

# Imputation Plots

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## Introduction

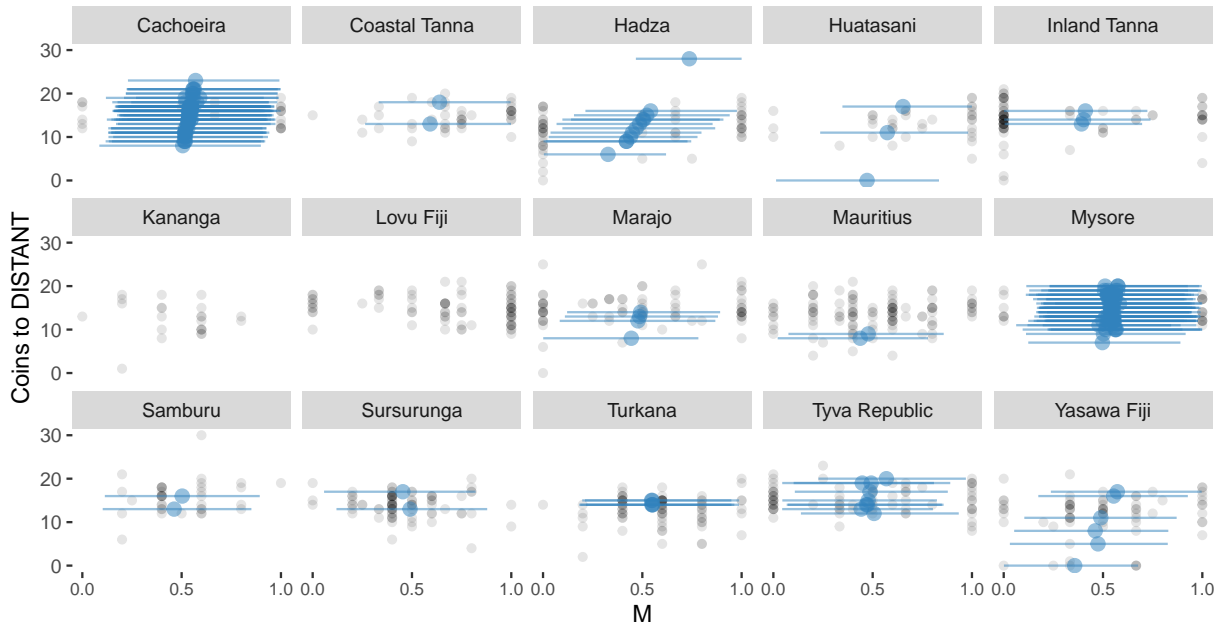
This notebook reports plots from missing data imputations of all variables and across all main models. The imputations of the supplementary models can also be inspected, see the `.Rmd` file for details.

In the plots, the black points are observed values, while the blue points and intervals are posterior means and HPDIs of the imputed values. The **caption gives the model** – e.g., `RAG SELF INT` refers to the RAG SELF interaction model and `RAG SELF ADD` refers to the RAG SELF additive model – and the ***x*-axis gives the variable key**.

Note that for the binary variables food security (`S`) and game check (`check`), the imputed values are the probabilities of a 1 (denoted, respectively, by  $\phi_{\text{food}}$  and  $\phi_{\text{check}}$  in our formal model notation).

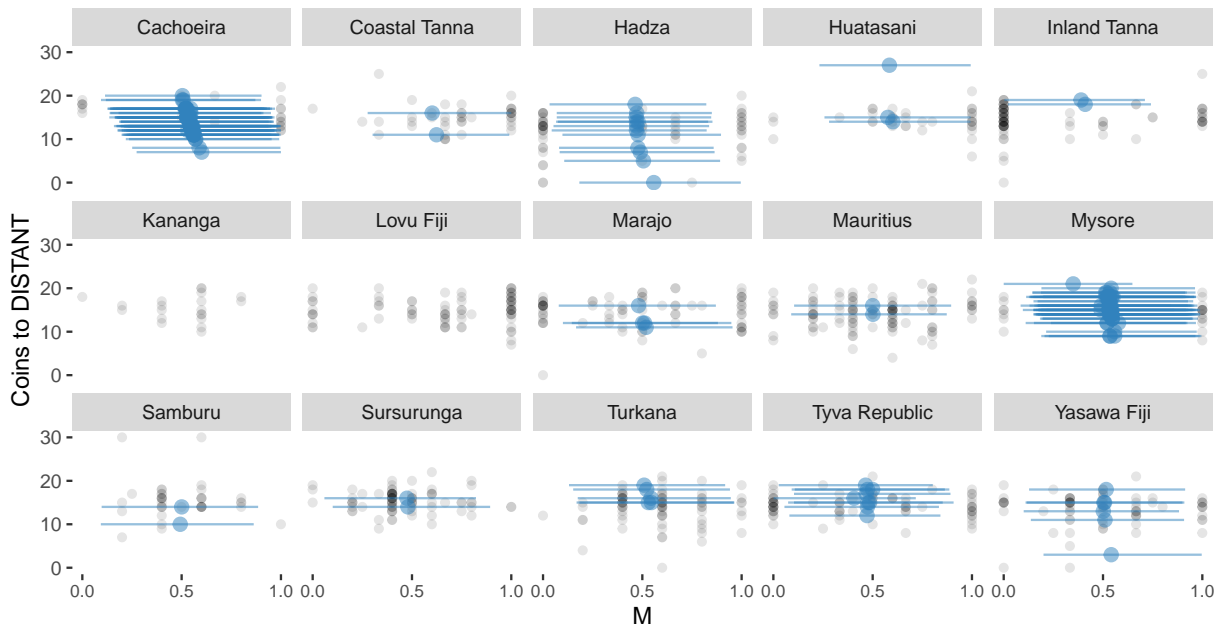
## Missing Data Imputation

Visualizing observed vs. **imputed** values



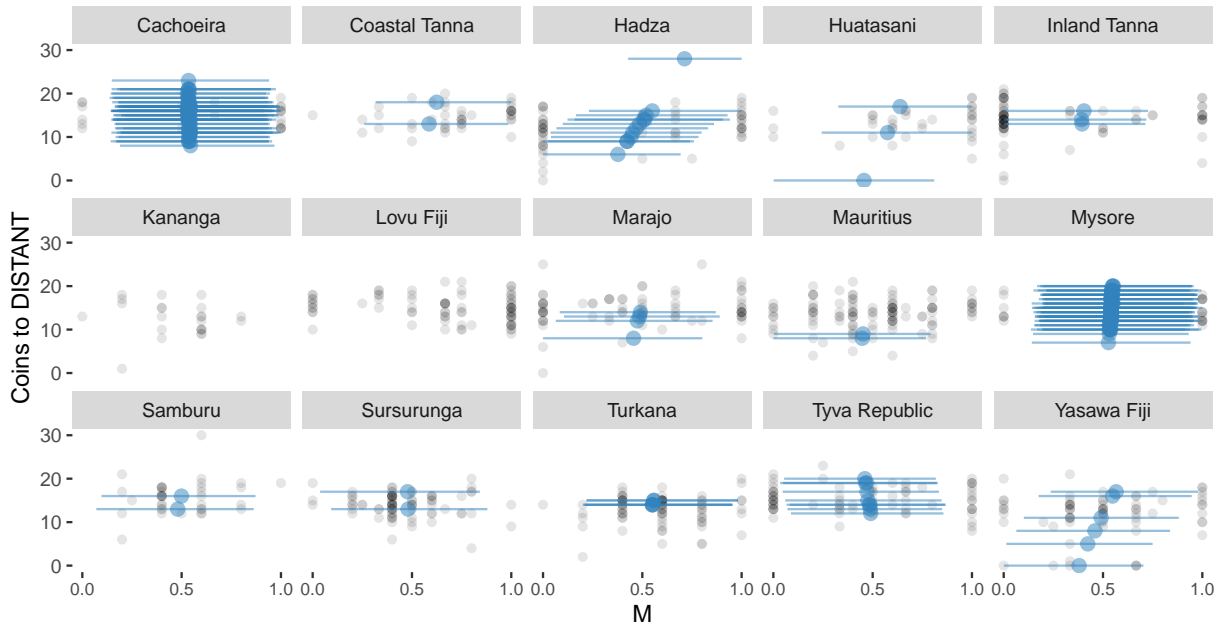
## Missing Data Imputation

Visualizing observed vs. **imputed** values



## Missing Data Imputation

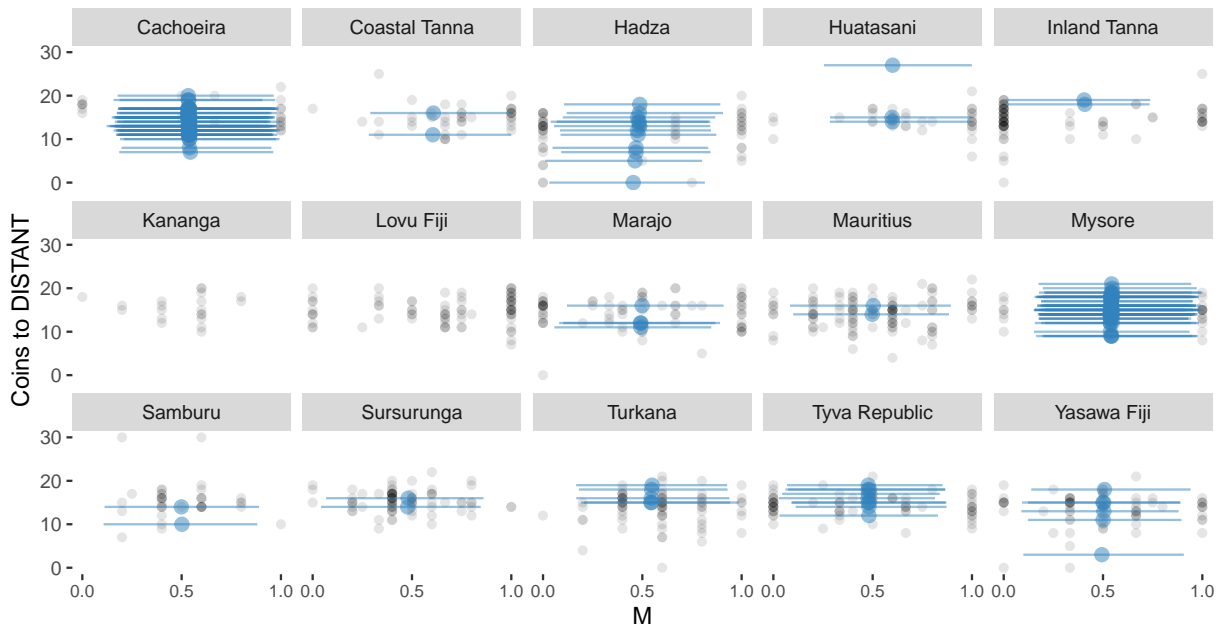
Visualizing observed vs. **imputed** values



RAG SELF ADD Model.  
Imputed values are posterior means and 89% HPDIs.

## Missing Data Imputation

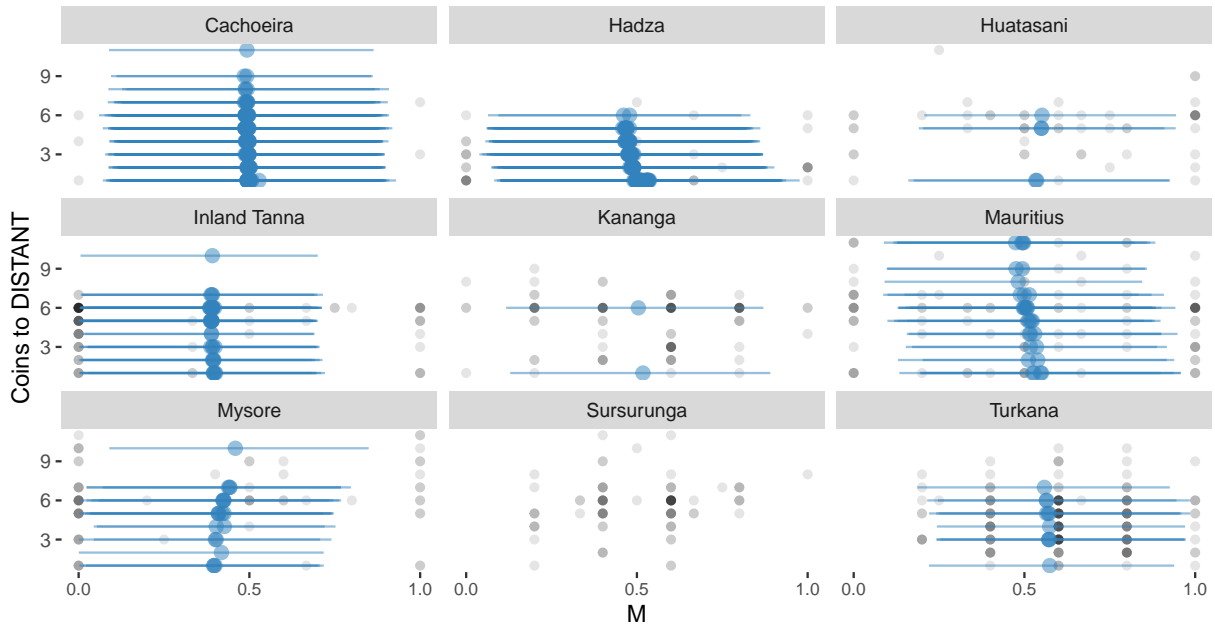
Visualizing observed vs. **imputed** values



