wide.)
```

(a) None of them

(b) c

(c) c and d

(d) c, d, and e

VI. Floating point representation

Consider a 12-bit variant of the IEEE floating point format as follows:

- Sign bit
- 5-bit exponent with a bias of 15.
- 6-bit significand

All of the rules for IEEE 754 Standard apply.

Fill in the numeric value represented by the following bit patterns. You **must** write your number in decimal form (e.g. 0.0146485375, -0.0146485375).

Bit Pattern	Numerical Value
010011101110	27.5
111011101011	-6848
100101001111	-0.001205444
001010111010	0.059570313

VII. Floating points puzzles

■ For each of the following C expressions, either:

- Argue that it is true for all argument values
- Explain why not true

```
int x = ...;  
float f = ...;  
double d = ...;
```

Assume neither
d nor f is NaN

- `x == (int)(float) x`
- `x == (int)(double) x`
- `f == (float)(double) f`
- `d == (double)(float) d`
- `f == -(-f);`
- `2/3 == 2/3.0`
- `d < 0.0` $\Rightarrow ((d*2) < 0.0)$
- `d > f` $\Rightarrow -f > -d$
- `d * d >= 0.0`
- `(d+f) - d == f`

Chapter 3: Practice Problems

VIII. You are given the following C code to compute integer absolute value:

```
int abs(int x)
{
    return x < 0 ? -x : x;
}
```

You've concerned, however, that mispredicted branches cause your machine to run slowly. So, knowing that your machine uses a two's complement representation, you try the following (recall that `sizeof(int)` returns the number of bytes in an `int`):

```
int opt_abs(int x)
{
    int mask = x >> (sizeof(int)*8-1);
    int comp = x ^ mask;
    return comp;
}
```

A. What bit pattern does `mask` have, as a function of `x`?

→ 1111....1111 for $x < 0$

0000...0000 for $x \geq 0$

B. What numerical value does `mask` have, as a function of `x`?

→ -1 for $x < 0$

0 for $x \geq 0$

C. For what values of `x` do functions **`abs`** and **`opt_abs`** return identical results?

→ $x \geq 0$

D. For the cases where they produce different results, how are the two results related?

→ `opt_abs(x) == abs(x)-1`

E. Show that with the addition of just one single arithmetic operation (any C operation is allowed) that you can fix opt abs. Show your modifications on the original code. (*You can just provide the line that you will add*).

→ adding 1 to the result : `int comp = x ^ mask + 1;`

F. Are there any values of x such that **abs** return a value that is **not** greater than 0? Which value(s)?

→ 0 and TMin

IX. Consider the following C functions and assembly code

```
long functionA(long a){  
    return a * 30;  
}
```

```
long functionB(long a){  
    return a * 34;  
}
```

```
long functionC(long a){  
    return a * 16;  
}
```

```
long functionD(long a){  
    return a * 18;  
}
```

```
long functionD(long a){  
    return a * 36;  
}
```

Assembly code:

```
movq %rdi, %rax  
salq $3, %rax  
addq %rdi, %rax  
addq %rax, %rax  
retq
```

Which of the functions compiled into the assembly code shown?

X. Consider the following C functions and assembly code

Assume that long is 64 bits, int is 32 bits, short is 16 bits, and the representation is two's complement.

Assembly Code:

```
imulq %rsi, %rdi
imulq %rdx, %rsi
addq %rsi, %rdi
leaq (%rdi,%rdi,2), %rax
salq $3, %rax
ret
```

```
long functionA(long a, long b, long c){
long d = a*b;
long e = b*c;
return 18 * (d+e);
}
```

```
long functionB(long a, long b, long c){
long d = a*b;
long e = b*c;
return 24 * (d*e);
}
```

```
long functionC(long a, long b, long c){
long d = a*b;
long e = b*c;
return 24 * (d+e);
}
```

```
long functionD(long a, long b, long c){
long d = a*b;
long e = b*c;
return 32 * (d*e);
}
```

Which of the functions compiled into the assembly code shown?

XI. What is the C equivalent of `mov 0x44(%rax,%rcx,8), %rdx`

- (a) `rdx = rax + rcx + 8 + 44`
- (b) `*(rax + rcx + 8 + 10) = rdx`
- (c) `rdx = *(rax + rcx*8 + 0x44)`
- (d) `rdx = *(rax + rcx + 8 + 0x44)`

XII. Reconstruct the following C code for this recursive function by looking at the assembly code. Fill in the blanks:

```
unsigned myfunction2(unsigned n)

{
    if (n==0) return 1;
    else {
        return 1 + myfunction2(n/4);
    }
}

myfunction2:
    testq    %rdi, %rdi
    jne     .L9
    movq    $1, %rax
    ret

.L9:
    subq    $8, %rsp
    shrq    $2, %rdi
    call    myfunction2
    addq    $1, %rax
    addq    $8, %rsp
    ret
```