# Updated High-Temperature Opacities for The Dartmouth Stellar Evolution Program and their Effect on the Jao Gap Location

THOMAS M. BOUDREAUX<sup>1</sup> AND BRIAN C. CHABOYER<sup>1</sup>

<sup>1</sup>Department of Physics and Astronomy, Dartmouth College, Hanover, NH 03755, USA

## ABSTRACT

The Jao Gap, a 17 percent decrease in stellar density at  $M_G \sim 10$  identified in both Gaia DR2 and EDR3 data, presents a new method to probe the interior structure of stars near the fully convective transition mass. The Gap is believed to originate from convective kissing instability wherein asymmetric production of <sup>3</sup>He causes the core convective zone of a star to periodically expand and contract and consequently the stars' luminosity to vary. Modeling of the Gap has revealed a sensitivity in its magnitude to a population's metallicity primarily through opacity. Thus far, models of the Jao Gap have relied on OPAL high-temperature radiative opacities. Here we present updated synthetic population models tracing the Gap location modeled with the Dartmouth stellar evolution code using the OPLIB high-temperature radiative opacities. Use of these updated opacities changes the predicted location of the Jao Gap by  $\sim 0.05$  mag as compared to models which use the OPAL opacities.

Keywords: Stellar Evolution (1599) — Stellar Evolutionary Models (2046)

## 1. INTRODUCTION

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Due to the initial mass requirements of the molecular 17 18 clouds which collapse to form stars, star formation is 19 strongly biased towards lower mass, later spectral class 20 stars when compared to higher mass stars. Partly as result of this bias and partly as a result of their ex-22 tremely long main-sequence lifetimes, M Dwarfs make 23 up approximately 70 percent of all stars in the galaxy. 24 Moreover, some planet search campaigns have focused 25 on M Dwarfs due to the relative ease of detecting small 26 planets in their habitable zones (e.g. Nutzman & Char-27 bonneau 2008). M Dwarfs then represent both a key 28 component of the galactic stellar population as well as 29 the possible set of stars which may host habitable ex-30 oplanets. Given this key location M Dwarfs occupy in 31 modern astronomy it is important to have a thorough understanding of their structure and evolution.

Jao et al. (2018) discovered a novel feature in the Gaia Data Release 2 (DR2)  $G_{BP}-G_{RP}$  color-magnitudediagram. Around  $M_G=10$  there is an approximately percent decrease in stellar density of the sample of

Corresponding author: Thomas M. Boudreaux thomas.m.boudreaux.gr@dartmouth.edu, thomas@boudreauxmail.com

stars Jao et al. (2018) considered. Subsequently, this has become known as either the Jao Gap, or Gaia M Dwarf Gap. Following the initial detection of the Gap in DR2 the Gap has also potentially been observed in 2MASS (Skrutskie et al. 2006; Jao et al. 2018); however, the significance of this detection is quite weak and it resis on the prior of the Gap's location from Gaia data. Further, the Gap is also present in Gaia Early Data Resis (EDR3) (Jao & Feiden 2021). These EDR3 and 2MASS data sets then indicate that this feature is not a bias inherent to DR2.

The Gap is generally attributed to convective instabilaties in the cores of stars straddling the fully convective transition mass (0.3 - 0.35  $\rm M_{\odot})$  (Baraffe & Chabrier 2018). These instabilities interrupt the normal, slow, main sequence luminosity evolution of a star and result in luminosities lower than expected from the main sequence mass-luminosity relation (Jao & Feiden 2020).

The Jao Gap, inherently a feature of M Dwarf populations, provides an enticing and unique view into the interior physics of these stars (Feiden et al. 2021). This be specially important as, unlike more massive stars, M Dwarf seismology is infeasible due to the short periods and extremely small magnitudes which both radial and low-order low-degree non-radial seismic waves are predicted to have in such low mass stars (Rodríguezknich López 2019). The Jao Gap therefore provides one of the 64 only current methods to probe the interior physics of M

Despite the early success of modeling the Gap some issues remain. Jao & Feiden (2020, 2021) identify that the Gap has a wedge shape which has not been successful reproduced by any current modeling efforts and which miplies a somewhat unusual population composition of young, metal-poor stars. Further, Jao & Feiden (2020) identify substructure, an additional over density of stars, directly below the Gap, again a feature not yet fully acaptured by current models.