RAG LOCAL ADD Model.  
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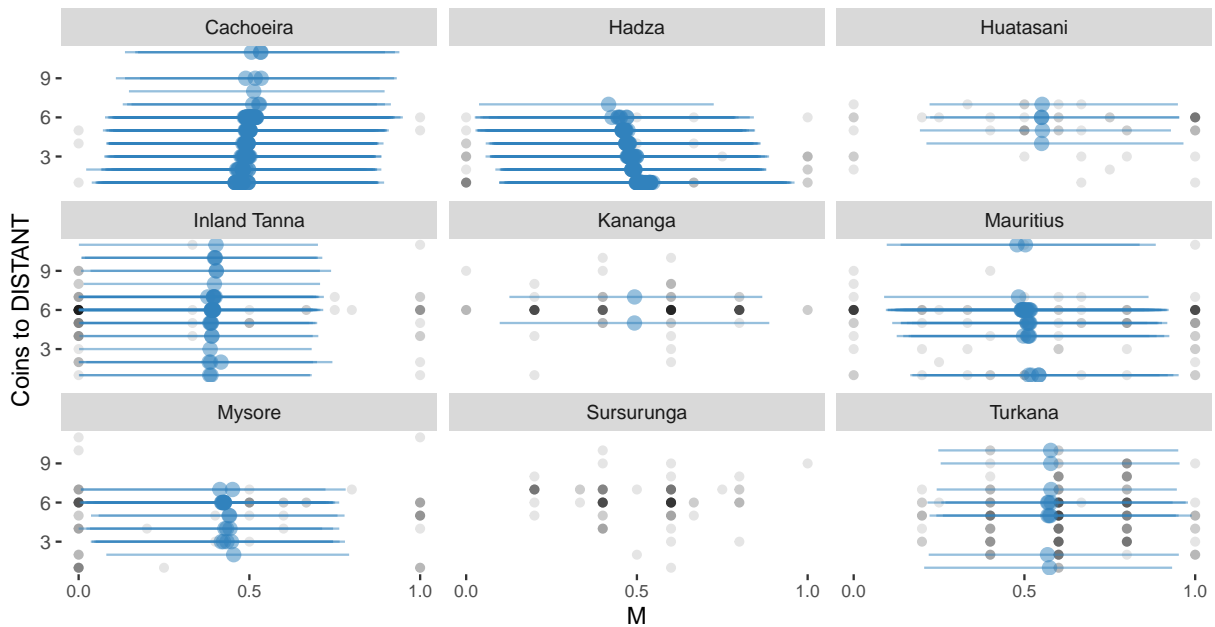
## Missing Data Imputation

Visualizing observed vs. **imputed** values



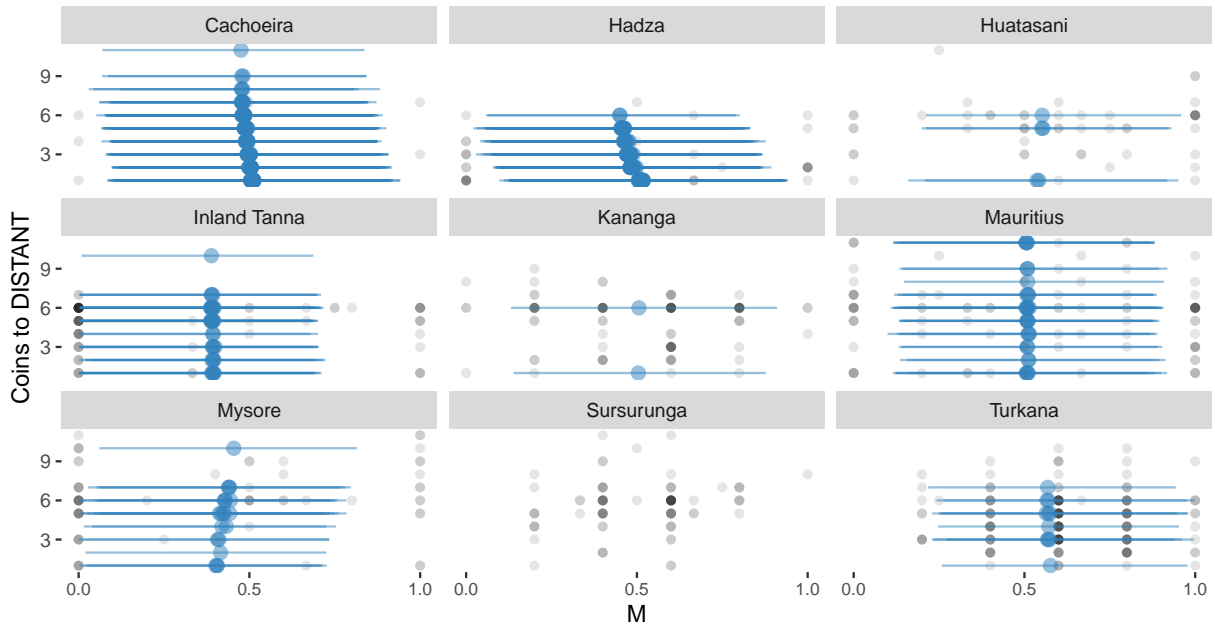
## Missing Data Imputation

Visualizing observed vs. **imputed** values



## Missing Data Imputation

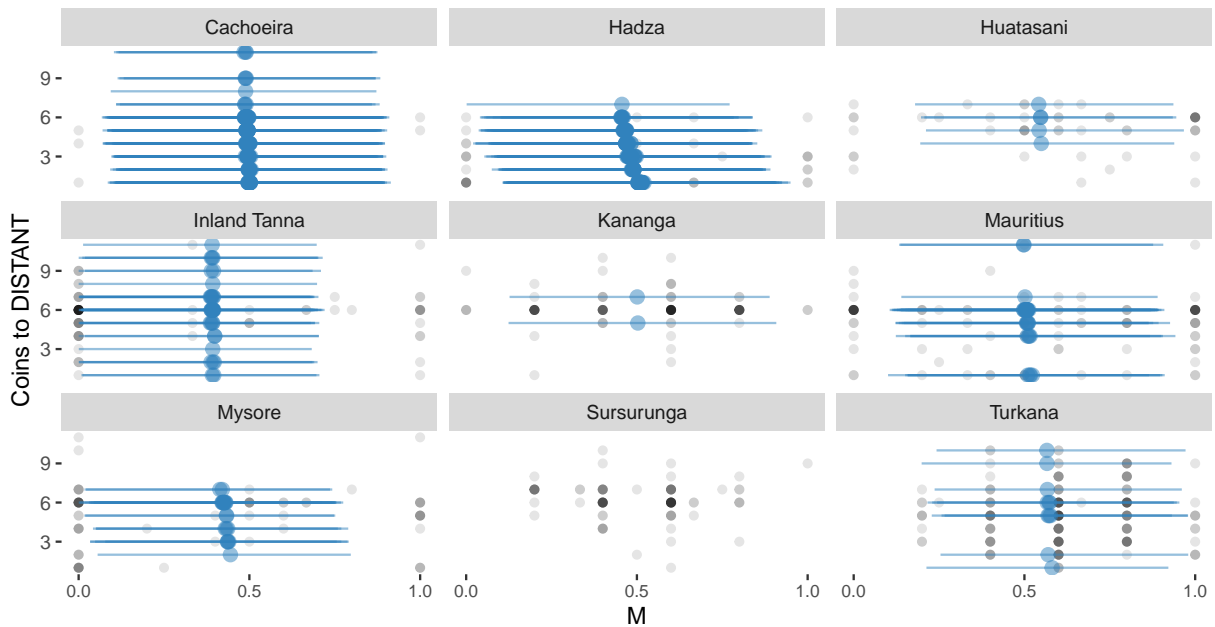
Visualizing observed vs. **imputed** values



DG SELF ADD Model.  
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## Missing Data Imputation

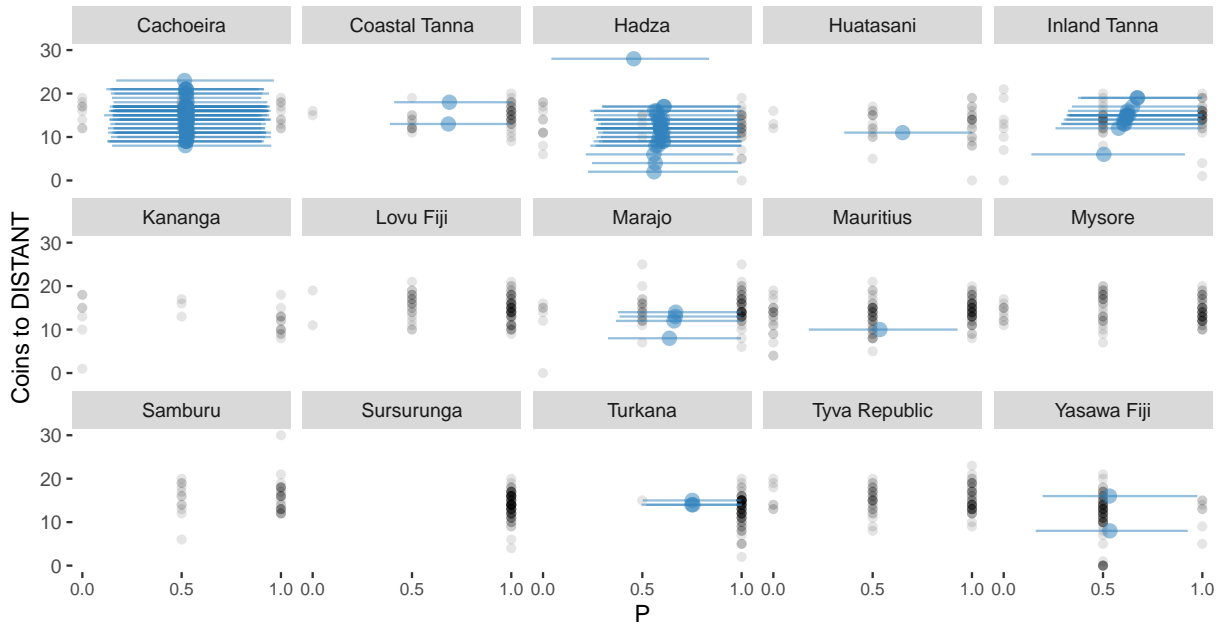
Visualizing observed vs. **imputed** values



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## Missing Data Imputation

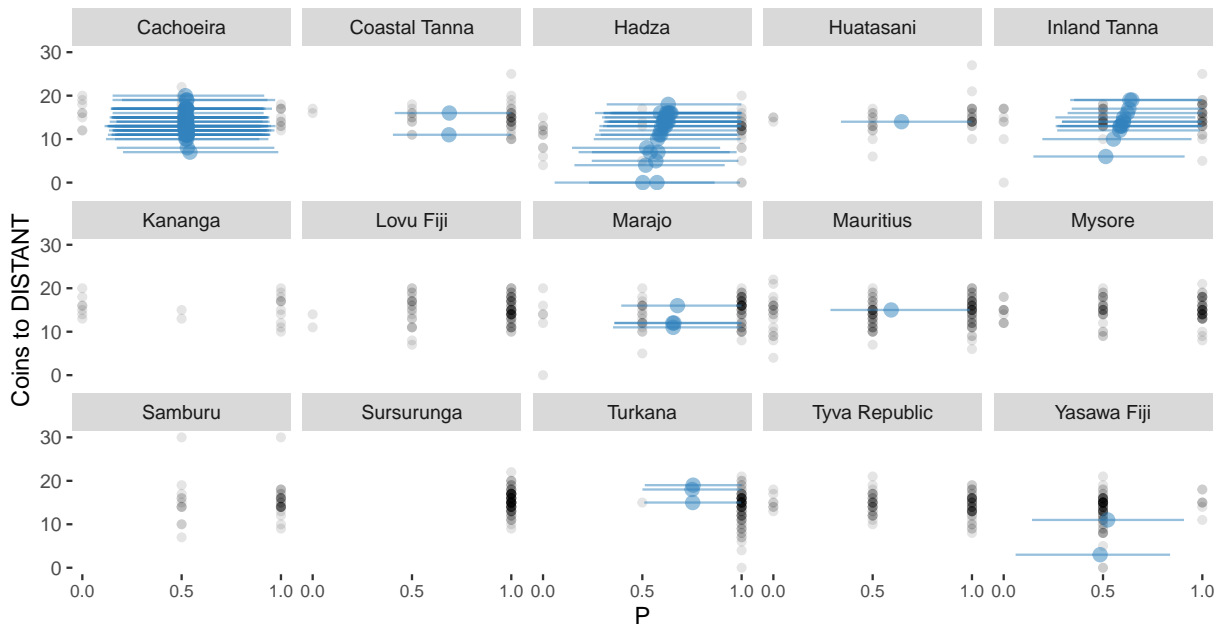
Visualizing observed vs. **imputed** values



RAG SELF INT Model.  
Imputed values are posterior means and 89% HPDIs.

