

# Memo

To: Xiaoli Zhang and Mollie Brombaugh

From: Ben Pacheco and Tessa Haws

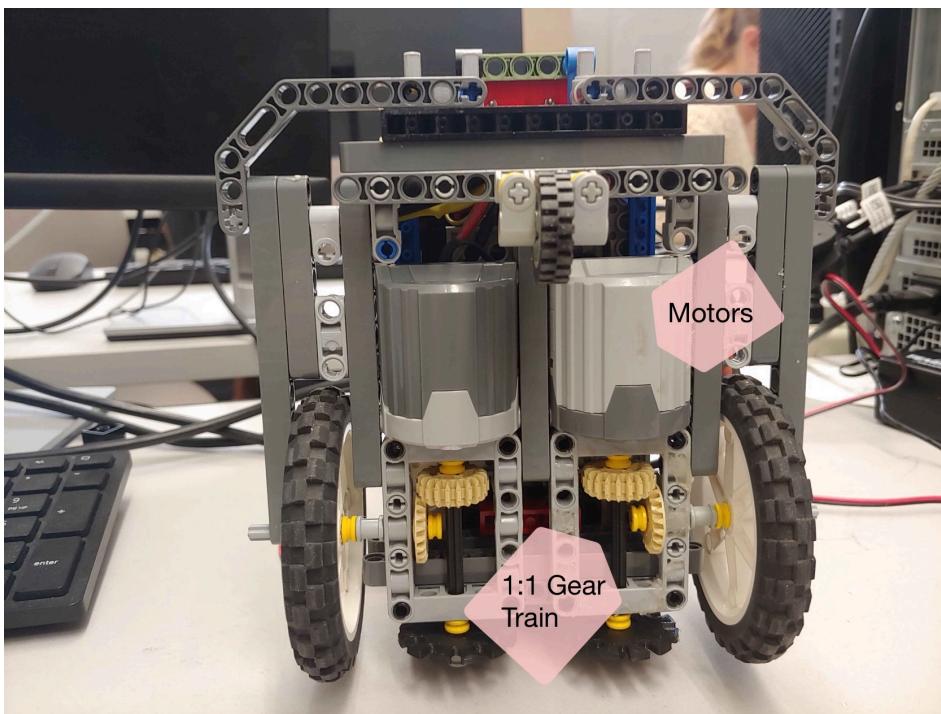
Team #: N-424

Date: November 10, 2024

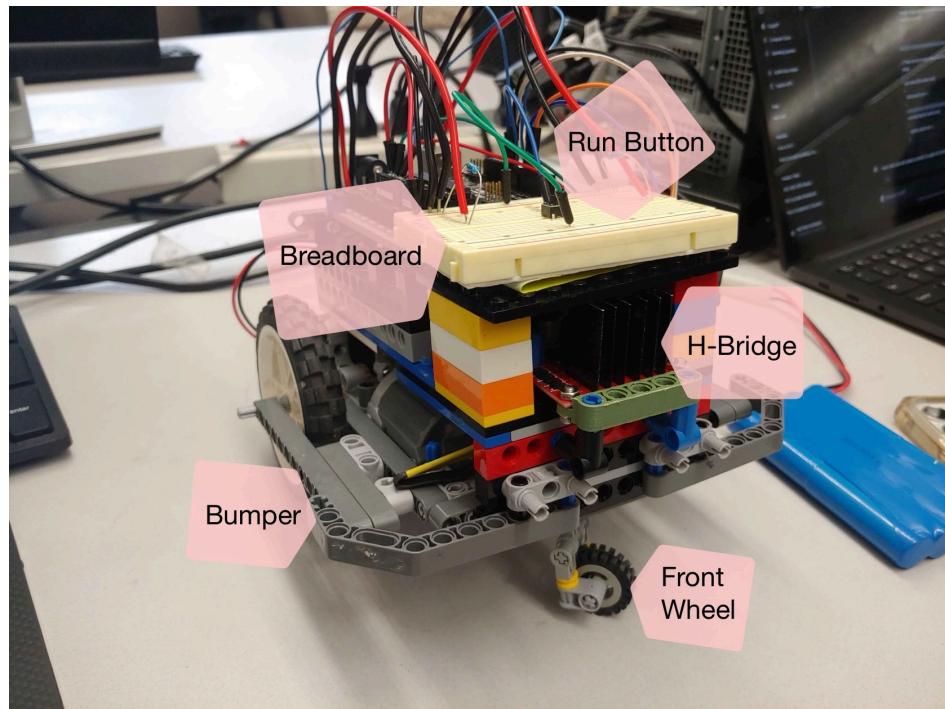
Re: Lab 4: Solving the Maze

## Problem Statement

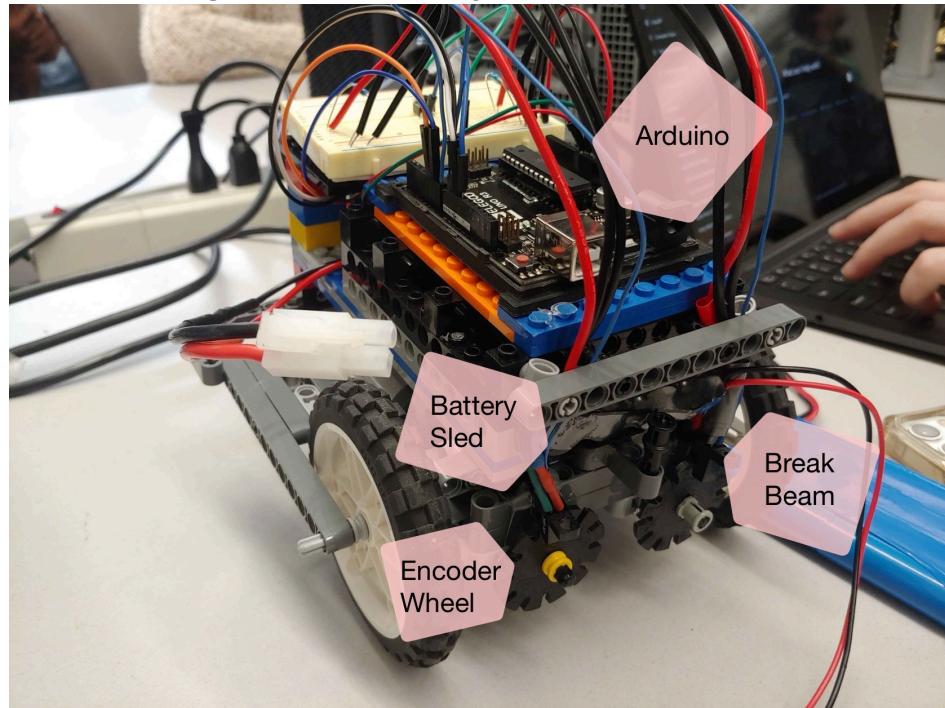
As a group, our task in this lab is to collaboratively develop and implement a strategy for a robot to navigate and solve a maze autonomously. The robot must use distance sensors to detect walls and obstacles, systematically explore the entire maze from start to finish, and log its movements. With this recorded data, we will collectively determine and eliminate unnecessary steps, allowing the robot to retrace the maze in the most direct route possible on a second attempt. This lab requires us to apply our skills in sensor calibration, interfacing with infrared and ultrasonic sensors, and algorithm development. Together, we aim to deepen our understanding of robotic navigation, modular programming, and the iterative process of designing practical solutions for real-world challenges.



**Figure 1.** Labeled image the bottom of the car



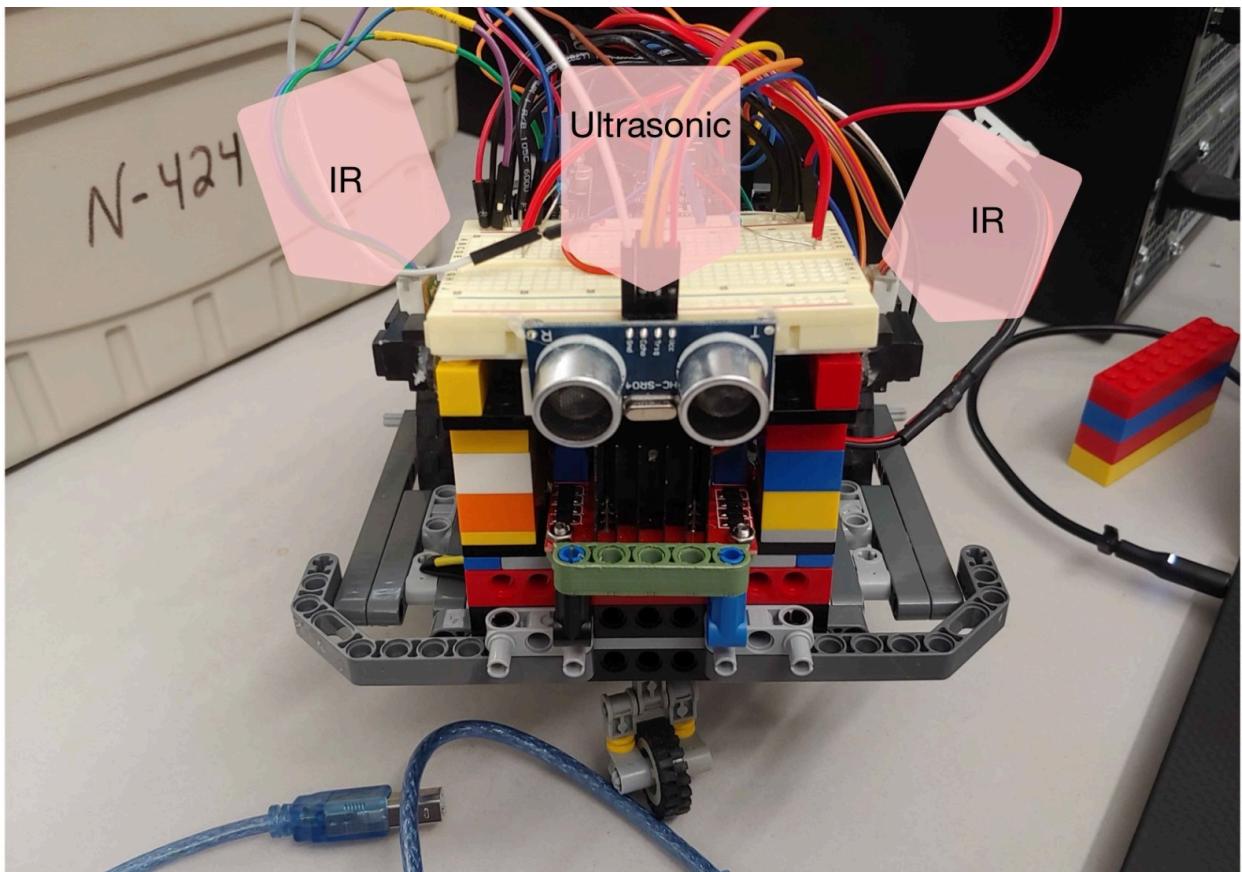
**Figure 2.** Labeled image of the front of the car



**Figure 3.** Labeled image of the back of the car

## Methods

### a. Sensor Configuration and Photo



**Figure 4.** Labeled image of the new sensors

### b. Overall code and testing Description

The first step will be integrating the new sensors into the code. The infrared sensors need to be calibrated, and the ultrasonic sensor library added. New functions will be added to return the readings from each sensor. Using this data, the robot can use the existing control system to move through the maze and use logic to determine the best direction to travel in.

### c. Reading of path

The simplest version of the path reading algorithm will use the sensors to follow a wall on either the left or right side. This is a less efficient algorithm because it will result in the robot finding a lot of dead ends and needing to backtrack. Some basic research shows how competitive maze-solving robots solve their mazes. A popular and more efficient algorithm is called a waterfall algorithm[1]. Veritasium explores this concept in his video on maze solving, showing how a matrix can be constructed to assign a score to each position in the maze based on its distance from the goal position. An example of such a matrix for our maze is shown in Figure 5.

