

3.  $H \Rightarrow$  Set of all integers divisible by  $13-3=10$

$$h \in 10\mathbb{Z} \text{ in } (H, +) = (10\mathbb{Z}, +)$$

Requirements of a group...

$$\{b, c\} \subset \mathbb{Z}$$

① Closed:

$$\rightarrow 10 + 10b + 10c = 10(1+b+c)$$

10 always divides 10

so any member in the set + another member returns a member of the set

② Associative:  $\{a, b, c\} \subset \mathbb{Z}$

$$\rightarrow 10a + (10b + 10c) = 10a + 10b + 10c = (10a + 10b) + 10c$$

Follows from rules of arithmetic that  $(H, +)$  is associative

③ Identity:  $\{a, b, c\} \subset \mathbb{Z}$

$$\rightarrow 0 \in 10\mathbb{Z}$$

$$\rightarrow 10a + 0 = 10a \text{ making } 0 \text{ the identity element of } 10\mathbb{Z}$$

④ Inverse:  $\{a, b\} \subset \mathbb{Z}$

$\rightarrow$  The inverse of  $10a$  is  $-10a$ . Proof:

$$10a + b = 0$$

$$10a = -b$$

$$b = -10a$$

Every element's inverse is its negative counterpart