

# F-16 Model

## Linear vs. Non-linear models

- Linear model has form

$$\dot{x} = Ax + Bu$$

$$y = Cx + Du$$

- Contains all dynamics around an operating (trim) point
- Is defined by matrices A, B, C, and D

- Non-linear model has form  $\dot{x} = f(x, u)$

- In this case function  $f$  is called *nlplant*
  - In Simulink it is contained in a Matlab function block
  - Source is a C-function (`nlplant.c`)
  - Compiled into Mex-function (`mex nlplant.c`)

# F-16 Model

## States

- Model has 12 “core” states ( $x$ ) which need to be integrated
  - North position
  - East position
  - Altitude
  - Bank angle  $\phi$
  - Pitch angle  $\theta$
  - Heading angle  $\psi$
  - Total airspeed  $V$
  - Angle of attack  $\alpha$
  - Sideslip angle  $\beta$
  - Roll rate  $p$
  - Pitch rate  $q$
  - Yaw rate  $r$

# F-16 Model

## States

- Model has 6 “auxilliary” states

- Mostly 1<sup>st</sup> order dynamics

- Gain usually 1

$$\frac{K}{\tau s + 1}$$

- Engine thrust dynamics

- Elevator actuator

- Aileron actuator

- Rudder actuator

- Leading edge flap

- 2 internal states
  - Not used in low fidelity model

- Total of **18** states in linear & non-linear model

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# F-16 Model

## Inputs

- Model has 4 pilot inputs
  - Thrust [lbf]
    - Range from 1000 to 19000
  - Elevator angle [deg]
    - Range from  $-25^{\circ}$  to  $+25^{\circ}$
  - Aileron angle [deg]
    - Range from  $-21.5^{\circ}$  to  $+21.5^{\circ}$
  - Rudder angle [deg]
    - Range from  $-30^{\circ}$  to  $+30^{\circ}$
- Linear model only has these inputs (B matrix size =  $18 \times 4$ )
  - Are passed through the first order actuator dynamics before going to the aerodynamic part of the model
  - Non-linear model is different

# F-16 Model

Inputs non-linear model

$$\dot{x} = f(x, u)$$

- Non-linear model (nlplant function) has **18** inputs
  - 12 “core” states
  - Thrust (after dynamics!)
  - Elevator angle (after dynamics!)
  - Aileron angle (after dynamics!)
  - Rudder angle (after dynamics!)
  - Leading edge flap angle (keep at zero)
  - Fidelity switch (keep at zero for lofi)

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# F-16 Model

## Outputs

- Linear and non-linear model have 18 outputs
  - 12 “core” states
  - Longitudinal load factor  $n_x$
  - Lateral load factor  $n_y$
  - Vertical load factor  $n_z$
  - Mach number
  - Dynamic pressure  $q_{bar}$
  - Static pressure  $p_s$
- Linear model's C matrix has size **18 x 18**
  - Outputs are deviations from trim point
- Output from *nlplant* function has size **18**
  - 12 “core” state derivatives to be integrated
  - 6 “quasi” derivatives that are really outputs



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