

BIODS253 W24: Statistical Wordle Assistant

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How To Play

Guess the Wordle in 6 tries.

- Each guess must be a valid 5-letter word.
- The color of the tiles will change to show how close your guess was to the word.

Examples



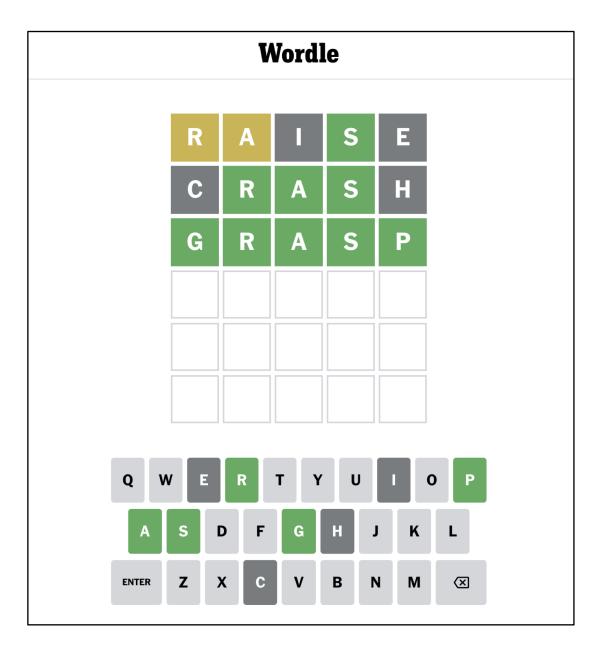
W is in the word and in the correct spot.



I is in the word but in the wrong spot.



U is not in the word in any spot.



(Abridged) Design Considerations

Aims:

A lightweight wordle assistant to help users make statistically informed guesses.

Non-Aims:

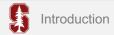
This isn't a graphical wordle simulator, it's a statistical assistant. We will be doing some evaluations, but we aren't trying to design an optimal algorithm.

Requirements:

Fast enough to run interactively, (with caveats for evaluations). Guesses and behavior should replicate behavior of NYT app, not necessarily other wordle copies.

Dependencies:

This is designed to be super lightweight, so written mostly in pure python with some common libraries (NumPy, pandas). Nonetheless, packaged everything in a reproducible conda env.



Intuition

The quality of a guess is how well it *filters* possible answers (2315 valid answers)

F U Z Z Y

What Makes a Good Guess?

The quality of a guess is how well it *filters* possible answers (2315 valid answers)





Not much information gained, many words fit this.



A lot of information gained, very few words fit this

What Makes a Good Guess?

The quality of a guess is how well it *filters* possible answers (2315 valid answers)



Quality = likelihood x information gained



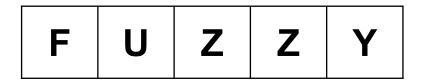
Not much information gained, many words fit this.



A lot of information gained, very few words fit this

Measuring Guess Quality with Information Theory

The quality of a guess is how well it *filters* possible answers (2315 valid answers)



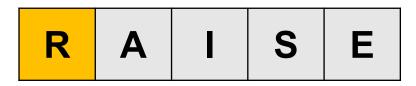
$$E[I] = \sum_{x} p(x)I(x)$$

$$= \sum_{x} p(x)\log_2 \frac{1}{p(x)}$$

$$= -\sum_{x} p(x)\log_2 p(x)$$

*flyer or foyer

Strategies



Best Guess:

select *word* with highest possible expected information



4.91 bits, not possible answer

Best Answer:

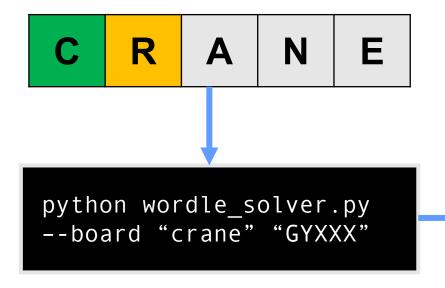
select possible *answer* with highest possible expected information



4.33 bits, possible answer

Tradeoff between maximizing expected information and getting "lucky" on the next turn

Demo



flexible usage, can help with first guess, or after (multiple) previous turns. ~0.5 sec latency enables interactive assistance.