All currently published models of the Jao Gap make use of OPAL high temperature radiative opacities. Here we investigate the effect of using the more up-tothe date OPLIB high temperature radiative opacities and whether these opacity tables bring models more in line with observations. In Section 2 we provide an overview of the physics believed to result in the Jao Gap, in Section 3 we review the differences between OPAL and OPLIB and describe how we update DSEP to use OPLIB opacity tables. In Section 4 we validate the update opacities by generating solar calibrated stellar models. Section 5 walks through the stellar evolution and population synthesis modeling we perform. Finally, in Section 6 we present our findings.

# 2. JAO GAP

A theoretical explanation for the Jao Gap (Figure 1) comes from van Saders & Pinsonneault (2012), who pro-92 pose that in a star directly above the transition mass, 93 due to asymmetric production and destruction of <sup>3</sup>He 94 during the proton-proton I chain (ppI), periodic lumi-95 nosity variations can be induced. This process is known 96 as convective-kissing instability. Such a star will descend 97 the pre-main sequence with a radiative core; however, as 98 the star reaches the zero age main sequence (ZAMS) and <sub>99</sub> as the core temperature exceeds  $7 \times 10^6$  K, enough engy will be produced by the ppI chain that the core 101 becomes convective. At this point the star exists with 102 both a convective core and envelope, in addition to a 103 thin, radiative layer separating the two. Subsequently, asymmetries in ppI affect the evolution of the star's convective core. 105

The proton-proton I chain constitutes three reactions

1. 
$$p+p \longrightarrow d+e^++\nu_e$$

108 2. 
$$p+d \longrightarrow {}^{3}\text{He} + \gamma$$

$$3. {}^{3}\text{He} + {}^{3}\text{He} \longrightarrow {}^{3}\text{He} + 2p$$

Because reaction 3 of ppI consumes <sup>3</sup>He at a slower rate than it is produced by reaction 2, core <sup>3</sup>He abundance, and consequently the rate of reaction 3, increases with

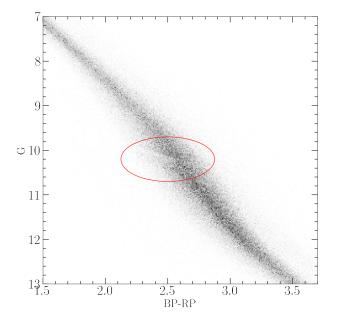


Figure 1. The Jao Gap seen in the Gaia Catalogue of Nearby Stars (circled)

113 time. The core convective zone expands as more of the 114 star becomes unstable to convection. This expansion 115 continues until the core connects with the convective 116 envelope. At this point convective mixing can transport material throughout the entire star and the high concen-118 tration of <sup>3</sup>He rapidly diffuses outward, away from the 119 core, decreasing energy generation as reaction 3 slows 120 down. Ultimately, this leads to the convective region 121 around the core pulling back away from the convective 122 envelope, leaving in place the radiative transition zone, at which point <sup>3</sup>He concentrations grow in the core un-124 til it once again expands to meet the envelope. These periodic mixing events will continue until <sup>3</sup>He concen-126 trations throughout the star reach an equilibrium ul-127 timately resulting in a fully convective star. Figure 2 128 traces the evolution of a characteristic star within the 129 Jao Gap's mass range.

## 2.1. Efforts to Model the Gap

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Since the identification of the Gap, stellar modeling has been conducted to better constrain its location, effects, and exact cause. Both Mansfield & Kroupa (2021) and Feiden et al. (2021) identify that the Gap's mass location is correlated with model metallicity — the mass-luminosity discontinuity in lower metallicity models being at a commensurately lower mass. Feiden et al. (2021) suggests this dependence is due to the steep relation of the radiative temperature gradient,  $\nabla_{rad}$ , on temperature and, in turn, on stellar mass.

