## Highlights

A study on multicriteria ABC classification with analytical hierarchy process

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- generative method for force consistency of pairwise comparisons matrix;
- importance of the correct balance of weights assigned to the criteria;
- evidence of the importance of ABC multicriteria clssf for forecasting.

# A study on multicriteria ABC classification with analytical hierarchy process

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#### Abstract

Multicriteria classification is usually very important to the decision-making in manufacturing management process. For such classification, the attribution of weights to the criteria strongly influences the coherence of the results found. Saaty's Analytic Hierarchy Process (AHP) is an important method for assigning weights to multiple criteria. AHP's logic is not complicated at all but, since matrices of pairwise comparisons of criteria are usually generated manually and based only on some employee know-how, there is a huge complexity on generating a consistent pairwise matrix. Especially when many criteria are used. This paper presents a constructive algorithm that can be used to adjust inconsistent matrices, forcing such matrices to have a better consistency rate. We tested this algorithm by applying the AHP method, for multicriteria ABC classification, to companies in two sectors. As a result we

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observed that the algorithm can adjust the pairwise matrices in just a few seconds, avoiding the manual work that would be done in weeks, therefore showing that it is an important resource for applying the AHP method. We also present in this paper an analysis of the importance of the attribution of the weights to the criteria and show how the multicriteria classification may influence the decision on the choice of the appropriate forecasting method. Keywords: multi-product batch, processing time maximization, mathematical model, analytical solution, COPSolver, LINGO

#### 1. Introduction

### 2. Algorithm for forcing pairwise matrix consistency

The algorithm is not represented correctly.

Changes will be made during the preparation of the article according to the module of software COPSolver: library for solving classification problems.

```
Algorithm 1 function consistencyRate()
```

```
Require: [a_{ij}]_{i,j=1}^n, RI[x]_{x=1}^{10}

\lambda_{max} = mainEigenvalue([a_{ij}]_{i,j=1}^n)^{-1}

CI = (\lambda_{max} - n)/(n-1)

CR \leftarrow CI/RI[n]

return CR
```

## $\overline{\textbf{Algorithm 2} \text{ function } constructivelyForceConsistency([a_{ij}]_{i,j=1}^n)}$

#### 2.1. Constructive algorithm

### 3. Tests and results

#### 4. Conclusions and suggestions for future works

In this paper we presented ...

### 5. CRediT authorship contribution statement

T.B. Fraga: Conceptualization, Project administration, Supervision, Software, Methodology, Validation, Formal analysis, Writing – original draft, Writing – review & editing.

### **Algorithm 3** function $forceConsistency([a_{ij}]_{i,j=1}^k)$

```
Require: [a_{ij}]_{i,j=1}^n \mid consistencyRate([a_{ij}]_{i,j=1}^{n-1}) \leq 0.1
Ensure: consistencyRate([a_{ij}]_{i,j=1}^n) \le 0.1
   CR \leftarrow consistencyRate([a_{ij}]_{i,j=1}^n)
   for j \leq n-2 do
       for j + 1 \le k \le n - 1 do
            g \leftarrow 0
            s \leftarrow 0
            if a_{nj} > a_{nk} and a_{jk} \leq 1 then
                 g \leftarrow j
            else if a_{nj} < a_{nk} and a_{jk} \ge 1 then
                 g \leftarrow k
                 s \leftarrow j
            end if
            if g \neq 0 then
                 ([a_{ij}]_{i,j=1}^n, CR) \leftarrow reduce([a_{ij}]_{i,j=1}^n, g, s)
                if CR \ge 0.1 then
                     ([a_{ij}]_{i,j=1}^n, CR) \leftarrow encrease([a_{ij}]_{i,j=1}^n, g, s)
                 end if
            end if
            if CR \leq 0.1 then
                 break for
            end if
       end for
       if CR \leq 0.1 then
            break for
       end if
   end for
   return ([a_{ij}]_{i,j=1}^n, CR)
```

## Algorithm 4 function $reduce([a_{ij}]_{i,j=1}^n, g, s)$

```
Require: g, s < n; [a_{ij}]_{i,j=1}^n
   while a_{ng} > a_{ns} do
        a_{ng} \leftarrow a_{ng}^{--}
        a_{gn} \leftarrow a_{gn}^{++}
        aux_{CR} = consistencyRate([a_{ij}]_{i,j=1}^n)
        if aux_{CR} < CR then
             CR = aux_{CR}
             if CR \leq 0.1 then
                  break
             end if
        else
             a_{ng} \leftarrow a_{ng}^{++}
             a_{gn} \leftarrow a_{gn}^{--}
             break
        end if
   end while
   return ([a_{ij}]_{i,j=1}^n, CR)
```

#### 6. Acknowledgments

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```
Algorithm 5 function encrease([a_{ij}]_{i,j=1}^n, g, s)
Require: g, s < n; [a_{ij}]_{i,j=1}^n
   while a_{ng} > a_{ns} do
       a_{ns} \leftarrow a_{ns}^{++}
       a_{sn} \leftarrow a_{sn}^{--}
       aux_{CR} = consistencyRate([a_{ij}]_{i,j=1}^n)
       if aux_{CR} < CR then
            CR = aux_{CR}
            if CR \leq 0.1 then
                 break
            end if
       else
            a_{ns} \leftarrow a_{ns}^{--}
            a_{sn} \leftarrow a_{sn}^{+}
            break
       end if
   end while
   return ([b_{ij}]_{i,j=1}^n, CR)
Algorithm 6 function a_{ij}^{++}
                    a_{ij} \in \{1/9, 1/7, 1/5, 1/3, 1, 3, 5, 7, 9\}
Require: a_{ij}
   if a_{ij} \geq 1 and a_{ij} \neq 9 then
       a_{ij} \leftarrow a_{ij} + 2
   else if a_{ij} < 1 then
       a_{ij} \leftarrow 1/(1/a_{ij} - 2)
   end if
   return a_{ij}
Algorithm 7 function a_{ij}^{--}
Require: a_{ij}
                    a_{ij} \in \{1/9, 1/7, 1/5, 1/3, 1, 3, 5, 7, 9\}
   if a_{ij} \geq 3 then
       a_{ij} \leftarrow b_{ij} - 2
   else if a_{ij} \leq 1 and a_{ij} \neq 1/9 then
       a_{ij} \leftarrow 1/(1/a_{ij} + 2)
   end if
   return a_{ij}
```

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