1	2	3	4	5
1	2	3	4	4
1	2	3	3	3
1	2	2	2	2
0	1	1	1	1

**Figure 5.** Example of waterfall solve matrix

Then, when multiple paths are available to the robot, the scores of the respective tiles can be compared, and the robot can take the one that gets it closer to the goal. In cases where the scores are the same, the robot can be instructed to favor the rightmost path. The shape and limited complexity of the maze result in this more complex algorithm putting the robot in the same number of dead ends as the right following method, but it is more applicable to different maze shapes and sizes. A combination of the sensor readings and encoder counts from the wheels will tell us when we have traveled the distance, marking one cube and assigning a direction to each direction in the maze, allowing us to generate coordinates for the current position. Using this information, as we explore the maze, we can append our current coordinates to the end of the history matrix to keep track of the route we have taken.

#### d. Method of eliminating deadends

We have some dead ends included by tracking the entire route we take in exploration. When duplicate coordinates are detected, the robot has visited the same place twice, and a dead end must have occurred. To remove these useless steps before generating our final solve instruction set, we iterate through the coordinate history till we find redundant coordinates with only one coordinate in between; this is the dead end. We can then work outwards from the dead end, pruning each redundant coordinate until the outermost redundant coordinate is found. One of the two outermost redundant coordinates will be kept so the robot still visits the first overlapping square. By iterating through the matrix, all the dead ends can be removed, and the resulting coordinates are the most direct route discovered. From these coordinates, an instruction set can be generated for the robot to execute using our existing control system.

## Results

#### a. Problems you're facing

The constructed robot is having power issues. The Infrared sensors do not consistently read when connected to the battery, resulting in extreme difficulty debugging control logic. No matter what the wall tolerance is set to, the infrared sensors will only detect a wall missing one in five attempts.

## b. Solutions attempted

The first solution attempted was to verify the sensor was consistently emitting light. A phone with a camera that doesn't have an infrared sensor was pointed at the infrared sensor emitter to see emitted light. The first sensor did not emit much light, so it was replaced. This did not solve the problem of the sensor failing to detect missing walls. Next, print statements were used inside the code to print out readings while on a test stand to check control logic. In this configuration, the sensors detect the missing wall every time. An eight-sample moving average filter was implemented to limit entrant readings to get an average of the results.

Similarly, when plugged into the computer, this filter gave consistent readings. When the computer connection was removed, and the robot was placed in the maze, it regularly failed to detect missing walls. Another attempted solution was to move pins and verify the sensor's wiring using the provided datasheet. The sensor was wired correctly, and moving to a different analog pin initially provided better results, but after a few attempts, the sensor failed to detect missing walls again. Since dropping battery voltage could affect the ADC readings, the battery was charged to full and re-installed in the robot, resulting in no change in the detection. The code was simplified to limit the chance that an errant loop or control logic influenced the read rate or ability to read. When the robot was only driven until it detected the missing wall, it consistently failed to detect it until it was plugged into a computer again to check serial readings. At that point, it detected the missing wall every time.

## c. Limiting factors

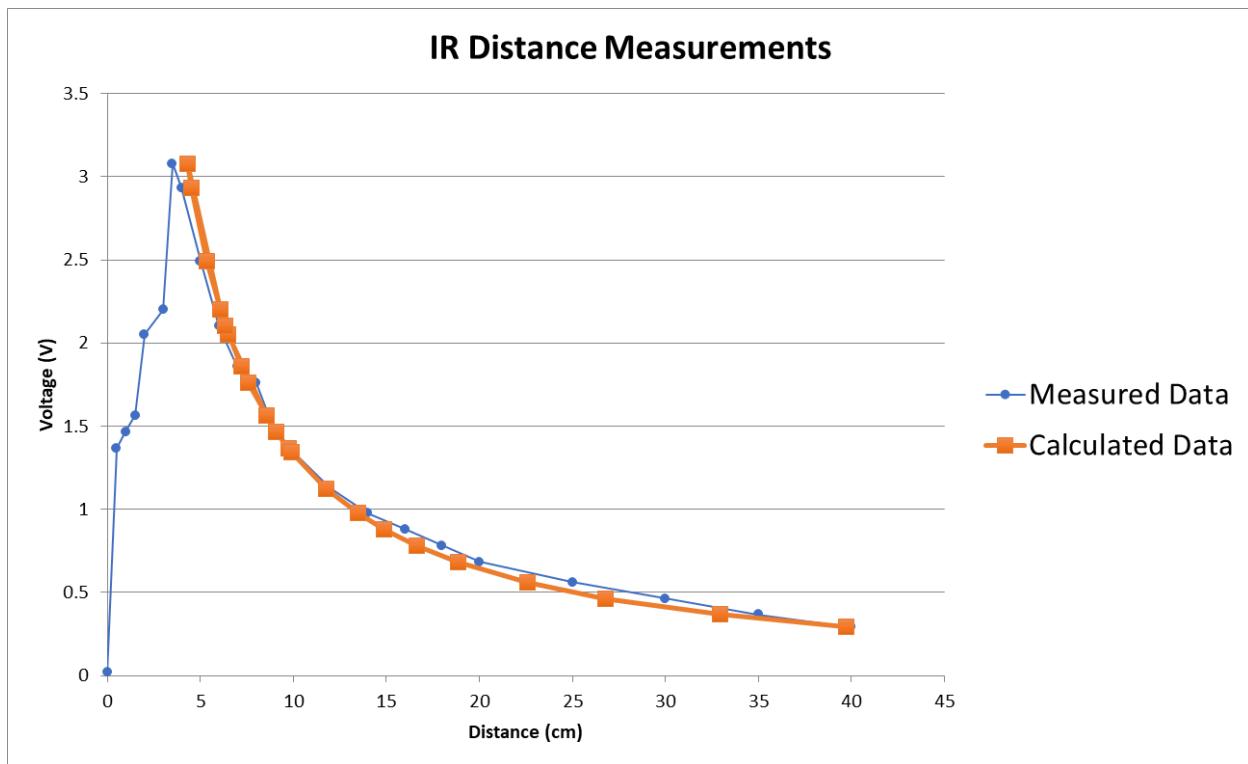
The inability to use the serial monitor to debug issues is incredibly frustrating. The Arduino's power indicator appears to dimmer when the computer is disconnected, and it switches over to battery power. This adds to the possibility that the battery through the h-bridge is providing inconsistent power to the Arduino, which could cause inconsistencies in the ADC readings. Because the supplied cable is too short to navigate the maze while plugged into the computer and sensors cannot be relied upon to navigate on battery power, it is impossible to build up and debug maze-solving algorithms. The issue could be addressed using different hardware, but further problem-solving would be required to address power issues outside the scope of this lab.