## Missing Data Imputation

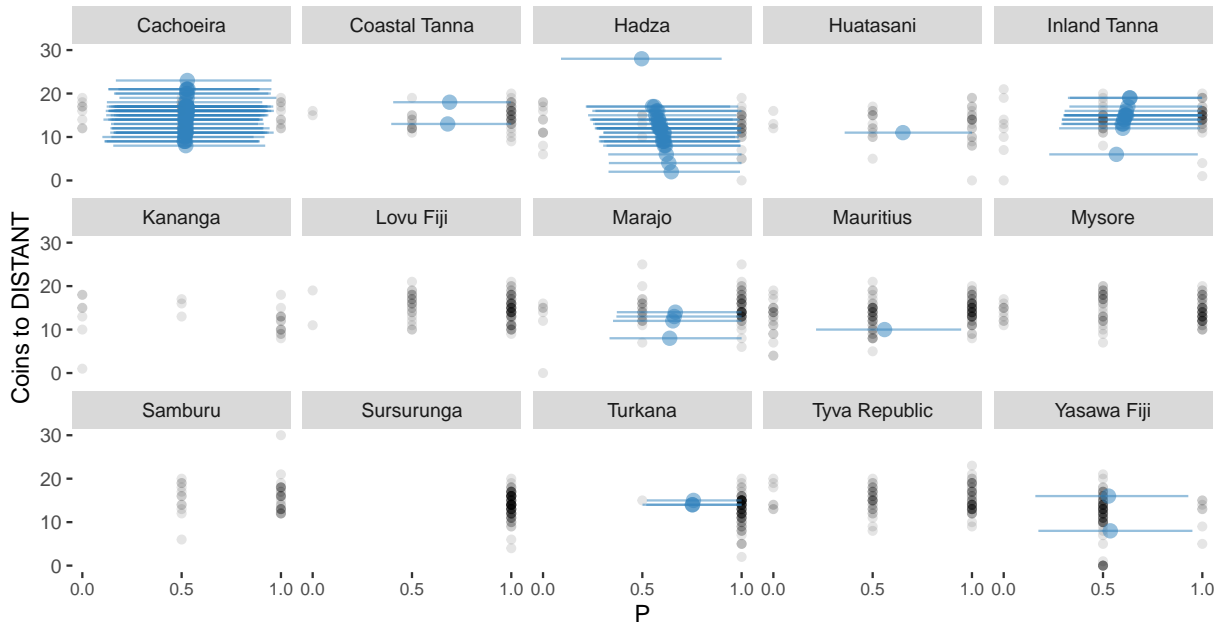
Visualizing observed vs. **imputed** values



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## Missing Data Imputation

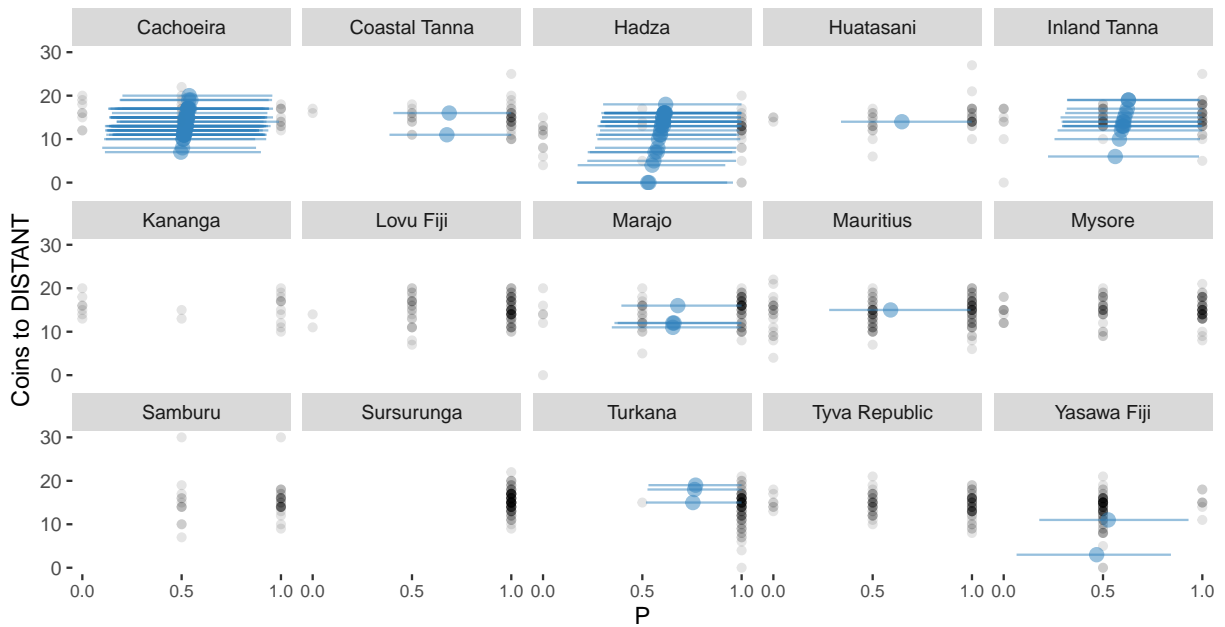
Visualizing observed vs. **imputed** values



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## Missing Data Imputation

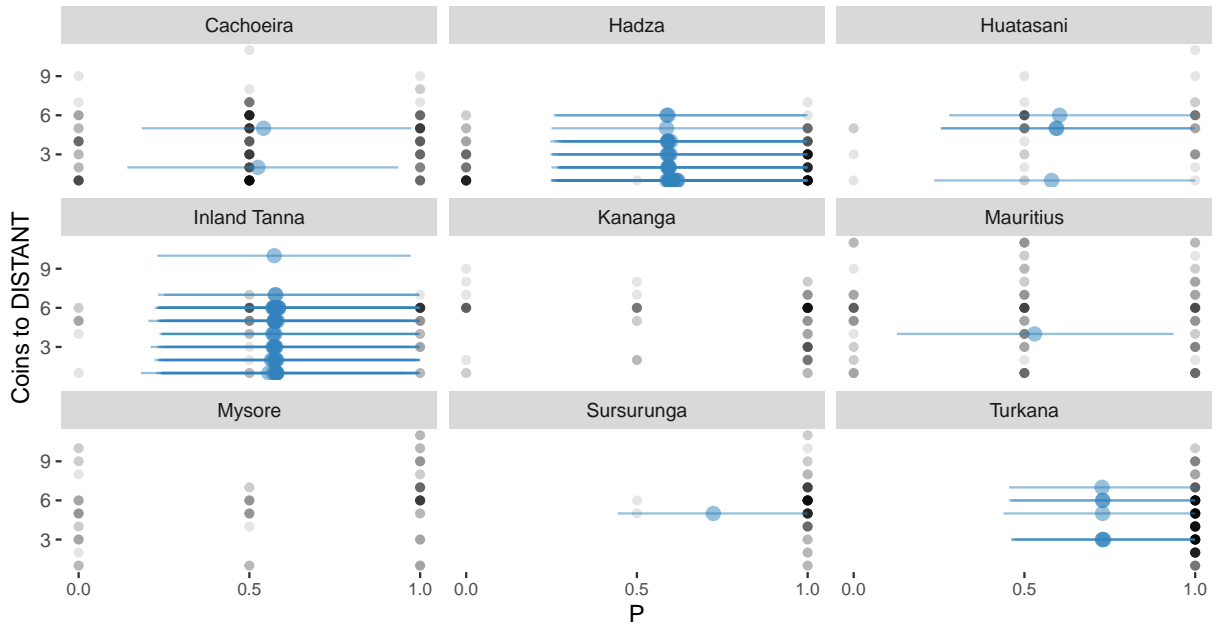
Visualizing observed vs. **imputed** values



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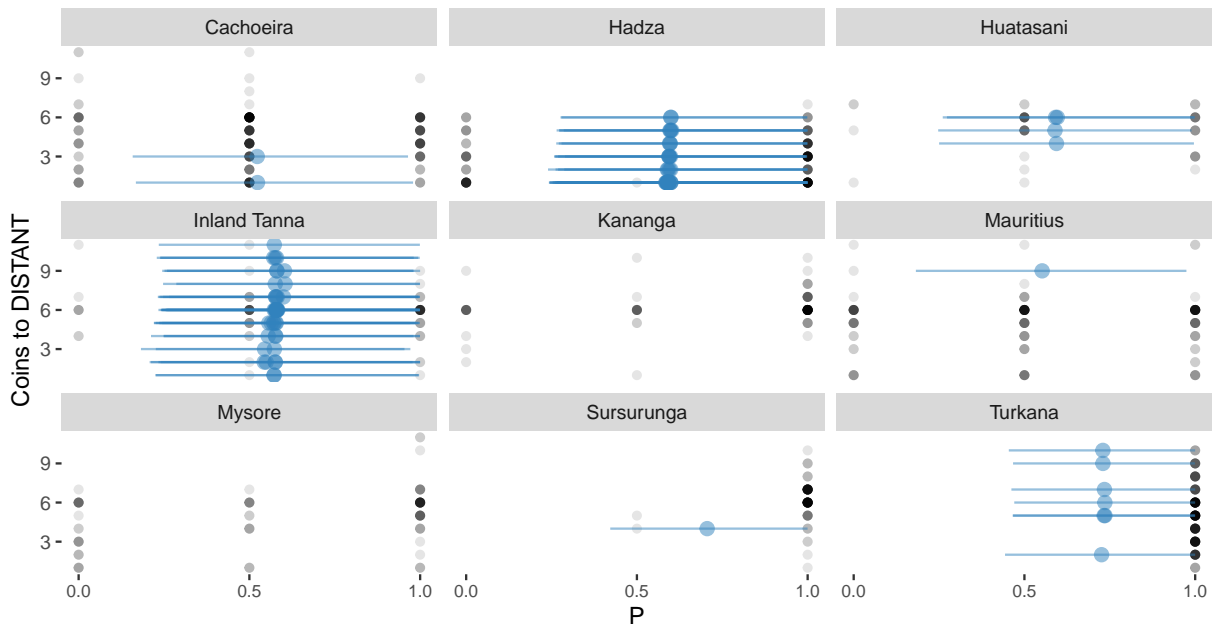
## Missing Data Imputation

Visualizing observed vs. **imputed** values



## Missing Data Imputation

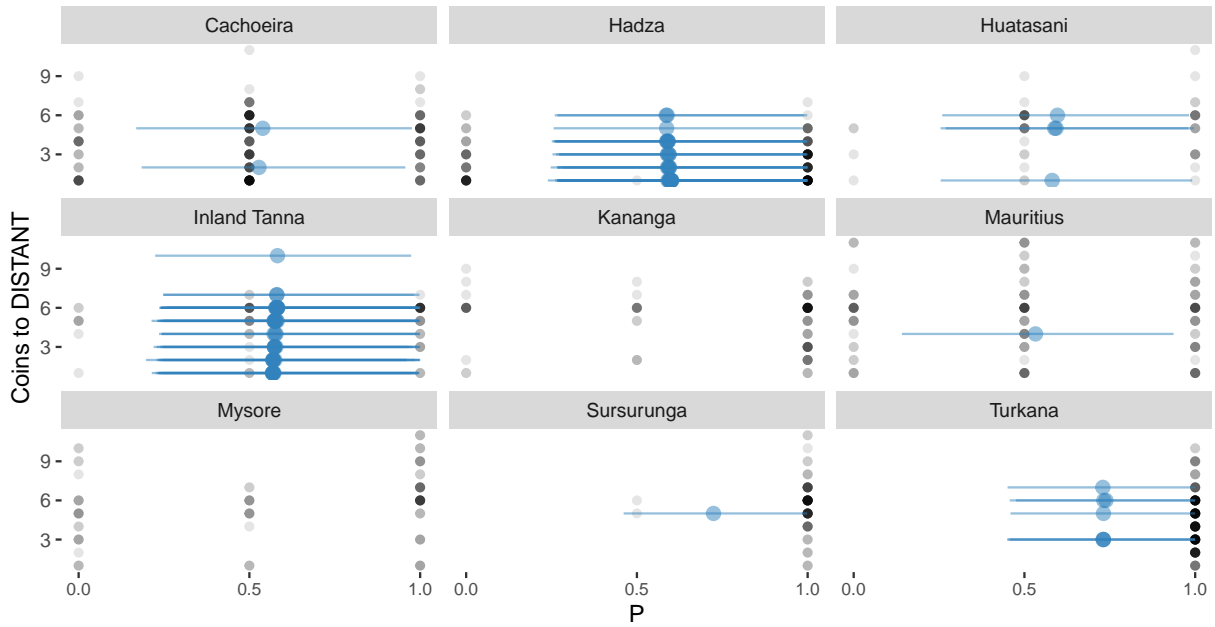
Visualizing observed vs. **imputed** values