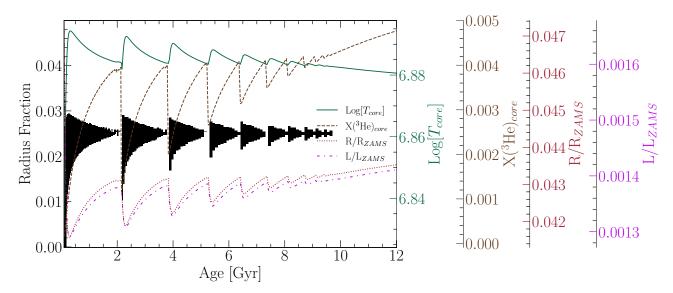


Figure 2. Kippenhan diagram for a characteristic stellar model of  $0.35625~M_{\odot}$  which is within the Jao Gap's mass range. The black shaded regions denote whether, at a particular model age, a radial shell within the model is radiative or convective (with white meaning convective and black meaning radiative). The lines trace the models core temperature, core <sup>3</sup>He mass fraction, fractional luminosity wrt. the zero age main sequence and fractional radius wrt. the zero age main sequence.

$$\nabla_{rad} \propto \frac{L\kappa}{T^4} \tag{1}$$

As metallicity decreases so does opacity, which, by Equation 1, dramatically lowers the temperature at which radiation will dominate energy transport (Chabrier & Baraffe 1997). Since main sequence stars are virialized the core temperature is proportional to the core density and total mass (Equation 2). Therefore, if the core temperature where convective-kissing instability is expected decreases with metallicity, so too will the mass of stars which experience such instabilities.

$$T_c \propto \rho_c M^2 \tag{2}$$

The strong opacity dependence of the Jao Gap begs the question: what is the effect of different opacity [estimates?] on Gap properties. As we can see above, changing opacity should affect the Gap's location in the mass-luminosity relation and therefore in a color-magnitude diagram. Moreover, current models of the Gap have yet to locate it precisely in the CMD (Feiden et al. 2021) with an approximate 0.16 G-magnitude difference between the observed and modeled Gaps. Opacity provides one, as yet unexplored, knob to turn which has the potential to resolve these discrepancies.

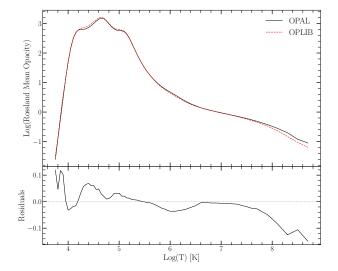
## 3. UPDATED OPACITIES

Multiple groups have released high-temperature opacities including, the Opacity Project (OP Seaton et al. 168 1994), Laurence Livermore National Labs OPAL opac-169 ity tables (Iglesias & Rogers 1996), and Los Alamos 170 National Labs OPLIB opacity tables (Colgan et al. 171 2016). OPAL high-temperature radiative opacity tables 172 in particular are very widely used by current generation 173 isochrone grids (e.g. Dartmouth, MIST, & StarEvol, 174 Dotter et al. 2008; Choi et al. 2016; Amard et al. 2019). 175 However, they are relatively old and therefore do not in-176 corporate the most up-to-date understanding of plasma 177 modeling in their code (Colgan et al. 2016)

While the overall effect on the CMD of using OPLIB 179 compared to OPAL tables is small, the strong theoreti-180 cal opacity dependence of the Jao Gap raises the poten-181 tial for these small effects to measurably shift the Gap's 182 location. We update DSEP to use high temperature 183 opacity tables based on measurements from Los Alamos 184 national Labs T-1 group (OPLIB, Colgan et al. 2016). 185 The OPLIB tables use the ATOMIC. ATOMIC (Magee 186 et al. 2004; Hakel et al. 2006; Fontes et al. 2015) is a 187 modern LTE and non-LTE opacity and plasma model-188 ing code which was used to generate opacity tables in an attempt to resolve the discrepancy between helioseis-190 mic and solar model predictions of chemical abundances 191 in the sun (Bahcall et al. 2005). For a detailed break-192 down of how the most up-to-date set of OPLIB tables 193 are generated see (Colgan et al. 2013a,b, 2015, 2016). OPLIB tables include monochromatic Rosseland

mean opacities — composed from bound-bound, boundmean opacities — composed from bound-bound, boundmean opacities — free-free, and scattering opacities — for elements
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**Figure 3.** Rosseland mean opacity with the GS98 solar composition for both OPAL opacities and OPLIB opacities (top). Residuals between OPLIB opacities and OPAL opacities (bottom). These opacities are plotted at  $\log_{10}(R) = -1.5$ , X = 0.7, and Z = 0.02. Note how the OPLIB opacities are systematically lower than the OPAL opacities for temperatures above  $10^6$  K.