## d. IR Sensor Characterization Data and Graphs

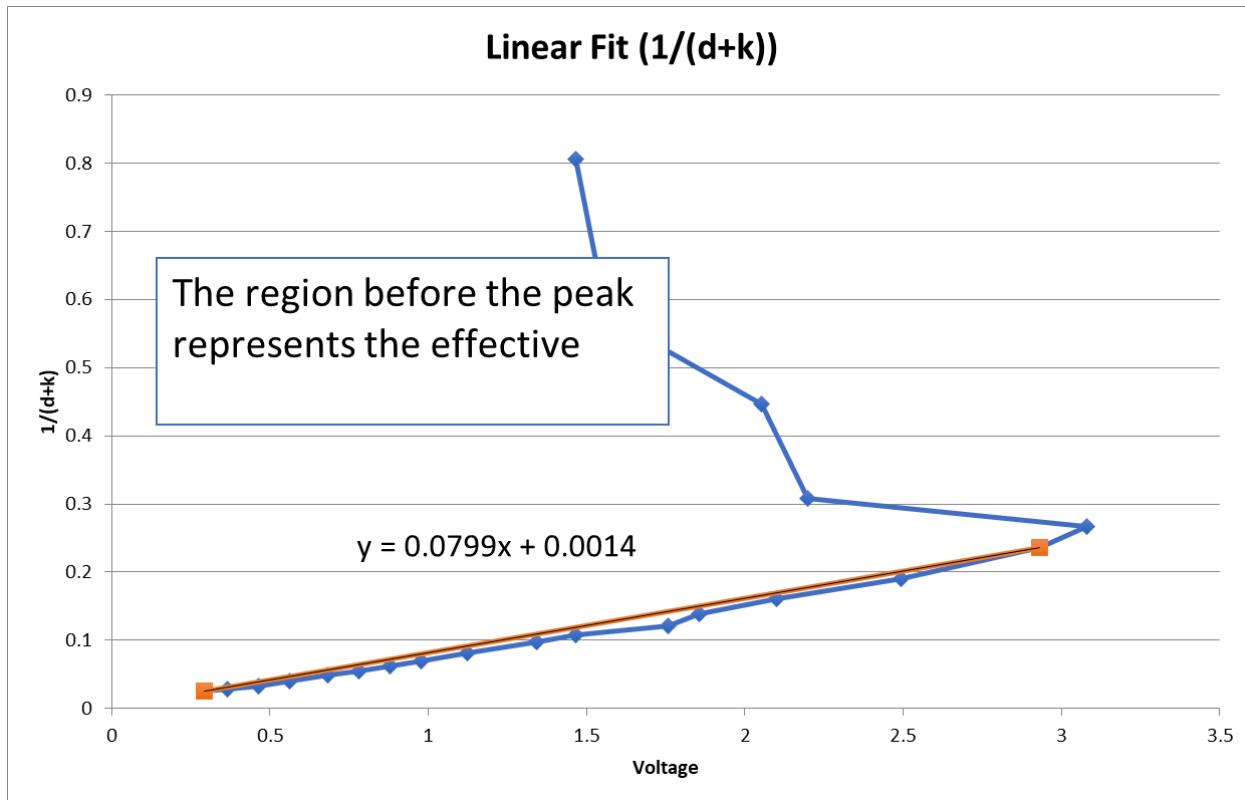
Distance (cm)	1/(d+k)	ADC	Voltage	m*V + b	d = 1/(m*V + b) - k	Error	Squared Error
0	#DIV/0!	4	0.019550 342	0.005868 524	170.1605 997	-170.1605 997	28954.62 967
0.5	1.3513513 51	280	1.368523 949	0.100296 676	9.730420 112	-9.230420 112	85.20065 545
1	0.8064516 13	300	1.466275 66	0.107139 296	9.093643 542	-8.093643 542	65.50706 579
1.5	0.5747126 44	320	1.564027 37	0.1139819 16	8.533321 556	-7.033321 556	49.46761 21
2	0.4464285 71	420	2.052785 924	0.148195 015	6.507865 32	-4.507865 32	20.32084 974

3	0.3086419 75	450	2.199413 49	0.158458 944	6.070782 926	-3.070782 926	9.429707 777
3.5	0.2673796 79	630	3.079178 886	0.220042 522	4.304576 162	-0.804576 162	0.647342 8
4	0.2358490 57	600	2.932551 32	0.209778 592	4.526930 642	-0.526930 642	0.277655 901
5	0.1908396 95	510	2.492668 622	0.178986 804	5.347004 071	-0.347004 071	0.1204118 26
6	0.1602564 1	430	2.101661 779	0.151616 325	6.355595 844	-0.355595 844	0.126448 404
7	0.1381215 47	380	1.857282 502	0.134509 775	7.194403 921	-0.194403 921	0.037792 885
8	0.1213592 23	360	1.759530 792	0.127667 155	7.592868 185	0.407131 815	0.165756 315
9	0.1082251 08	300	1.466275 66	0.107139 296	9.093643 542	-0.093643 542	0.008769 113
10	0.0976562 5	275	1.344086 022	0.098586 022	9.903425 86	0.096574 14	0.009326 564
12	0.0816993 46	230	1.124144 673	0.083190 127	11.780657 2	0.219342 8	0.0481112 64
14	0.0702247 19	200	0.977517 107	0.072926 197	13.47249 338	0.527506 618	0.278263 232
16	0.0615763 55	180	0.879765 396	0.066083 578	14.89235 261	1.107647 385	1.226882 73
18	0.0548245 61	160	0.782013 685	0.059240 958	16.64021 319	1.359786 811	1.849020 171
20	0.0494071 15	140	0.684261 975	0.052398 338	18.84457 47	1.155425 299	1.335007 621
25	0.0396196 51	115	0.562072 336	0.043845 064	22.56758 469	2.432415 308	5.916644 229
30	0.0330687 83	95	0.464320 626	0.037002 444	26.78524 205	3.214757 948	10.33466 867
35	0.0283768 44	75	0.366568 915	0.030159 824	32.91669 211	2.083307 891	4.340171 767
40	0.0248508 95	60	0.293255 132	0.025027 859	39.71547 484	0.284525 163	0.080954 568