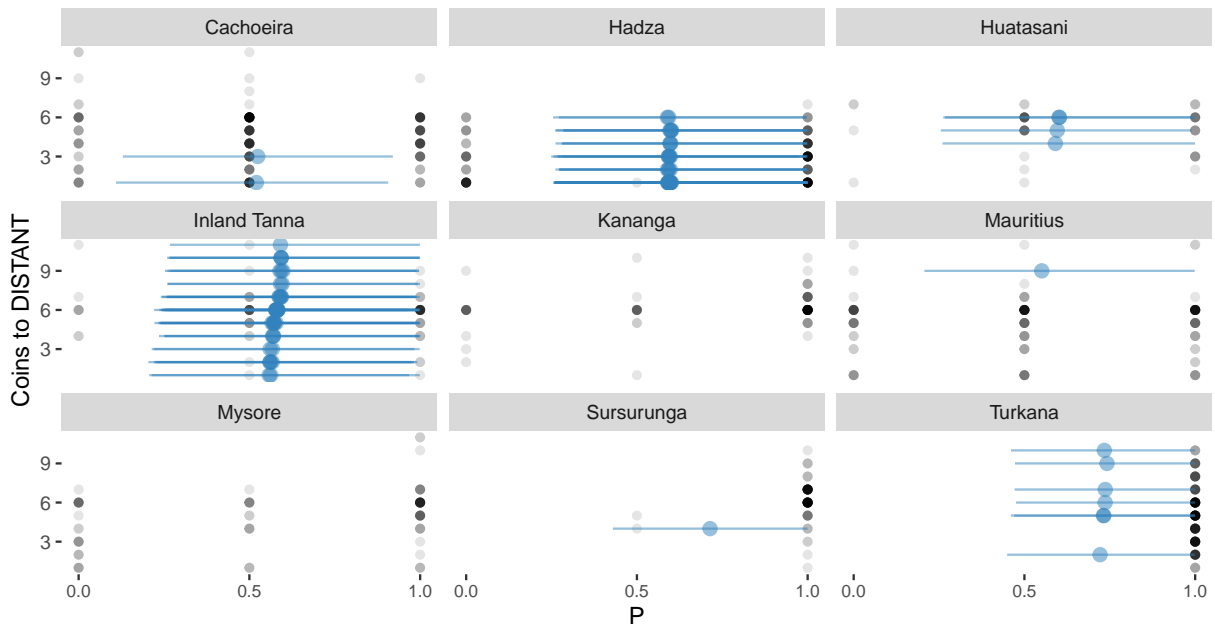
## Missing Data Imputation

Visualizing observed vs. **imputed** values



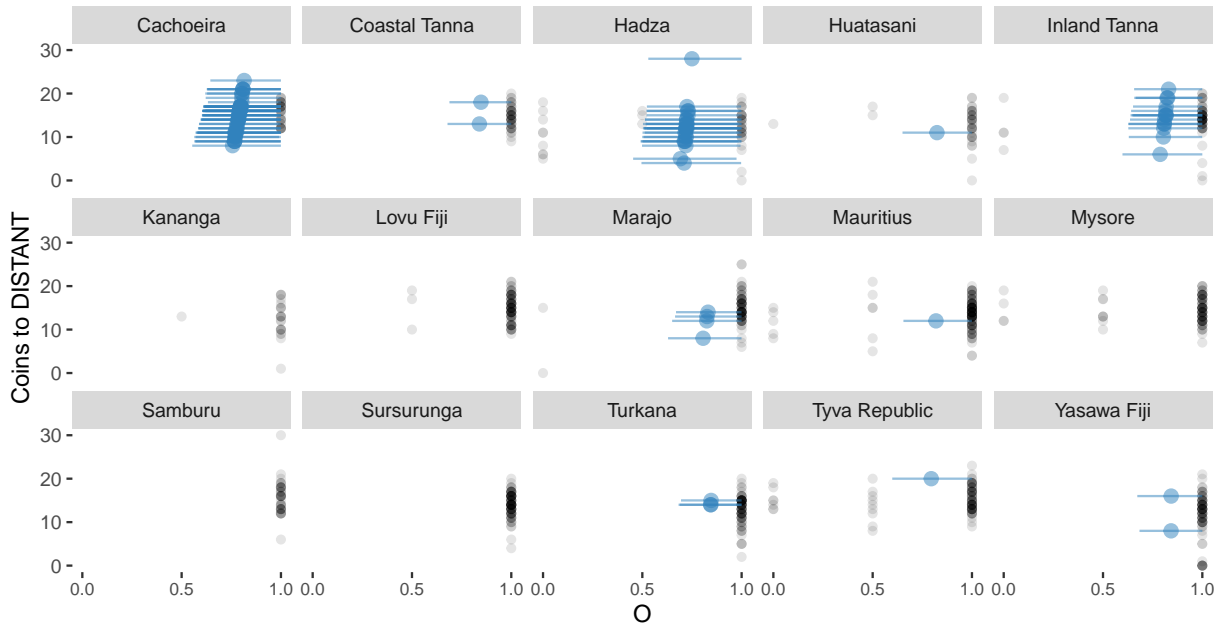
## Missing Data Imputation

Visualizing observed vs. **imputed** values



## Missing Data Imputation

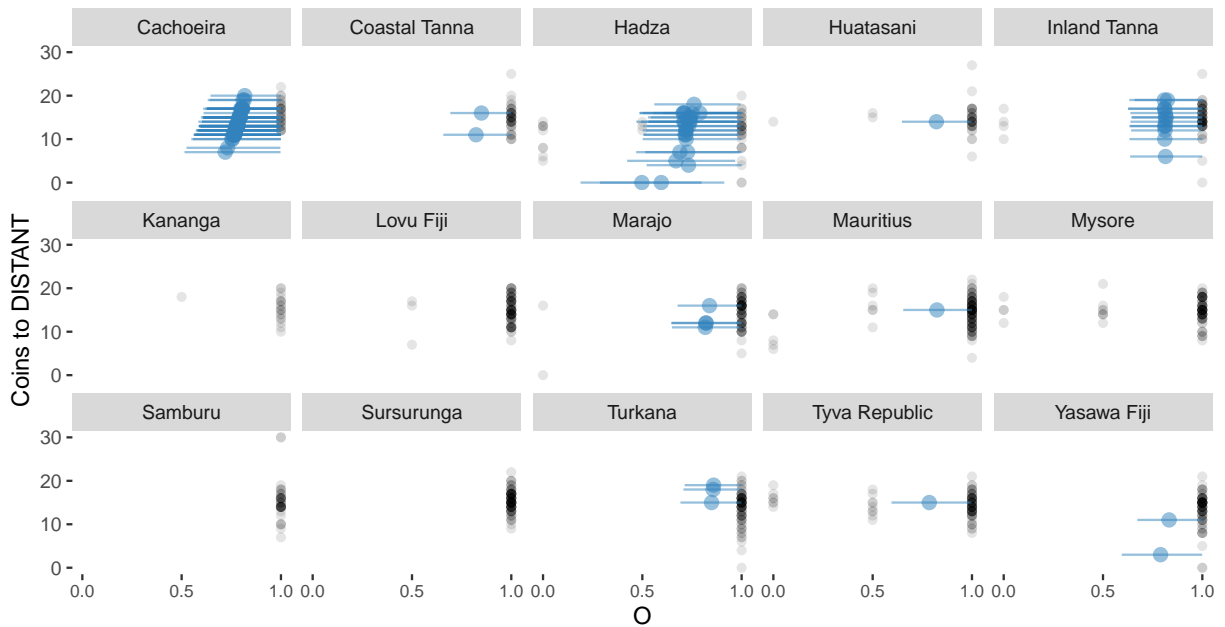
Visualizing observed vs. **imputed** values



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## Missing Data Imputation

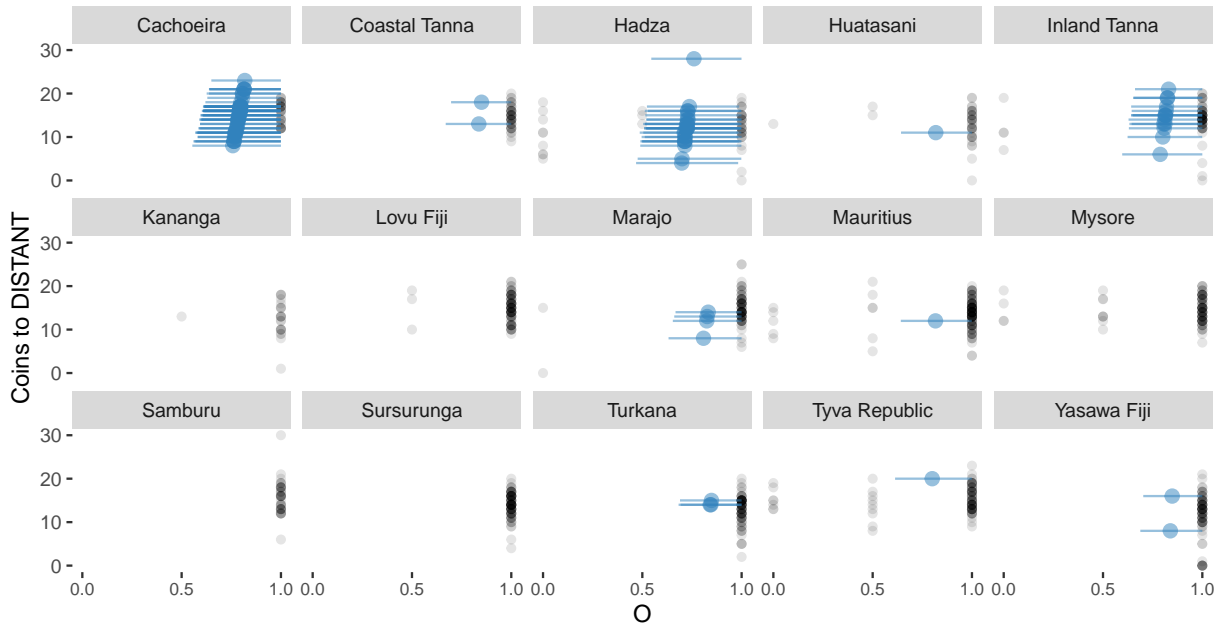
Visualizing observed vs. **imputed** values



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## Missing Data Imputation

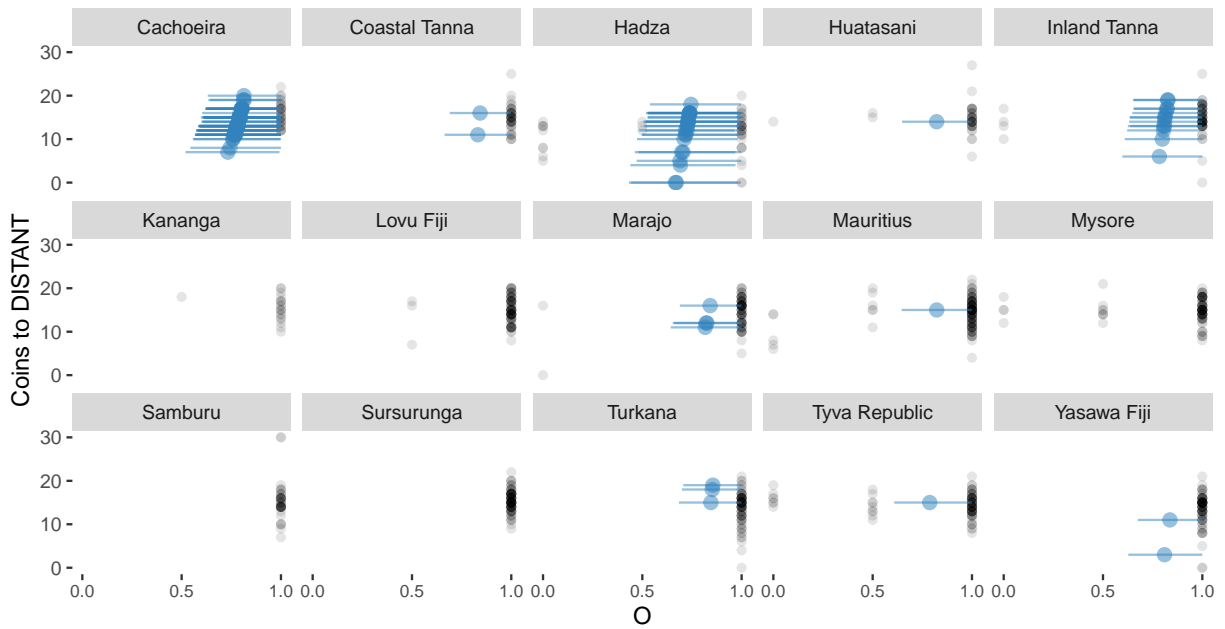
Visualizing observed vs. **imputed** values



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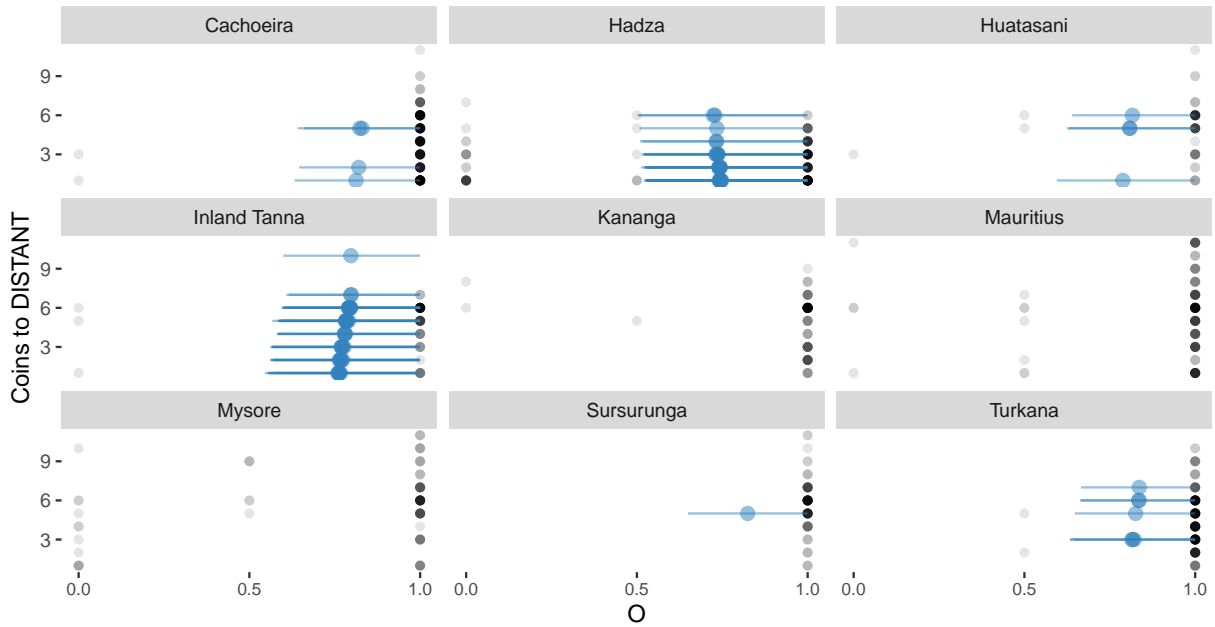
Visualizing observed vs. **imputed** values