199 cm<sup>-3</sup> up to approximately 10<sup>4</sup> g cm<sup>-3</sup> (though the exact mass density range varies as a function of temperature).
201 When comparing OPAL and OPLIB opacity tables (Figure 3) we find OPLIB opacities are systematically 203 lower than OPAL opacities for temperatures above 10<sup>6</sup> K. These lower opacities will decrease the radiative temperature gradient. Consequently, the radiative layer in a stellar model evolved using OPLIB opacity tables should 207 be closer into the model core than it would be in models 208 making use of OPAL tables.

# 3.1. Table Querying and Conversion

The high-temperature opacity tables used by DSEP give Rosseland-mean opacity,  $\kappa_R$ , along three dimensions: temperature, a density proxy R, and composition. R is defined as

$$R = \frac{\rho}{T_6^3} \tag{3}$$

Where  $T_6 = T \times 10^{-6}$  and  $\rho$  is the mass density. If  $T_{217}$  and  $\rho$  are given in cgs then for much of the radius of a star  $\log(R) \sim -1.5$  [CITATION]. R is used, as opposed to simply tracking opacity over mass density, because of this small dynamic range when compared to  $\rho$  ( $\rho \sim 10^5$  [g cm<sup>-3</sup>] at the core of an RGB star all the way down to  $\sim 10^{-8}$  [g cm<sup>-3</sup>] within the envelope).

OPLIB tables are queried from a web interface<sup>1</sup>. In 224 order to generate many tables easily and quickly we 225 develop a web scraper built with Python's requests 226 module in addition to the 3rd party mechanize and 227 BeautifulSoup modules (Chandra & Varanasi 2015; 228 Richardson 2007) which can automatically retrieve all 229 the tables needed to build an opacity table that DSEP 230 can make use of. This web scraper submits a user re-231 quested chemical composition (composed of mass frac-232 tions for elements from hydrogen to zinc) to the Los 233 Alamos web form, selects 0.0005 keV as the lower tem-234 perature bound and 60 keV as the upper temperature 235 bound, and finally requests opacity measurements for  $_{236}$  100 densities, ranging from  $1.77827941 \times 10^{-15}$  [g cm<sup>-3</sup>] <sub>237</sub> up to  $1 \times 10^7$  [g cm<sup>-3</sup>], at each temperature interval. 238 These correspond to approximately the same tempera-239 ture and density range of opacities present in the OPAL <sup>240</sup> opacity tables. For a detailed discussion of how OPLIB 241 tables are transformed into a format DSEP can use see 242 Appendix A.

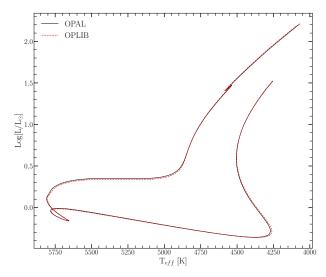
#### 4. SOLAR CALIBRATED STELLAR MODELS

In order to validate the OPLIB opacities, we generate a solar calibrated stellar model (SCSM) using these new tables. We allow both the convective mixing length parameter,  $\alpha_{ML}$ , and the initial Hydrogen mass fraction, X, to vary simultaneously, minimizing the difference between resultant models' final radius and luminosity to those of the sun.

Optimization of  $\alpha_{ML}$  and X is conducted using gra-252 dient descent. For each optimization step three mod-253 els are evolved: a reference model, a model with a 254 small perturbation to the hydrogen mass fraction but 255 the same mixing length as the reference model, and a 256 model with a small perturbation to the mixing length 257 but the same hydrogen mass fraction as the reference. 258 Perturbations are sampled from a normal distribution 259 (using numpy.random). This distribution is sampled and 260 that sample is then added to the reference value for ei-<sub>261</sub> ther X or  $\alpha_{ML}$ . The luminosity and radius of the three 262 evolved models are compared to solar values and the gradient of the resultant  $L-L_{\odot},\ R-R_{\odot}$  surface is fol-264 lowed down to new estimates for the reference values of  $_{265}$  X and  $\alpha_{ML}$ . This process is is repeated until the dif-<sub>266</sub> ference between successive X and  $\alpha_{ML}$  drops below one  $_{267}$  part in  $10^{5}$ .