**Figure 4.** Data Plots for the Right IR Sensor



**Figure 5.** Graph plot for the Right IR Sensor



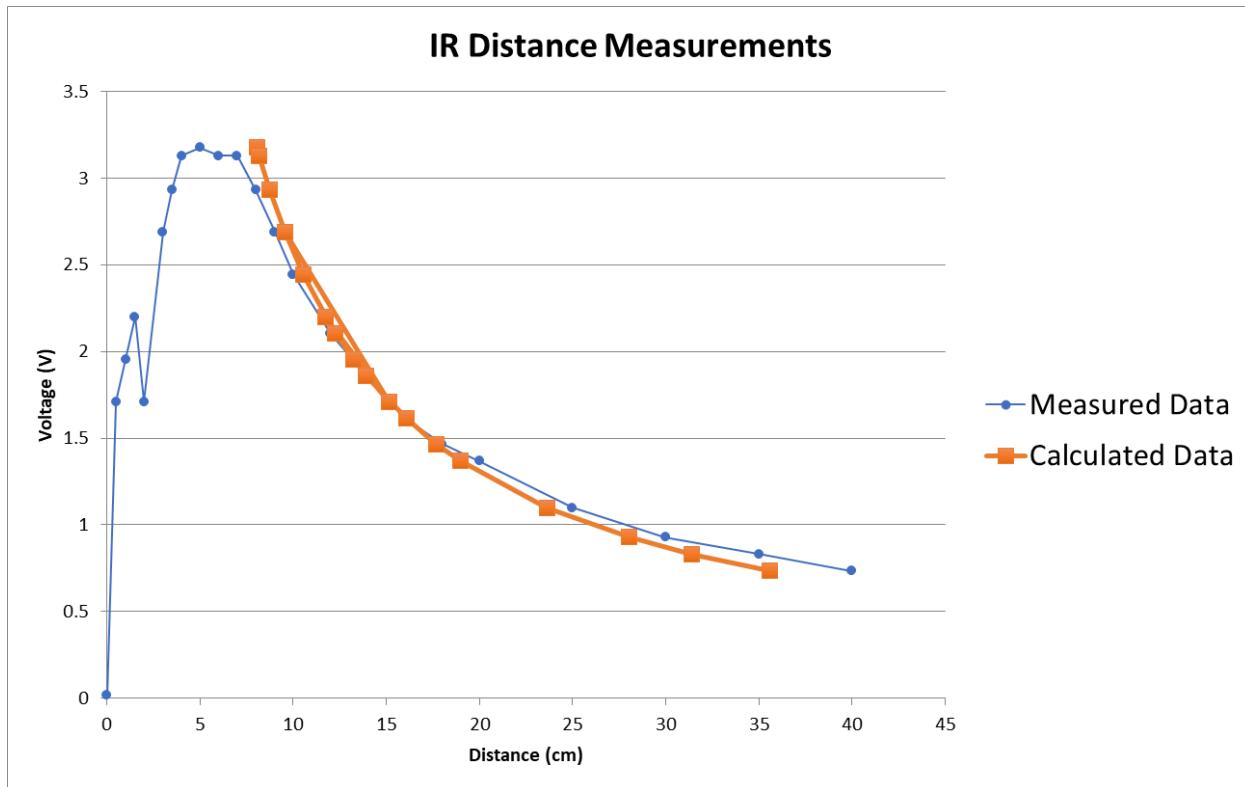
**Figure 6.** Linear Fit for the Right Sensor

Please note that, for some reason, our Excel document outputs this graph sideways for both the right and left IR sensors.