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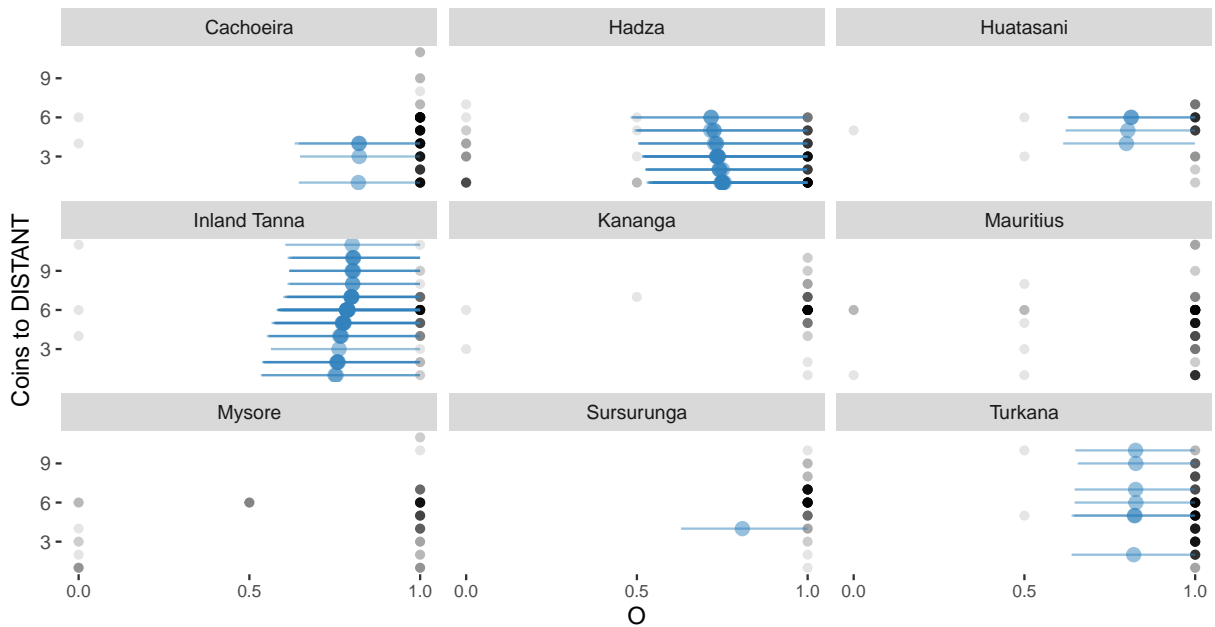
Visualizing observed vs. **imputed** values



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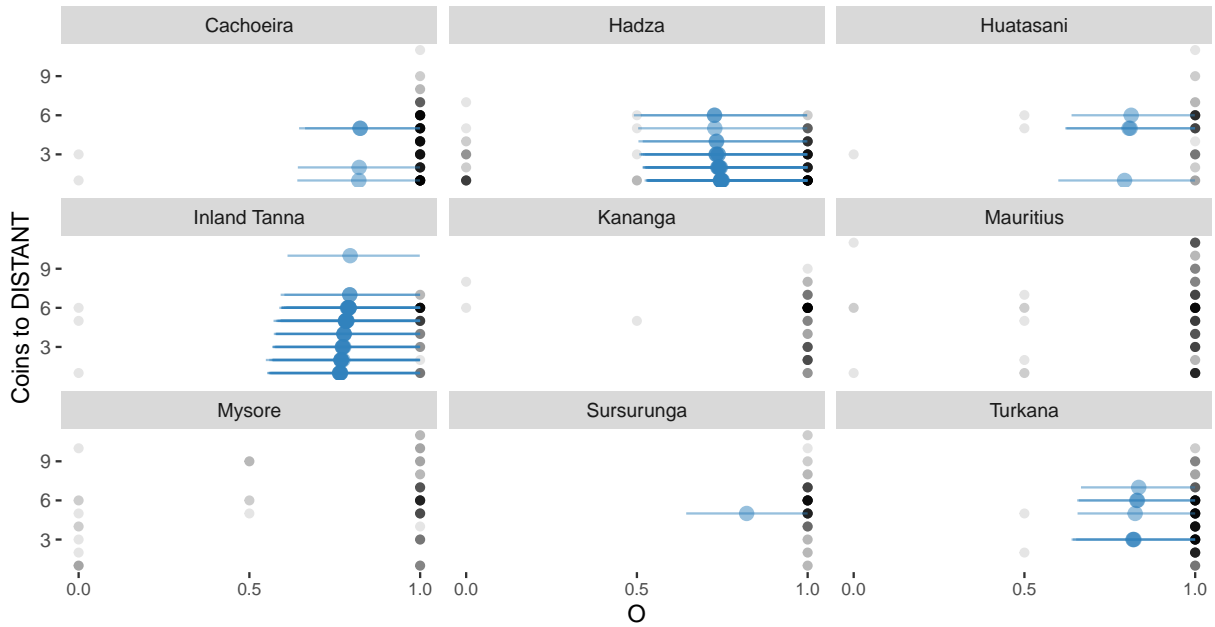
Visualizing observed vs. **imputed** values



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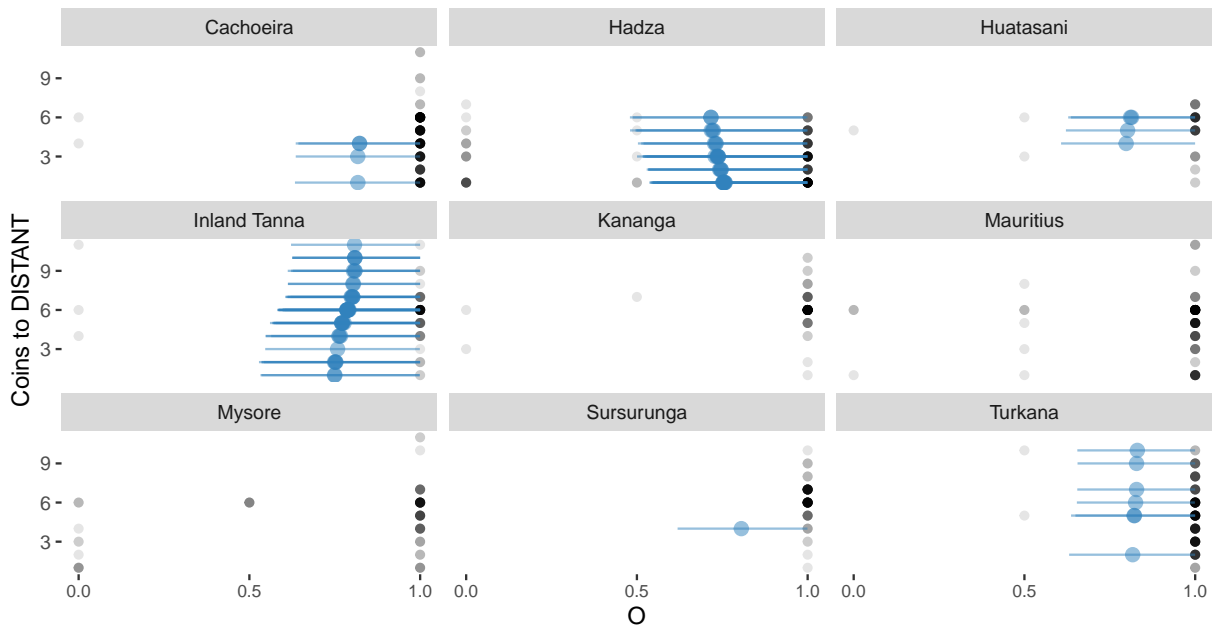
Visualizing observed vs. **imputed** values



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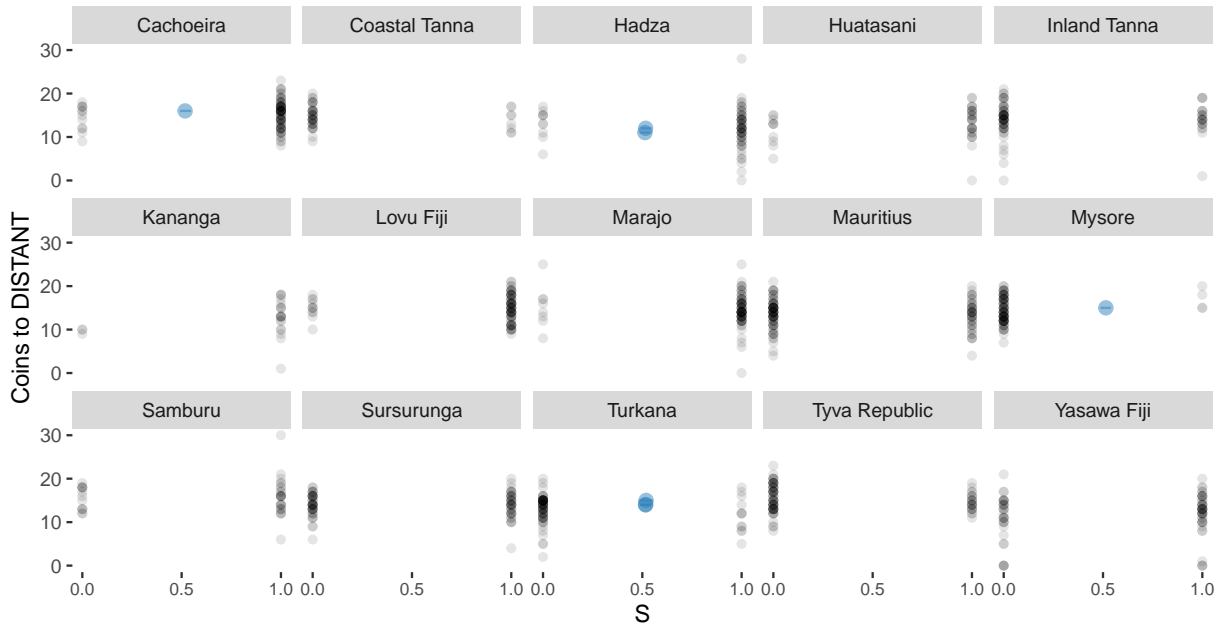
Visualizing observed vs. **imputed** values



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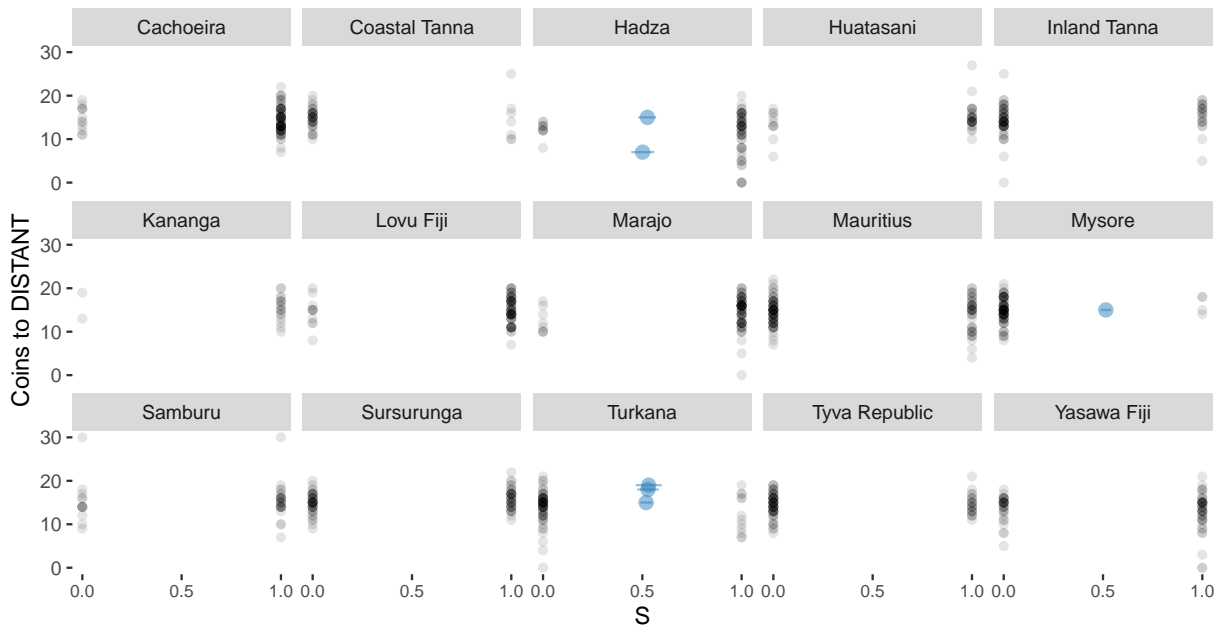
Visualizing observed vs. **imputed** values



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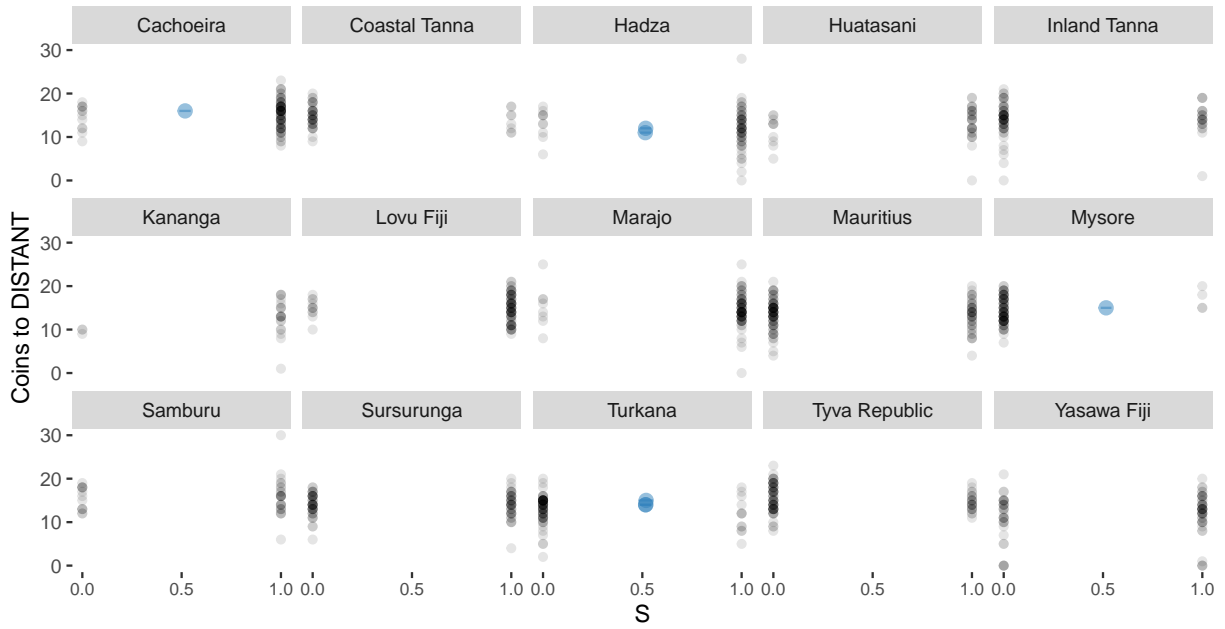
Visualizing observed vs. **imputed** values