Solar calibrated stellar models evolved using GS98 OPAL and OPLIB opacity tables (Figure 4) differ  $\sim$  270 0.5% in the SCSM hydrogen mass fractions and  $\sim1.5\%$ 

<sup>&</sup>lt;sup>1</sup> https://aphysics2.lanl.gov/apps/



**Figure 4.** HR Diagram for the two SCSMs, OPAL and OPLIB. OPLIB is shown as a grey dashed line.

Model	X	$\alpha_{ML}$
OPAL	0.7066	1.9333
OPLIB	0.7107	1.9629

**Table 1.** Optimized parameters for SCSMs evolved using OPAL and OPLIB high temperature opacity tables.

271 in the SCSM convective mixing length parameters (Ta-272 ble 1). While the two evolutionary tracks are very simi-273 lar, note that the OPLIB SCSM's luminosity is system-274 atically lower at the same age until the star leaves the 275 main sequence, at which point it is effectively the same 276 as the OPAL SCSM. This luminosity difference between 277 OPAL and OPLIB based models is consistent with ex-278 pectations given the shallow radiative temperature gra-279 dient resulting from the lower OPLIB opacities

# 5. MODELING

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In order to model the Jao Gap we evolve two extremely finely sampled mass grids of models. One of these grids uses the OPAL high-temperature opacity tables while the other uses the OPLIB tables (Figure 5). Each grid evolves a model every  $0.00025~M_{\odot}$  from 0.2 to  $0.4~M_{\odot}$  and every  $0.005~M_{\odot}$  from 0.4 to  $0.8~M_{\odot}$ . All models in both grids use a GS98 solar composition, the (1, 101, 0) Free\_EOS (version 2.7) configuration, and 1000 year old pre-main sequence polytropic models, with polytropic index 1.5, as their initial conditions.

Because in this work we are just interested in the lo-292 cation shift of the Gap as the opacity source varies, we 293 do not model variations in composition. Mansfield & 294 Kroupa (2021); Jao & Feiden (2020); Feiden et al. (2021) 295 all look at the effect composition has on Jao Gap loca-

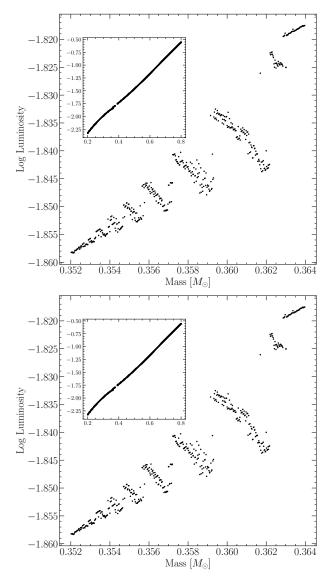


Figure 5. Mass-luminosity relation for models evolved using OPAL opacity tables (top) and those evolved using OPLIB opacity tables (bottom) [UPDATE OPLIB FIG WHEN MODELS DONE]. Note the lower mass range of the OPLIB Gap.

tion. They find that as population metallicity increases so too does the mass range and consequently the magnitude of the Gap. From an extremely low metallicity population (Z=0.001) to a population with a more solar like metallicity this shift in mass range can be up to 0.05  $\rm M_{\odot}$  (Mansfield & Kroupa 2021).

## 5.1. Population Synthethis

In order to compare the Gap to observations we use in house population synthesis code. Our population synthesis code first uses inverse CDF sampling to build a distribution of target masses from some initial mass function (IMF). Specifically we use the Sollima

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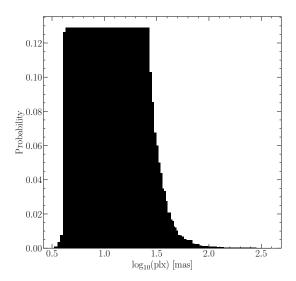
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**Figure 6.** Probability distribution sampled when assigning true parallaxes to synthetic stars. This distribution is built from the GCNS.

 $_{308}$  (2019) IMF where, for masses 0.25  $M_{\odot} < M < 1 M_{\odot},$   $_{309}$   $\alpha = -1.34 \pm 0.07.$  The model nearest in mass to the samples mass above and the nearest model below are then selected from the evolved model database. The surface gravity, luminosity, and effective temperature of the sample are estimated from a linear interpolation between the upper and lower bounding models.  $T_{eff},\ g,$  and  $\log(L)$  are transformed to Gaia G, BP, and RP magnitudes using the Gaia (E)DR3 bolometric corrections (Creevey et al. 2022) along with code obtained thorough personal communication with Aaron Dotter [How to cite Aaron's color code?]. Next, we introduce observationally informed photometric and astrometric uncertainties into our population.