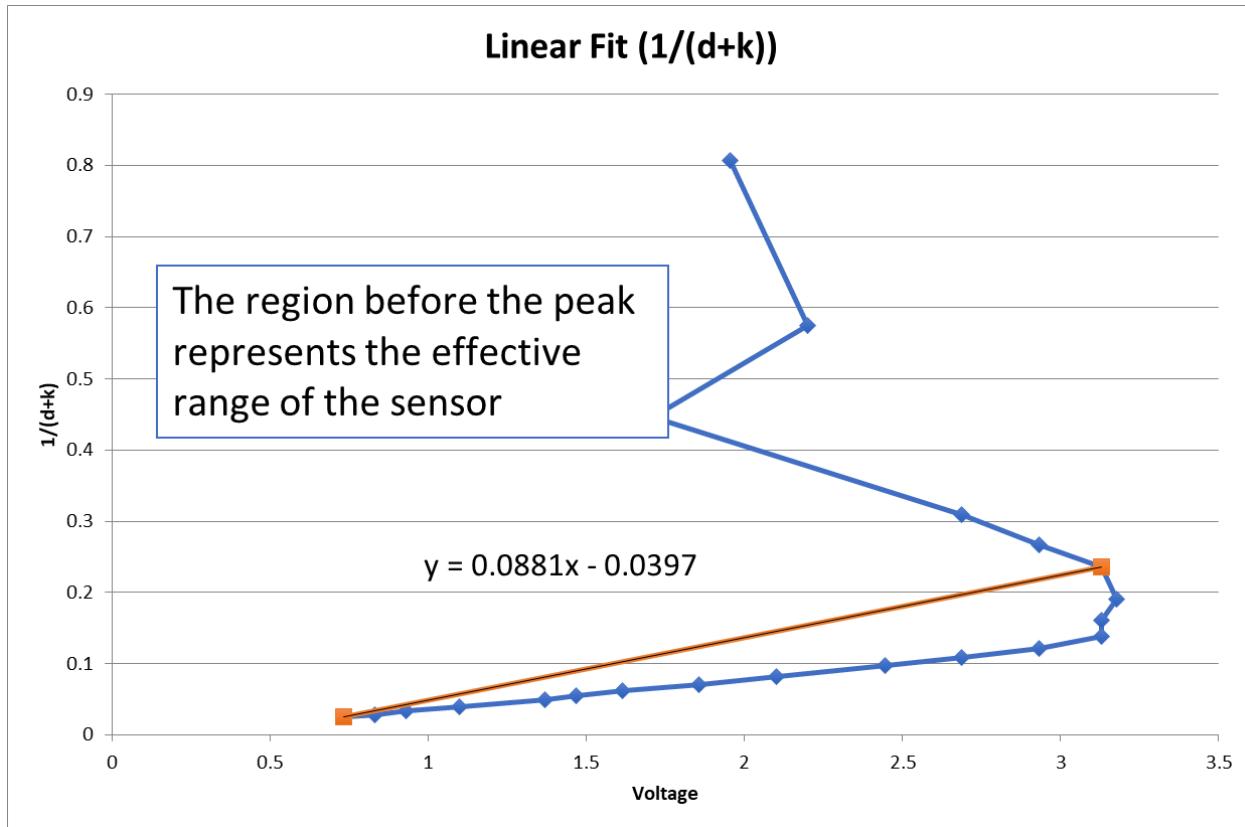
Distance (cm)	$1/(d+k)$	ADC	Voltage	$m^*V + b$	$d = 1/(m^*V + b) - k$	Error	Squared Error
0	#DIV/0!	4	0.019550 342	0.000792 913	1260.932 41	-1260.932 41	1589950. 541
0.5	1.351351 351	350	1.710654 936	0.065054 888	15.13163 52	-14.63163 52	214.0847 487
1	0.806451 613	400	1.955034 213	0.074341 3	13.211473 12	-12.21147 312	149.1200 758
1.5	0.574712 644	450	2.199413 49	0.083627 713	11.717758 6	-10.21775 86	104.4025 909
2	0.446428 571	350	1.710654 936	0.065054 888	15.13163 52	-13.13163 52	172.4398 43
3	0.308641 975	550	2.688172 043	0.102200 538	9.544684 339	-6.544684 339	42.83289 309

3.5	0.267379 679	600	2.932551 32	0.1114869 5	8.729659 666	-5.229659 666	27.34934 022
4	0.235849 057	640	3.128054 741	0.1189160 8	8.169291 651	-4.169291 651	17.38299 287
5	0.190839 695	650	3.176930 596	0.120773 363	8.039971 494	-3.039971 494	9.241426 682
6	0.160256 41	640	3.128054 741	0.1189160 8	8.169291 651	-2.169291 651	4.705826 266
7	0.138121 547	640	3.128054 741	0.1189160 8	8.169291 651	-1.169291 651	1.367242 965
8	0.121359 223	600	2.932551 32	0.1114869 5	8.729659 666	-0.729659 666	0.532403 228
9	0.108225 108	550	2.688172 043	0.102200 538	9.544684 339	-0.544684 339	0.296681 029
10	0.097656 25	500	2.443792 766	0.092914 125	10.52262 623	-0.522626 228	0.273138 174
12	0.081699 346	430	2.101661 779	0.079913 148	12.27358 544	-0.273585 436	0.074848 991
14	0.070224 719	380	1.857282 502	0.070626 735	13.91894 418	0.081055 817	0.006570 045
16	0.061576 355	330	1.612903 226	0.061340 323	16.06249 007	-0.062490 074	0.003905 009
18	0.054824 561	300	1.466275 66	0.055768 475	17.69127 746	0.308722 541	0.095309 607
20	0.049407 115	280	1.368523 949	0.052053 91	18.97085 272	1.029147 277	1.059144 117
25	0.039619 651	225	1.099706 745	0.041838 856	23.66122 695	1.338773 047	1.792313 271
30	0.033068 783	190	0.928641 251	0.035338 368	28.05785 498	1.942145 022	3.771927 285
35	0.028376 844	170	0.830889 541	0.031623 803	31.38175 07	3.618249 305	13.09172 803
40	0.024850 895	150	0.733137 83	0.027909 238	35.59043 065	4.409569 352	19.44430 187

Figure 7. Data Plots for the Right IR Sensor



**Figure 8.** Graph plot for the Left IR Sensor



**Figure 9.** Linear Fit for the Left Sensor

Please note that, for some reason, our Excel document outputs this graph sideways for both the right and left IR sensors.

#### e. IR Sensor Characterization Equation

The IR sensor characterization equation for the right IR sensor is:  $\text{dist} = 1/(0.07*\text{voltage} + 0.0045) - 0.24$ .

The left IR sensor's characterization equation is  $\text{dist} = 1/(0.038*\text{voltage} + 0.00005) - 0.24$ .

#### f. Table of results

Due to the issues discussed above, results still need to be obtained.

### Conclusions

The control systems built and tuned throughout the previous labs were very successful. Encoders with this low resolution aren't the most reliable units of measurement, but implementing reliable control on top of it resulted in consistent enough control for navigating the maze. The new sensor implementation for this lab ultimately killed our performance. Much of the time spent working on this lab was spent debugging these sensors, with a likely hardware issue resulting in an unsolvable problem. In theory, the maze-solving algorithm we research should be powerful and, when combined with our fast control system, should speed up the maze's exploration and running.

We were surprised by how unreliable the Arduino's ADC is in reading the infrared sensors. Additionally, it was surprising that disconnecting from the computer caused a significant enough change in the system to remove all reliability.