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There are 9 possible answers remaining.
All Guesses Ranked by Information (* = possible answer)
ivory 3.170 tulip 2.948 sorry 2.948 slurp 2.948 court 2.948 *
viola 3.170 quile 2.948 quirk 2.948 folio 2.948 hovel 2.948
lorry 3.170 could 2.948 intro 2.948 rumor 2.948 furor 2.948
glory 3.170 quail 2.948 worry 2.948 ovoid 2.948 fluid 2.948
... top 20/2315 shown
Possible Answers Ranked by Information
court 2.948 choir 2.642 curly 2.419 chirp 2.419 curvy 2.059
chord 2.725 curry 2.503 curio 2.419 color 2.419
... top 9/9 shown
Using the strategy: best_guess, we suggest picking one of:
ivory viola lorry glory
Using the strategy: best_answer, we suggest picking one of:
court
```

Evaluation

Play wordle over all 2315 possible answers with 10 repetitions*, counting the number of guesses until correct. Compare against baselines

Random Answer:

Select possible answers at each turn randomly.

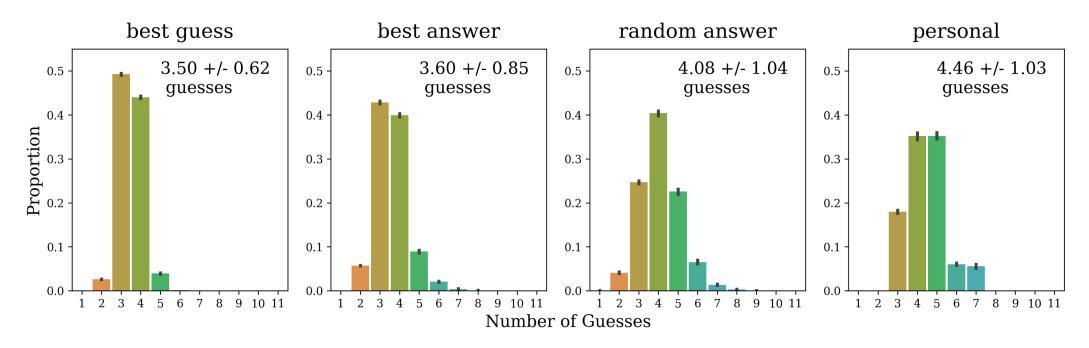
Human (aka me):

Bootstrap resample my historical performance on the NYT app.

*if there is a tie in expected information, both strategies will randomly pick a guess



Results



Using a paired* t-test, we have with statistical significance that the strategies in order of least to most number of guesses are:

best guess, best answer, random answer, and me (⊗)

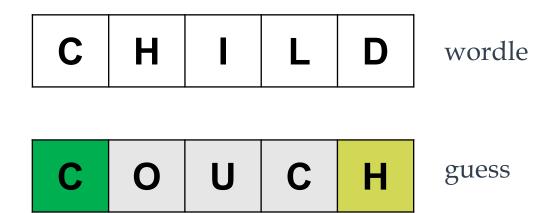
*paired per secret word



(Some) Engineering Details

Testing:

Wordle is surprisingly ambiguous with its rules, particularly concerning duplicate letters. I ran tests on these edge cases to ensure I replicated the NYT app's behavior.



Speed:

The solver is fast enough for interactive applications, with ~ 0.5 sec/guess.

For simulations, too slow (2 secs/game, 1 hour per strategy). After profiling, introduced intermediate caching to yield 0.35 secs/game, ~13 mins per strategy)



Thanks for Listening!

Still polishing repo for final submission, but check it out here: https://github.com/tboen1/biods253_final_project