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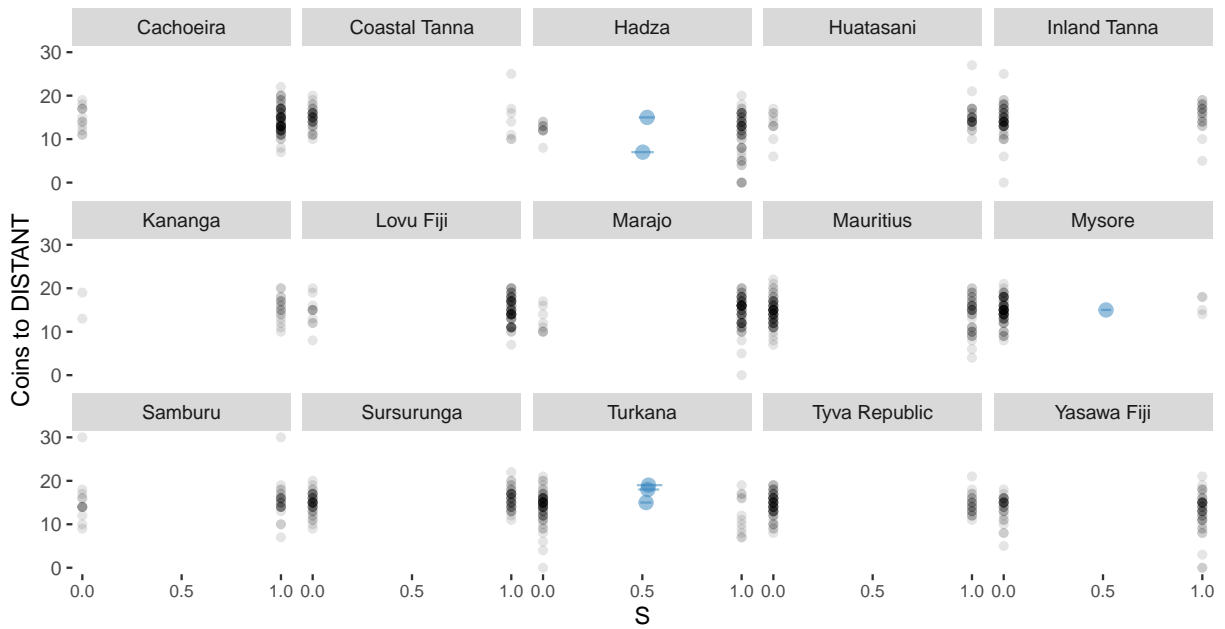
Visualizing observed vs. **imputed** values



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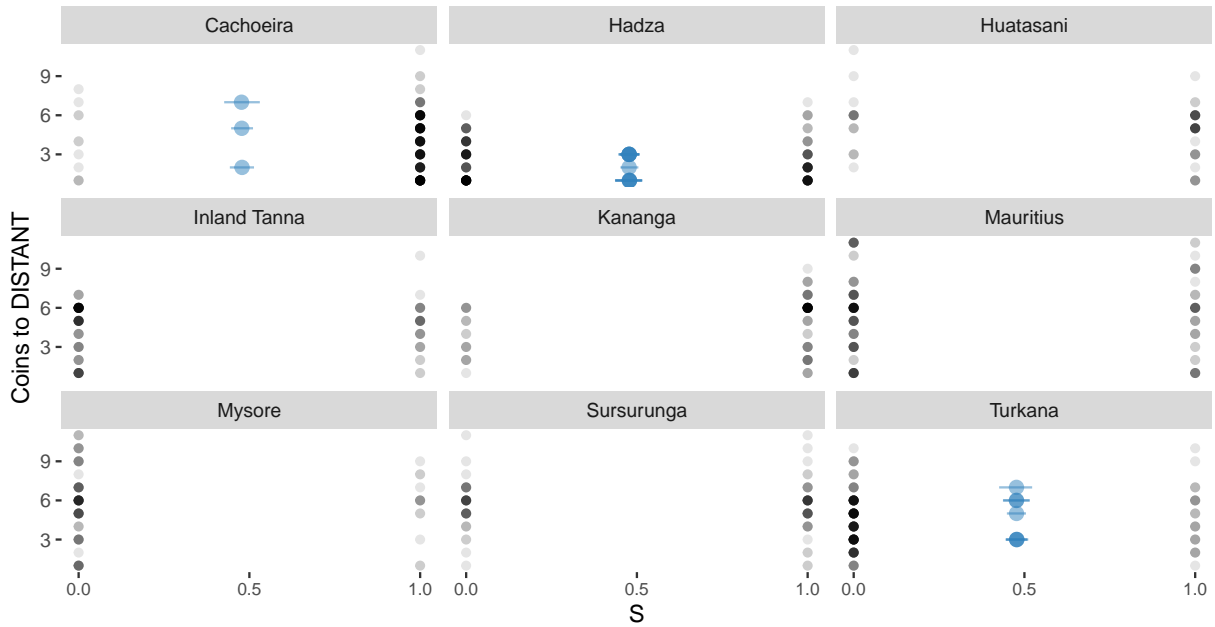
Visualizing observed vs. **imputed** values



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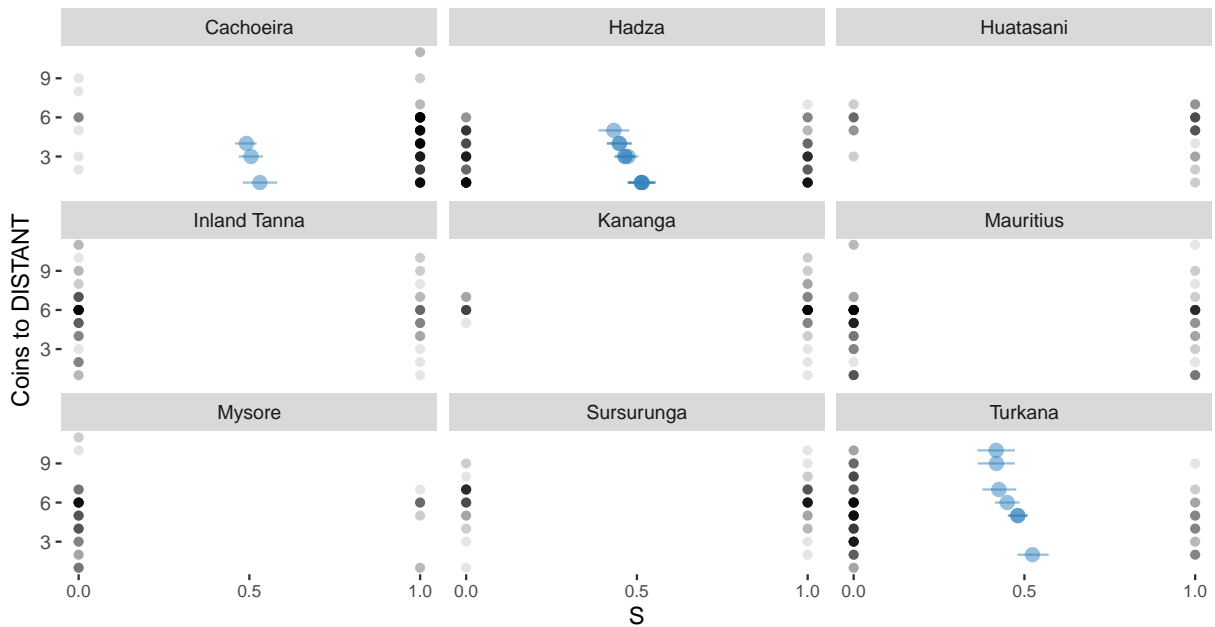
Visualizing observed vs. **imputed** values



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Visualizing observed vs. **imputed** values

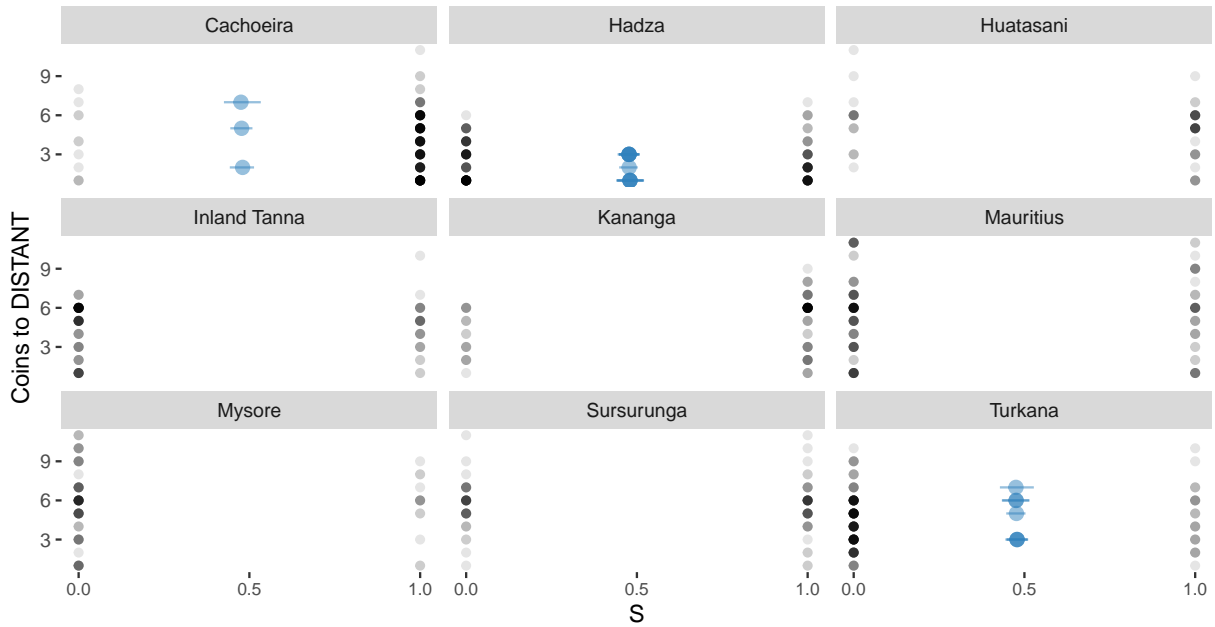


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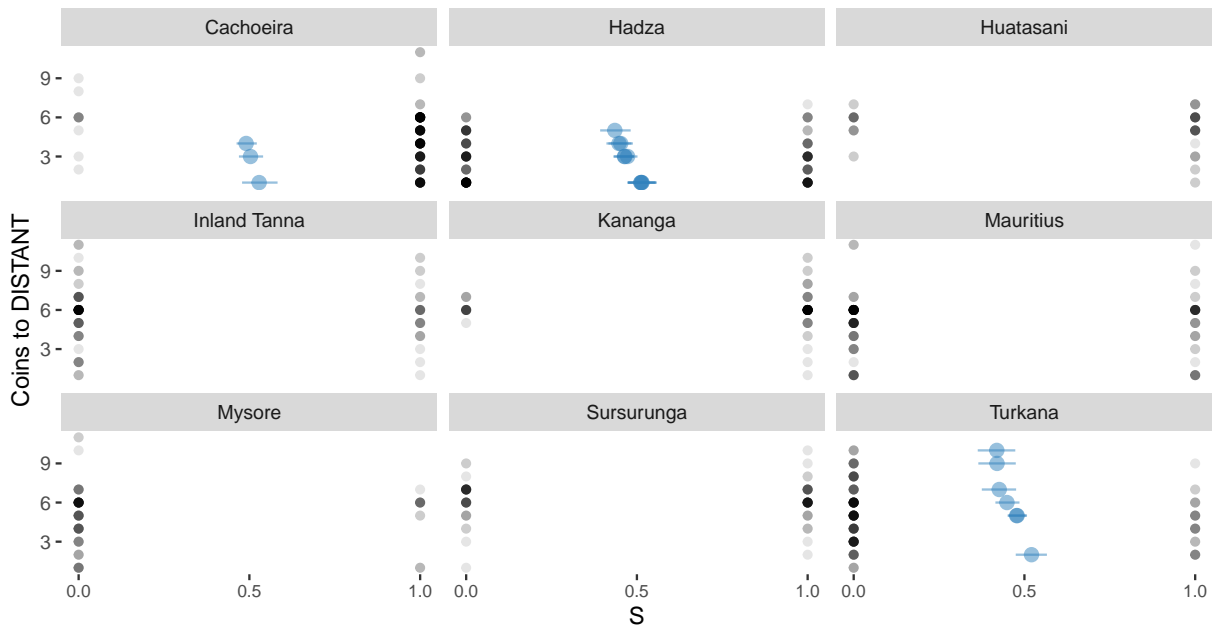
Visualizing observed vs. **imputed** values