We used all the tools available to debug the system and attempt to resolve the issues we were running into, but no solution resulted. Sensor calibration went well; when connected to the computers, all the sensors read extremely accurately. The final robot construction was solid and introduced little error.

We could have done better implementing the control logic, but more debugging, with the help of the robot, would be needed to achieve a successful implementation. Our wiring also got progressively more messy as the labs progressed, and it would have been much easier to follow if it had been simplified and cleaned up using shorter wires on the breadboard cut to length.

Next time, a fuller test of the supplied hardware may reveal potential issues before spending considerable time trying to code around hardware problems that may not be solvable without replacing broken hardware.

Due to our hardware's limitations, we cannot test a final implementation of our algorithm.

## References

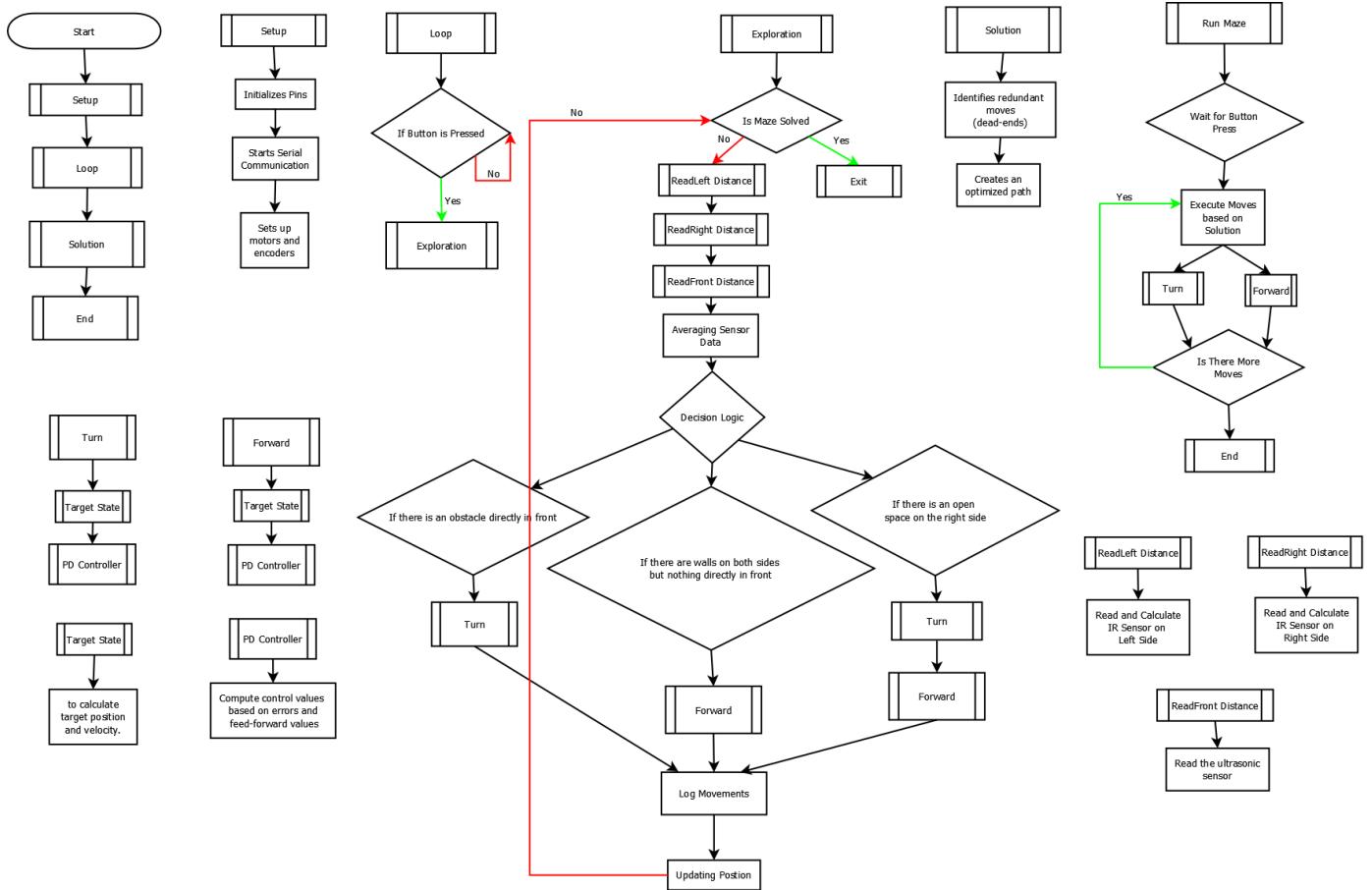
- [1] Veritasium video on maze solving competitions -  
<https://www.youtube.com/watch?v=ZMQbHMgK2rw>

## Appendices

### a. Video Link:

Unable to make a video due to issues with our robot.

## b. Software Diagram



## c. Software

```

/*
Lab 4: maze solving
last updated: gkn 20240327
*/

#include <PinChangeInterrupt.h>
#include <HC-SR04.h> // Ultrasonic distance sensor library for HC-SR04
// This code assumes the HC-SR04 Library by gamegine, but many work

// Define pins and constants for hardware setup
#define buttonPin 11

#define EncoderMotorLeft 7
#define EncoderMotorRight 8
  
```

```

#define A 0
#define B 1

// Motor driver shield settings
#define SHIELD false
#define motorApwm 3
#define motorAdir 12
#define motorBpwm 11
#define motorBdir 13

// Motor driver pins for a Dual H-Bridge setup
#define IN1 9
#define IN2 10
#define IN3 5
#define IN4 6

// Movement constants for direction
#define FORWARD 0
#define LEFT -75
#define RIGHT 85

#define pushButton 11

// Robot states and direction constants
#define STOPPED 0
#define SPEED 1
#define RUN 2
#define SLOW 3
#define NORTH 0
#define EAST 1
#define SOUTH 2
#define WEST 3

// Define IR distance sensor pins
#define LeftIR A2
#define RightIR A5

// Define Ultrasonic sensor pins
#define trig 4