We select the Gaia Catalogue of Nearby Stars (GCNS) (Gaia Collaboration et al. 2021) to empirically calibrate uncertainty relations. A function with the form of Equation 4 is fit to parallax uncertainty vs. G magnitude. Additionally, a function of the form of Equation 5 is fit to to i<sup>th</sup> (G, BP, RP) magnitude uncertainty vs. i<sup>th</sup> magnitude.

$$\sigma_{plx}(M_g) = ae^{bM_g} + c \tag{4}$$

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$$\sigma_i(M_i) = ae^{M_i - b} + c \tag{5}$$

Each of these functions estimates the uncertainty of some quantity at a given magnitude. Moreover, for each sampled star in the synthetic population we select a par337 allax from the distribution in the GCNS (Figure 6), re-338 ferred to as the "true parallax". A parallax uncertainty 339 is calculated based on the empirically calibrated par-340 allax uncertainty and G-magnitude relation along with 341 the synthetic stars G-magnitude (hereafter the "true" 342 G magnitude) and the results of the fitting described in 343 the previous paragraph. This uncertainty is then, with 344 equal weighting, either added or subtracted from the 345 true parallax, yielding an "observed parallax".

The true parallax is used to convert the true i<sup>th</sup> magnitude to an apparent i<sup>th</sup> magnitude and the observed
parallax is used to convert the apparent i<sup>th</sup> magnitude
into an observed i<sup>th</sup> magnitude. Finally, each observed
magnitude is summed with an estimated photometric
uncertainty for that magnitude based on the fit of the
i<sup>th</sup> magnitude to the uncertainty in the i<sup>th</sup> magnitude.

To summarize the process that each synthetic star will go through

- 1. Sample from a Sollima (2019) IMF to determine synthetic star mass.
- 2. Find the closest model above and below the synthetic star, lineally interpolate model parameters to the synthetic star mass.
  - 3. Convert synthetic star g,  $T_{eff}$ , and Log(L) to Gaia G, BP, and RP colors.
  - 4. Sample from the GCNS to assign synthetic star a "true" parallax.
  - 5. Evaluate the empirical calibration given in Equation 4 to find an associated parallax uncertainty and adjust the true parallax by this value resulting in an observed parallax.
  - 6. Use the true parallax to find an apparent magnitude for each filter.
  - 7. Use the observed parallax and the apparent magnitude to find an observed magnitude.
  - 8. Evaluate the empirical calibration given in Equation 5 to give a magnitude uncertainty scale in each band.
  - Adjust each magnitude by some amount sampled from a normal distribution with a standard deviation of the magnitude uncertainty scale.

This method then incorporates both photometric and astrometric uncertainties into our population synthesis. An example 7 Gyr old synthetic populations using OPAL and OPLIB opacities are presented in Figure 7.

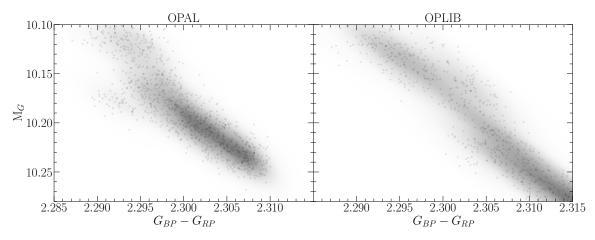


Figure 7. Population synthesis results for models evolved with OPAL (left) and models evolved with OPLIB (right). A Gaussian kernel-density estimate has been overlaid to better highlight the density variations. [THIS IS A PLACEHOLDER FIGURE]

	Model	Location	Prominence
	OPAL	10.15864	0.19501
	OPLIB 1	10.17813	0.26055
	OPLIB 2	10.21313	0.46898

Table 2. Locations identified as potential Gaps.

