

# MA 331 Quiz 2

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I pledge my honor that I have abided by the Stevens honor system.

## 1. Categorical

random variables

Variable 1: Commercial  
Version

→ first version

→ second version

→ third version

Variable 2: likelihood  
to buy

→ likely

a product

→ unsure or unlikely

## 2.

Commercial Version	Likely	unsure or unlikely	total
1 <sup>st</sup> version	25	40	65
2 <sup>nd</sup> version	20	10	30
3 <sup>rd</sup> version	54	31	85
total	99	81	180

likelihood to buy  
product

## 3.

Expected 2-way table

Commercial Version	Likely	unsure or unlikely	total
1 <sup>st</sup> version	35.75	29.25	65
2 <sup>nd</sup> version	16.5	13.5	30
3 <sup>rd</sup> version	46.75	38.25	85
total	99	81	180

## 4.

$$\chi^2 = \sum \frac{(\text{observed} - \text{expected})^2}{\text{expected}}$$

$\chi^2$	likely	unlikely
version 1	3.2325	3.9504
version 2	0.7424	0.9074
version 3	1.1243	1.3742

$$\Rightarrow \chi^2 = 11.3317$$

5.

The  $H_0$  is that there is no relationship between <sup>the</sup> commercial version and the likelihood of a potential customer to buy the product.

$$\chi^2 \sim \chi^2_k \text{ with } k = (r-1)(c-1) \quad \chi^2_{\alpha} \text{ as } k = (3-1)(2-1)$$

6.

$$P_{H_0}(\chi^2) = \sum_{i=1}^r \sum_{j=1}^c \frac{(O_{ij} - E_{ij})^2}{E_{ij}} < \alpha$$

$$P_{H_0}(\chi^2 > 11.3317) = 0.063465$$

$$P_{H_0}(\chi^2 > 11.3317) < \alpha$$

7. If the p-value is smaller than the significance level  $\alpha$  we reject the  $H_0$ . Otherwise we fail to accept the  $H_0$  if the p-value is too large.

8. If the p-value is small we reject the  $H_0$ .

So there is an association between the commercial version shown and a potential buyers likelihood of buying a product. If the p-value is higher than the significance level and we fail to reject the  $H_0$ , then we can conclude there is no <sup>apparent</sup> association between the commercial version shown and the potential buyers likelihood of buying a product.