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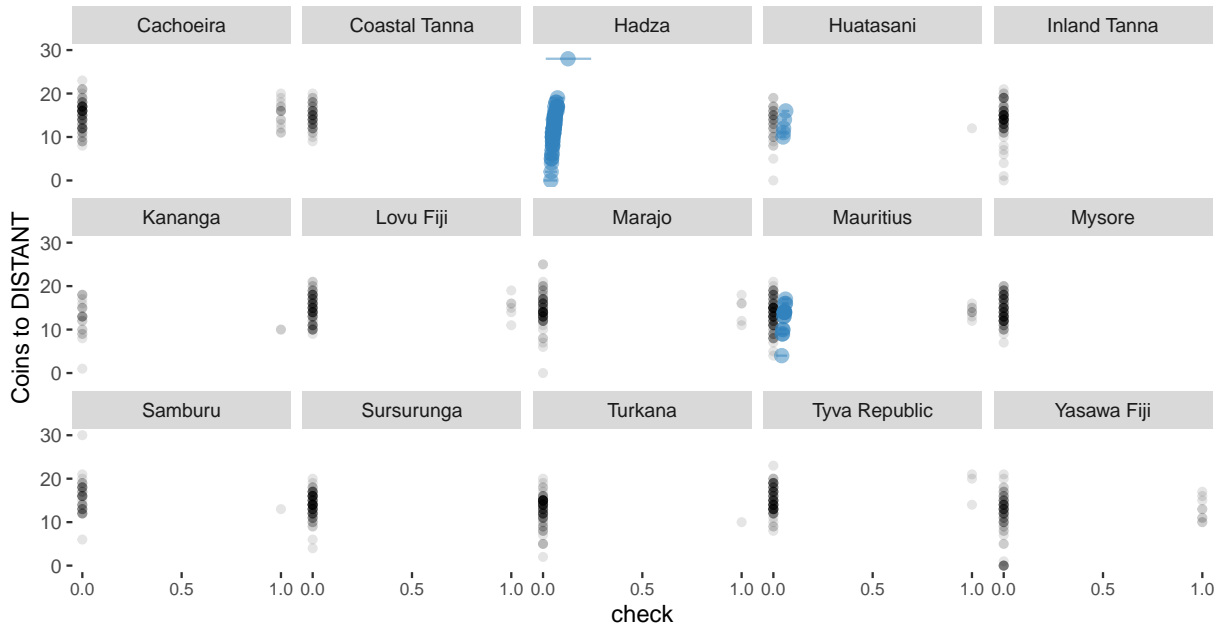
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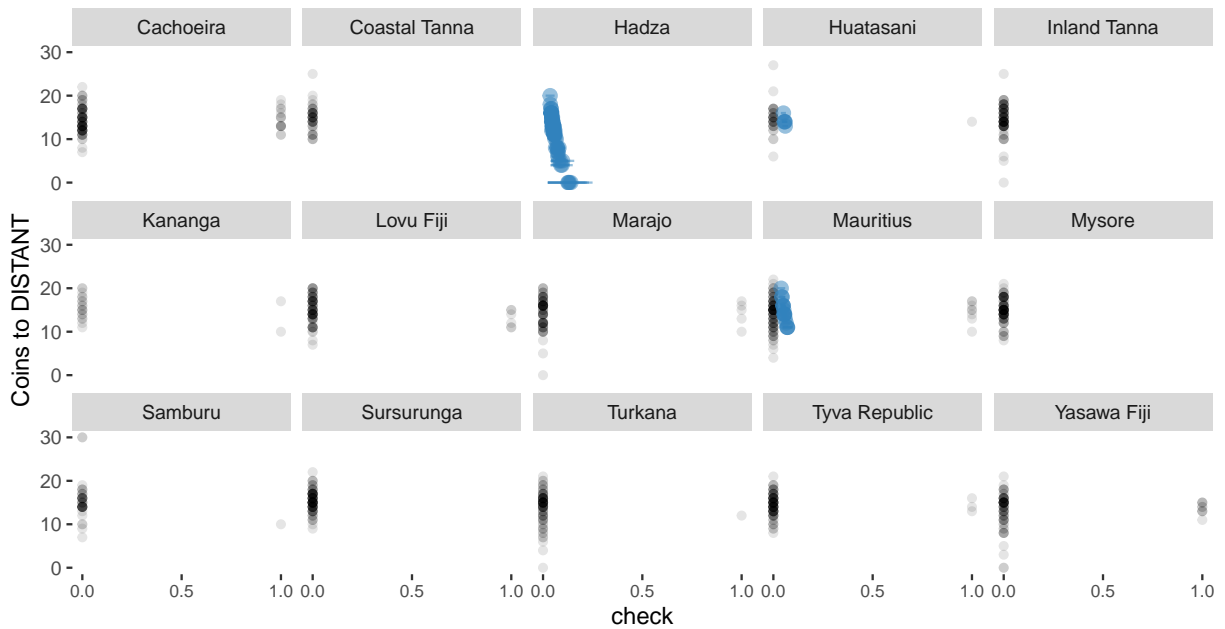
## Missing Data Imputation

Visualizing observed vs. **imputed** values



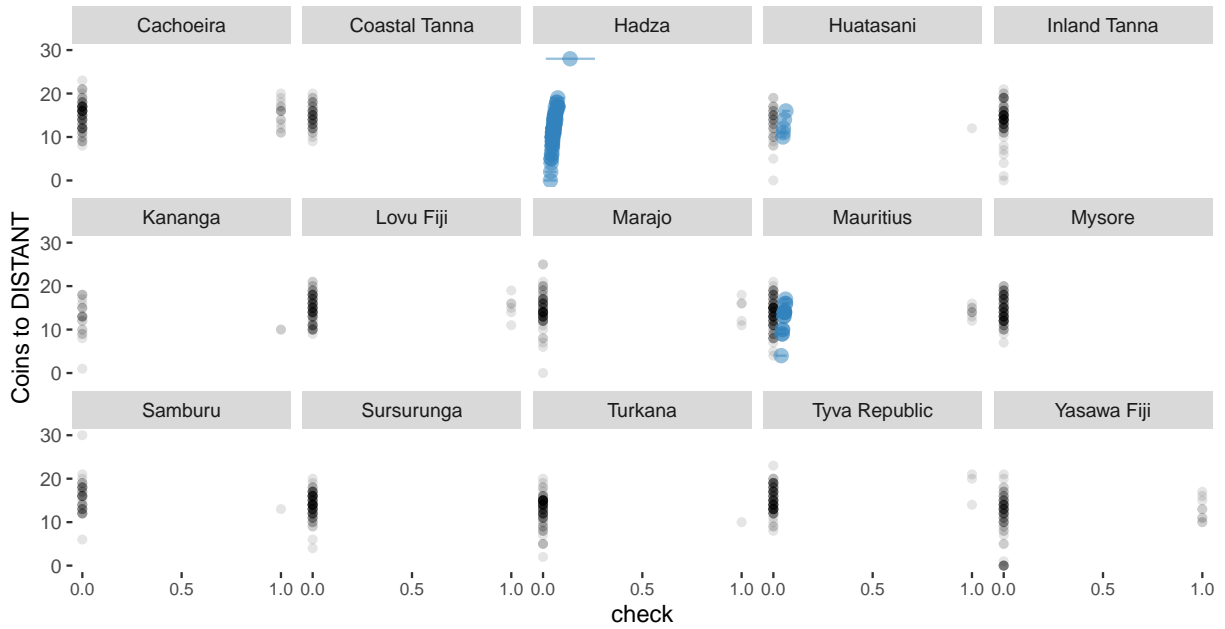
## Missing Data Imputation

Visualizing observed vs. **imputed** values



## Missing Data Imputation

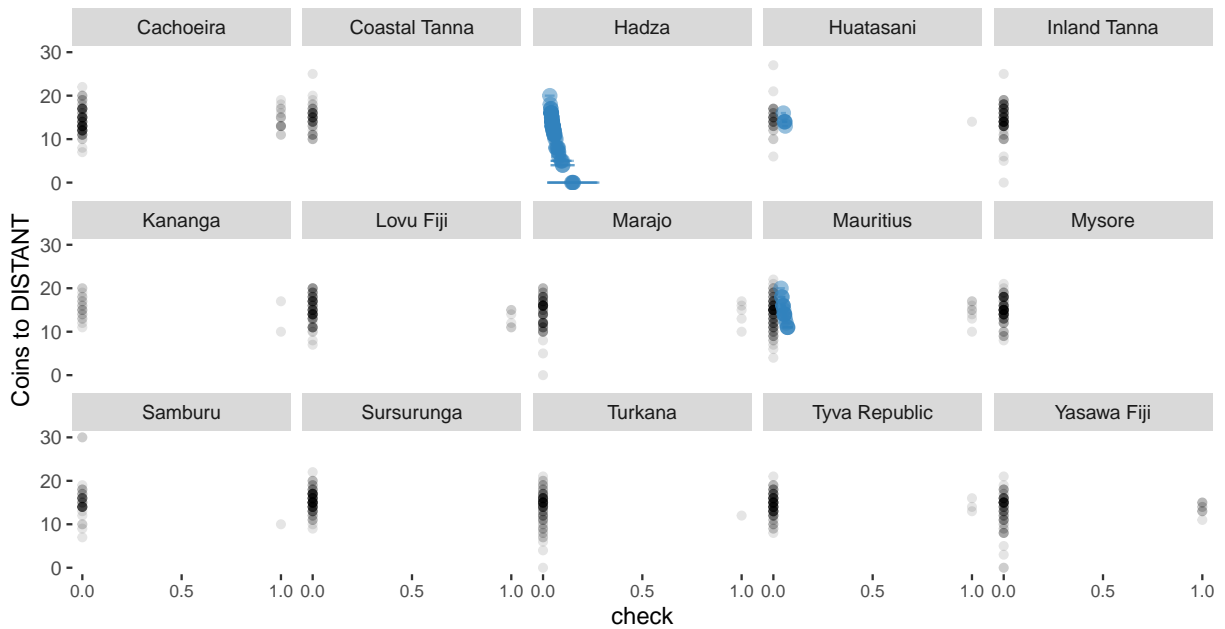
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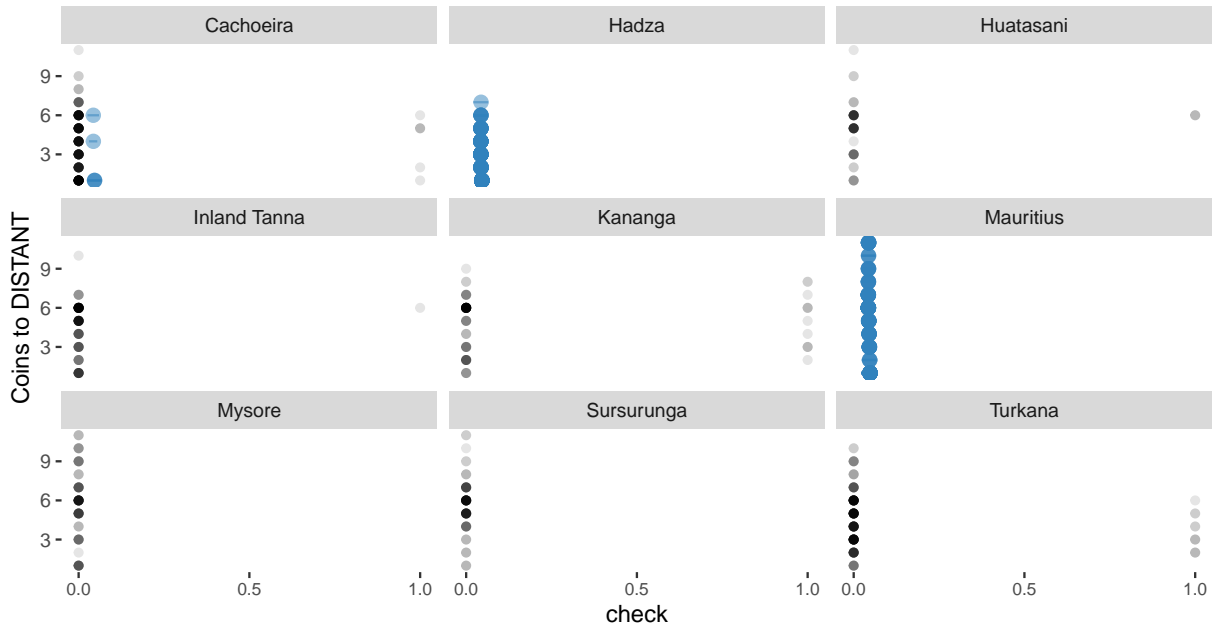
Visualizing observed vs. **imputed** values



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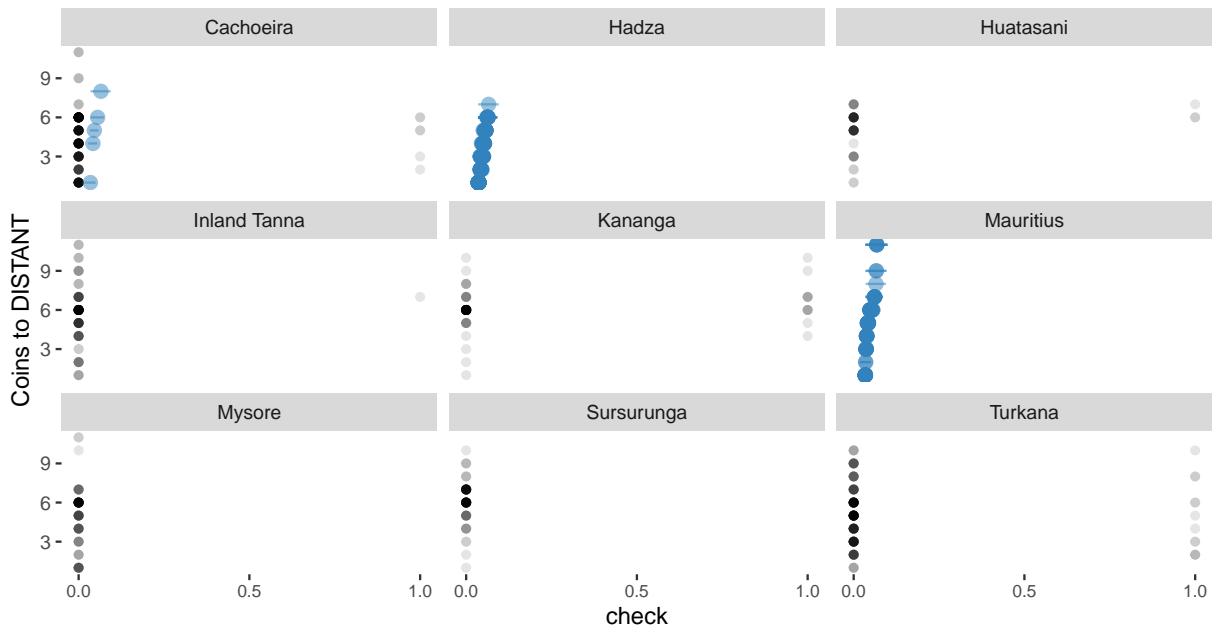
Visualizing **observed** vs. **imputed** values