# 6. RESULTS

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We quantify the Jao Gap location along the magnitude axis by sub-sampling our synthetic populations, finding the linear number density along the magnitude axis of each sub-sample, averaging these linear number densities, and extracting any peaks above some prominence threshold. Once we have the peak location we fit a Gaussian to a window centered at the peak giving both an estimate of the Gap location and the Gap width. Figure 8 shows this fit for both OPAL and OPLIB pop-

Our Gap identification method finds two potential Gaps in the OPLIB (Table 2) data while only finding one in the OPAL dataset. This apparent discrepancy is not due to a fundamental structural difference between the OPAL and OPLIB opacity tables; rather, it sattributable to the phasing of the periodic luminosity variations seen across mass in Figure 5 and whether or not the injected noise smears all of these together into one Gap or two Gaps.

[There will be text detailing a test where I manually shift the OPAL data to the same phase as the OPLIB in an attempt to explain the extra Gap seen in OPLIB].

Both Gaps identified in the OPLIB sample are at fainter magnitudes than the Gap identified in the OPAL sample. Consequently, in the OPLIB sample the convective mixing events which drive the kissing instability happen more regularly and therefore also start earlier in

the model's evolution. This is because each mixing event serves to interrupt the "standard" luminosity evolution of a stellar model, kicking its luminosity back down to what it would have been at some earlier stage of stellar evolution instead of allowing it to slowly increase.

Convective mixing events starting earlier in a model's 416 evolution are consistent with the slightly lower opacities 417 characteristic to OPLIB. A lower opacity fluid will have 418 a more shallow radiative temperature gradient than a 419 higher opacity fluid; however, as the adiabatic temper-420 ature gradient remains essentially unchanged as a func-421 tion of radius, a larger interior radius of the model will 422 remain unstable to convection [CHECK IF THIS OR IF 423 RADIATIVE ZONE MOVING IN]. This larger convec-424 tive zone, and therefore smaller radiative zone, is in line 425 with the behavior of the models presented here as it with 426 the radiative zone closer to the convective zone it takes 427 less time for that radiative zone to heat up and become 428 unstable to convection. We see that OPLIB models un-429 dergo convective mixing events earlier in their evolution 430 than OPAL models (Figure 9) implying that the inner 431 convective zone did not have to expand as much to meet 432 the outer convective zone.

The most precise published Gap location comes from Jao & Feiden (2020) who use EDR3 to locate the Gap at  $M_G \sim 10.3$ , we identify the Gap at a similar location in the GCNS data. The Gap in populations evolved using OPLIB tables is closer to this measurement than it is in populations evolved using OPAL tables (Table 2). It should be noted that the exact location of the observed Gap is poorly captured by a single value as the Gap visibly compresses across the width of the main-sequence, wider on the blue edge and narrower on the red edge such that the observed Gap has downward facing a wedge shape (Figure 1). This wedge

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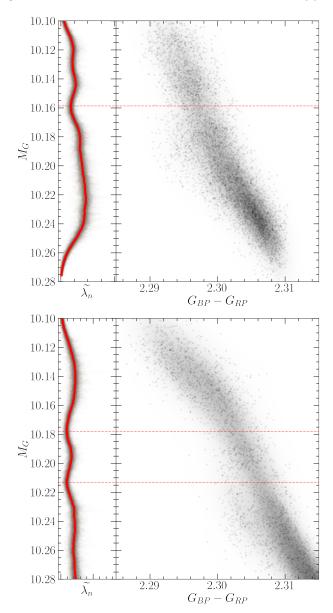


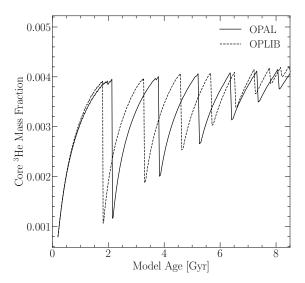
Figure 8. (right panels) OPAL (top) and OPLIB (bottom) synthetic populations. (left panels) Normalized linear number density along the magnitude axis. A dashed line has been extended from the peak through both panels to make clear where the identified Jao Gap location is wrt. to the population.

shape is not successfully reproduced by either any curfrent models or the modeling we preform here. We elect then to specify the Gap location where this wedge is at the its narrowest, on the red edge of the main sequence.

The Gaps identified in our modeling have widths of approximately 0.03 magnitudes, while the shift from OPAL to OPLIB opacities is anywhere from 0.02 to 0.05 magni-

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<sup>452</sup> tudes. With the prior that the Gaps clearly shift before <sup>453</sup> noise is injected we know that this shift is real. How-



**Figure 9.** Core <sup>3</sup>He mass fraction for a model evolved with OPAL and a model evolved with OPLIB within the Jao Gap's mass range. Note how the OPLIB model undergoes the mixing event earlier in its evolution than the OPAL model does.