```

```

#define echo 3

// Initialize ultrasonic sensor for the front
HCSR04 frontUS(trig, echo);

// Define distance tolerances for wall detection and collision prevention
#define wallTol 20 //cm
#define crashTol 7 //cm

// Initial state and direction variables
uint8_t currentState = 0;
uint8_t currentDirection = NORTH;

// Score table for maze-solving logic
uint8_t idealScores[5][5] = {
    {1, 1, 1, 1, 1},
    {1, 2, 2, 2, 2},
    {1, 2, 3, 3, 3},
    {1, 2, 3, 4, 4},
    {1, 2, 3, 4, 5}
};

// Movement tracking variables
int moves[50];
int maze[50];
int distance[50];
uint8_t pos[2];

// Structures for velocity and state data
struct velProfile {
    float t1;
    float t2;
    float tf;
    float vel;
};

struct state {
    float x;
    float v;
}

```

```

};

// PID and speed control variables
float Kp[] = {5.0, 4.75};
float Kd[] = {1, 1};

float maxSpeedA = 93.7;
float maxSpeedB = 112.4;

float cntCm = 0.955;
float DistancePerRev = 28;
float EncoderCountsPerRev = 24;
float l = 9;
float cmDegree = (2*3.5*l)/360;

float desiredMaxSpeed = 40; // Desired speed in cm/s
int desiredDistance = 30; // Test distance in cm

// Encoder variables for left and right motors
volatile unsigned int leftEncoderCount = 0;
volatile unsigned int rightEncoderCount = 0;

int PDdelay = 20;
unsigned long nextPDtime = 0;
int printDelay = 200;
unsigned long nextPrintTime = printDelay;
float rampFraction = 0.3;
struct velProfile profile;

// Setup function for initializing hardware and variables
void setup() {
    pinMode(pushButton, INPUT_PULLUP);
    Serial.begin(9600);
    motor_setup();
    encoder_setup();
    profile = genVelProfile(desiredMaxSpeed, desiredDistance, rampFraction);
}

// Main loop function

```

```

void loop() {
    // Wait for button press to start the maze exploration
    while (digitalRead(pushButton) == 1) {
        Serial.print(readLeftDist());
        Serial.print("\t");
        Serial.print(readRightDist());
        Serial.print("\t");
        Serial.println(readFrontDist());
    }

    delay(50); // debounce input
    while (digitalRead(pushButton) == 0); // wait for button release
    delay(50); // debounce input

    explore(); // Start maze exploration
}

// Function to read distance from the left IR sensor
float readLeftDist() {
    float reading = analogRead(LeftIR);
    float voltage = (reading/1024)*5;
    float dist = 1/(0.038*voltage + 0.00005) - 0.24; // Using calibration
equation
    return dist;
}

// Function to read distance from the right IR sensor
float readRightDist() {
    float reading = analogRead(RightIR);
    float voltage = (reading/1024)*5;
    float dist = 1/(0.07*voltage + 0.0045) - 0.24; // Using calibration
equation
    return dist;
}

// Function to read distance from the front ultrasonic sensor
float readFrontDist() {
    float dist = frontUS.dist(); // Distance in cm
    return dist;
}

```

```

}

// Maze exploration function
void explore() {
    while (digitalRead(pushButton) == 1) { // Loop until the maze is solved
        // Read distances and average sensor inputs
        static uint16_t lastcount = 0;
        static uint8_t ii = 0;
        static uint8_t jj = 0;
        static float rightSide, leftSide, front;
        static float avgTotRight, avgTotLeft, avgTotFront;
        static float rightRead[8], leftRead[8], frontRead[8];

        // Capture samples for averaging sensor inputs
        while(jj < 8){
            rightRead[jj] = readRightDist();
            avgTotRight += rightRead[jj];
            leftRead[jj] = readLeftDist();
            avgTotLeft += leftRead[jj];
            frontRead[jj] = readFrontDist();
            avgTotFront += frontRead[jj];
            jj++;
        }

        // Calculate averages and determine directions based on maze structure

        // Moving logic based on sensor readings
        uint8_t desiredDirection;
        if(currentState == STOPPED && desiredDirection == FORWARD) {
            driveForward(1); // Run acceleration profile
            currentState = RUN;
        }
        else if(currentState == RUN && rightSide < wallTol && leftSide <
wallTol && front > crashTol) {
            driveForward(2); // Continue driving forward
            // Update position based on encoder count and direction
        }
        else {
            // Handle other movement cases
        }
    }
}

```

```

        }
    }
}

// Function to solve the maze using recorded moves
void solve() {
    // Implement algorithm to solve the maze using explore data
}

// Function to navigate the maze with the shortest path
void runMaze() {
    int j = 0;
    // Wait for button press to start maze run
    while (digitalRead(buttonPin) == 1);
    delay(50); // Debounce delay
    while (digitalRead(buttonPin) == 0); // Wait for button release
    for (int i = 0; i < sizeof(maze)/2; i++) {
        if(moves[i] == FORWARD) {
            // Drive forward for specified distance
            j++;
        }
        else {
            run_motor(A, 0);
            turn(30, moves[i]); // Turn in specified direction
        }
        run_motor(A, 0);
        run_motor(B, 0);
    }
    j = 0; // Reset distance index
}

// Function to drive forward following a trapezoidal velocity profile
void driveForward(int forwardState) {
    // Implement forward driving logic based on velocity profile
}

// Function to turn by a specified angle
void turn(float maxAngularSpeed, float degrees) {
    // Convert speed to motor commands and encoder counts
}

```

```
}

// Function to calculate target state in velocity profile
struct state targetState(float time, struct velProfile vp) {
    // Calculate desired position and velocity at a given time
}

// PD controller function
int pdController(float FF, float Verr, float Xerr, float kp, float kd) {
    int u = FF + kp*Xerr + kd*Verr;
    int cmd = constrain(u, -255, 255);
    return cmd;
}
```