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## Missing Data Imputation

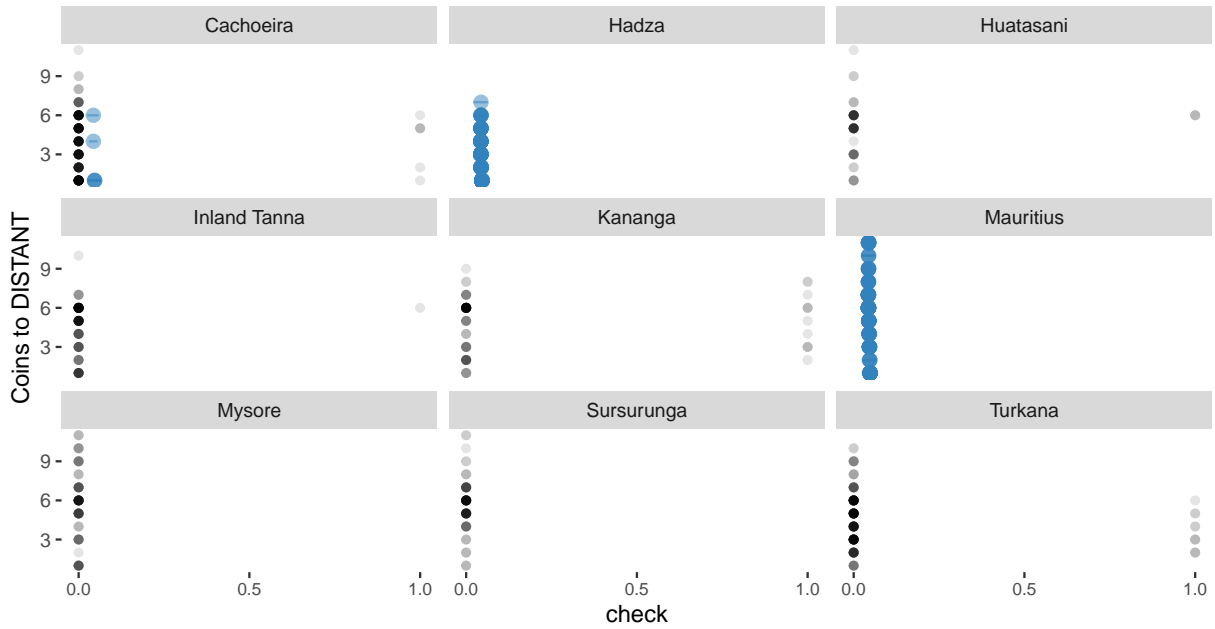
Visualizing **observed** vs. **imputed** values



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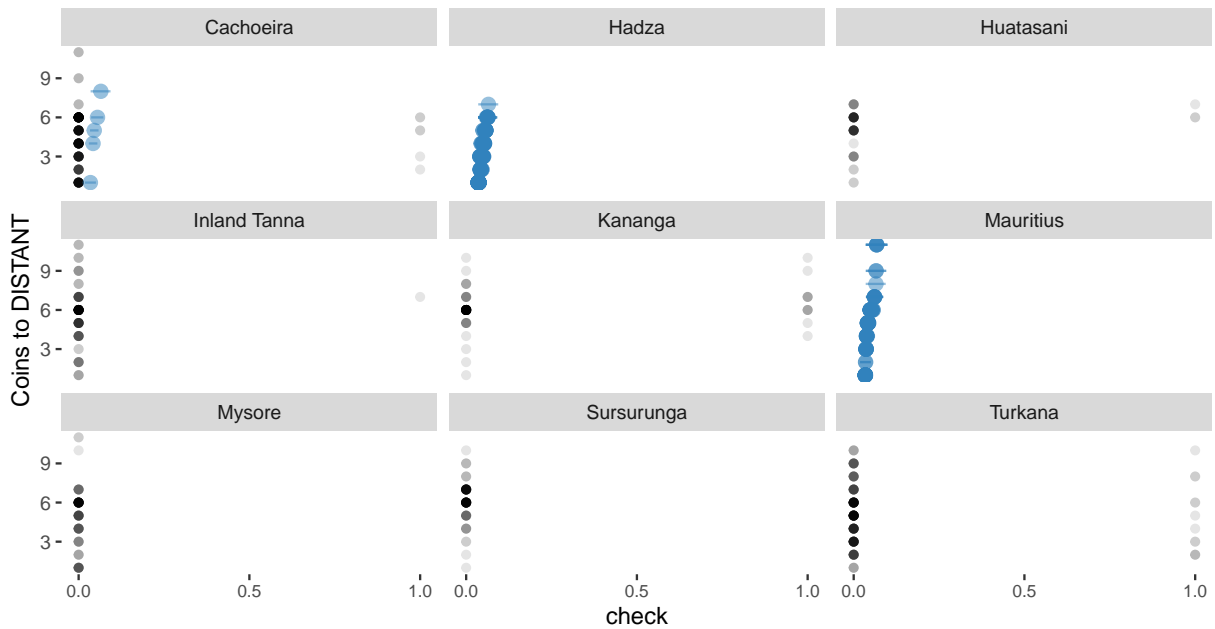
Visualizing **observed** vs. **imputed** values



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## Missing Data Imputation

Visualizing **observed** vs. **imputed** values



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## R packages

We used R version 4.1.2 (R Core Team 2021) and the following R packages: `abind` v. 1.4.5 (Plate and Heiberger 2016), `arrayhelpers` v. 1.1.0 (Beleites 2020), `backports` v. 1.4.1 (Lang and R Core Team 2021), `base64enc` v. 0.1.3 (Urbanek 2015), `bayesplot` v. 1.8.1 (Gabry et al. 2019; Gabry and Mahr 2021), `bdsmatrix` v. 1.3.6 (Therneau 2022), `brio` v. 1.1.3 (Hester and Csárdi 2021), `bslib` v. 0.3.1 (Sievert and Cheng 2021a), `cachem` v. 1.0.6 (Chang 2021a), `callr` v. 3.7.0 (Csárdi and Chang 2021a), `checkmate` v. 2.0.0 (Lang 2017), `coda` v. 0.19.4 (Plummer et al. 2006), `colorspace` v. 2.0.3 (Zeileis, Hornik, and Murrell 2009; Stauffer et al. 2009; Zeileis et al. 2020), `commonmark` v. 1.7 (Ooms 2018), `cpp11` v. 0.4.2 (Hester and François 2021), `curl` v. 4.3.2 (Ooms 2021), `data.table` v. 1.14.2 (Dowle and Srinivasan 2021), `desc` v. 1.4.0 (Csárdi, Müller, and Hester 2021), `diffobj` v. 0.3.5 (Gaslam 2021), `digest` v. 0.6.29 (Antoine Lucas et al. 2021), `distributional` v. 0.3.0 (O’Hara-Wild, Kay, and Hayes 2022), `ellipsis` v. 0.3.2 (H. Wickham 2021a), `evaluate` v. 0.15 (H. Wickham and Xie 2022), `fansi` v. 1.0.2 (Gaslam 2022), `farver` v. 2.1.0 (Pedersen, Nicolae, and François 2021), `fastmap` v. 1.1.0 (Chang 2021b), `finalfit` v. 1.0.6 (Harrison, Drake, and Ots 2023), `fs` v. 1.5.2 (Hester, Wickham, and Csárdi 2021), `generics` v. 0.1.2 (H. Wickham, Kuhn, and Vaughan 2022), `GGally` v. 2.1.2 (Schloerke et al. 2021), `ggdist` v. 3.1.1 (Kay 2022a), `ggridges` v. 0.5.3 (Wilke 2021), `ggtext` v. 0.1.1 (Wilke 2020a), `glue` v. 1.6.1 (Hester and Bryan 2022), `grateful` v. 0.1.11 (Rodríguez-Sánchez, Jackson, and Hutchins 2022), `gridExtra` v. 2.3 (Auguie 2017), `gridtext` v. 0.1.4 (Wilke 2020b), `gtable` v. 0.3.0 (H. Wickham and Pedersen 2019), `HDInterval` v. 0.2.2 (Meredith and Kruschke 2020), `highr` v. 0.9 (Xie and Qiu 2021), `htmltools` v. 0.5.2 (Cheng et al. 2021), `isoband` v. 0.2.5 (Wilke and Pedersen 2021), `jpeg` v. 0.1.9 (Urbanek 2021), `jquerylib` v. 0.1.4 (Sievert and Cheng 2021b), `knitr` v. 1.39 (Xie 2014, 2015, 2022a), `labeling` v. 0.4.2 (Justin Talbot 2020), `lifecycle` v. 1.0.1 (Henry and Wickham 2021), `lme4` v. 1.1.28 (Bates et al. 2015), `loo` v. 2.4.1 (Vehtari, Gelman, and Gabry 2017; Yao et al. 2017; Vehtari et al. 2020), `markdown` v. 1.1 (Allaire et al. 2019), `matrixStats` v. 0.61.0 (Bengtsson 2021), `memoise` v. 2.0.1 (H. Wickham, Hester, et al. 2021), `mice` v. 3.14.0 (van Buuren and Groothuis-Oudshoorn 2011), `mime` v. 0.12 (Xie 2021a), `minqa` v. 1.2.4 (Bates et al. 2014), `munsell` v. 0.5.0 (C. Wickham 2018), `nloptr` v. 2.0.0 (Johnson ?), `numDeriv` v. 2016.8.1.1 (Gilbert and Varadhan 2019), `patchwork` v. 1.1.1 (Pedersen 2020), `pkgconfig` v. 2.0.3 (Csárdi 2019), `pkgload` v. 1.2.4 (H. Wickham, Chang, et al. 2021), `plyr` v. 1.8.6 (H. Wickham 2011b), `png` v. 0.1.7 (Urbanek 2013), `posterior` v. 1.2.0 (Vehtari et al. 2021; Bürkner et al. 2022), `praise` v. 1.0.0 (Csardi and Sorhus 2015), `prettyunits` v. 1.1.1 (Csardi 2020), `pROC` v. 1.18.0 (Robin et al. 2011), `processx` v. 3.5.2 (Csárdi and Chang 2021b), `progress` v. 1.2.2 (Csárdi and FitzJohn 2019), `ps` v. 1.6.0 (Loden et al. 2021), `quadprog` v. 1.5.8 (Berwin A. Turlach R port by Andreas Weingessel <Andreas.Weingessel@ci.tuwien.ac.at> Fortran contributions from Cleve Moler dpodi/LINPACK) 2019), `R6` v. 2.5.1 (Chang 2021c), `rappdirs` v. 0.3.3 (Ratnakumar, Mick, and Davis 2021), `RColorBrewer` v. 1.1.2 (Neuwirth 2014), `Rcpp` v. 1.0.8 (Eddelbuettel and François 2011; Eddelbuettel 2013; Eddelbuettel and Balamuta 2018), `RcppEigen` v. 0.3.3.9.1 (Bates and Eddelbuettel 2013), `rematch2` v. 2.1.2 (Csárdi 2020), `renv` v. 0.16.0 (Ushey 2022), `reshape` v. 0.8.9 (H. Wickham 2007a), `reshape2` v. 1.4.4 (H. Wickham 2007b), `rethinking` v. 2.21 (McElreath 2021), `rmarkdown` v. 2.14 (Xie, Allaire, and Golemund 2018; Xie, Dervieux, and Riederer 2020; Allaire et al. 2022), `rprojroot` v. 2.0.2 (Müller 2020), `sass` v. 0.4.1 (Cheng et al. 2022), `scales` v. 1.1.1 (H. Wickham and Seidel 2020), `stringi` v. 1.7.6 (Gagolewski 2021a, 2021b), `svUnit` v. 1.0.6 (Grosjean 2021), `tensorA` v. 0.36.2 (van den Boogaart 2020), `testthat` v. 3.1.2 (H. Wickham 2011a), `tidybayes` v. 3.0.2 (Kay 2022b), `tidyselect` v. 1.1.2 (Henry and Wickham 2022), `tidyverse` v. 1.3.2 (H. Wickham et al. 2019), `tinytex` v. 0.38 (Xie 2019, 2022b), `utf8` v. 1.2.2 (Perry 2021), `vctrs` v. 0.3.8 (H. Wickham, Henry, and Vaughan 2021), `viridisLite` v. 0.4.0 (Garnier et al. 2021), `waldo` v. 0.3.1 (H. Wickham 2021b), `withr` v. 2.5.0 (Hester et al. 2022), `xfun` v. 0.29 (Xie 2021b), `yaml` v. 2.3.5 (Garbett et al. 2022).

## References

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