<sup>454</sup> ever, since the shift magnitude and Gap width are of <sup>455</sup> approximately the same size in our synthetic popula-<sup>456</sup> tions its likely that in a real population — with both <sup>457</sup> compositional and age variations which we do not ac-<sup>458</sup> count for — the Gap location will not provide a <sup>459</sup> usable constraint on the opacity source.

## 7. CONCLUSION

The Jao Gap provides an intriguing probe into the interior physics of M Dwarfs stars where traditional methods of studying interiors break down. However, before
detailed physics may be inferred it is essential to have
models which are well matched to observations. Here
we investigate whether the OPLIB opacity tables reproduce the Jao Gap location and structure more accurately
than the widely used OPAL opacity tables. We find that
while the OPLIB tables do shift the Jao Gap location
more in line with observations the shift is small enough
more in line with observations the shift is small enough
that it is likely not distinguishable from noise due to
population age and chemical variation. Moreover, we
do not find that the OPLIB opacity tables help in re-

APPENDIX

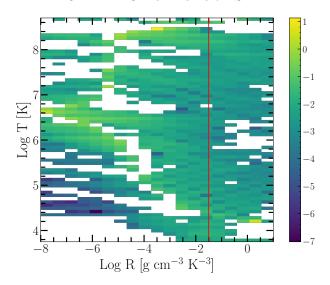


Figure 10. Log Fractional Difference between opacities in  $\kappa_R(\rho, T_{eff})$  space directly queried from the OPLIB web-form and those which have been interpolated into  $\log(R)$  space and back. Note that, due to the temperature grid DSEP uses not aligning perfectly which the temperature grid OPLIB uses there may be edge effects where the interpolation is poorly constrained. The red line corresponds to  $\log(R) = -1.5$  where much of a stellar model's radius exists.

# A. INTERPOLATING $\rho \to R$

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OPLIB reports  $\kappa_R$  as a function of mass density, temperature in keV, and composition. DSEP uses tables where opacity is given as a function of temperature in Kelvin, R, and composition. The conversion from temperature in keV to Kelvin is trivial

$$T_K = T_{keV} * 11604525.0061657 \tag{A1}$$

However, the conversion from mass density to R is more involved. Because R is coupled with both mass density and temperature there is no way to directly convert tabulated values of opacity reported in the OPLIB tables to their equivalents in R space. Instead we must rotate the tables, interpolating  $\kappa_R(\rho, T_{eff}) \to \kappa_R(R, T_{eff})$ .

To preform this rotation we use the interp2d function within scipy's interpolate (Virtanen et al. 2020) module to construct a cubic bivariate B-spline (Dierckx 1981) interpolating function s, with a smoothing factor of 0, representing the surface  $\kappa_R(\rho, T_{eff})$ . For each  $R^i$  and  $T_{eff}^j$  which DSEP expects high-temperature opacities to be reported for, we evaluate Equation 3 to find  $\rho^{ij} = \rho(T_{eff}^j, R^i)$ . Opacities in  $T_{eff}$ , R space are then inferred as  $\kappa_R^{ij}(R^i, T_{eff}^j) = s(\rho^{ij}, T_{eff}^j)$ .

As first-order validation of this interpolation scheme we can preform a similar interpolation in the opposite direction, rotating the tables back to  $\kappa_R(\rho, T_{eff})$  and then comparing the initial, "raw", opacities to those which have gone through the interpolations process. Figure 10 shows the fractional difference between the raw opacities and a set which have gone through this double interpolation. The red line denotes  $\log(R) = -1.5$  where models will tend to sit for much of their radius. Along the  $\log(R) = -1.5$  line the mean fractional difference is  $\langle \delta \rangle = 0.006$  with an uncertainty of  $\sigma_{\langle \delta \rangle} = 0.009$ . One point of note is that, because the initial rotation into  $\log(R)$  space also reduces the domain of the opacity function interpolation-edge effects which we avoid initially by extending the domain past what DSEP needs cannot be avoided when interpolating back into  $\rho$  space.

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The Dartmouth Stellar Evolution Program (Dotter et al. 2008), BeautifulSoup (Richardson 2007), mechanize (Chandra & Varanasi 2015)

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