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# Chemically Self-Consistant Modeling of the Globular Cluster NGC 2808 and its Effects on the Inferred Helium abundance of Multiple Stellar Populations.

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#### ABSTRACT

The Helium abundances in the multiple populations which are now known to comprise all closley studies Milky Way globular clusters are often inferred by fitting isochohrones generated from from stellar evolutionary models to globular cluster photometry. It is therefore important to understand build stellar models that are chemically self-consistent in the compositions of the structure, atmosphere, and opacity. In this work we present the first chemically self-consistent stellar models of the Milky Way Globular Cluster NGC 2808 using MARCS model atmospheres, OPLIB high-temperature radiative opacities, and AESOPUS low-temperature radiative opacities. In order to to this we develope a robust software suite for globular cluster photometry, Fidanka , which can be used for both population synthethis as well as isochrone optimization. Fidanka 's primary goal is to determine, in a relativly unbiased way, the ideal number of populations within photometric dataset to fit isochrones to. We achive this through a combinarion of Baysian Guassian Mixture Modeling and a novel number density estimation algorithm. Using Fidanka and F275W-F814W photometry from the Hubble UV Globular Cluster Survey we find that the helium abundance of the second generation of stars in NGC 2808 is higher than the first generation by  $15 \pm 3\%$ . This is in agreement with previous studies of NGC 2808.

Keywords: Globular Clusters (656), Stellar evolutionary models (2046)

#### 1. INTRODUCTION

Globular clusters (GCs) are among the oldest observable able objects in the universe (Peng et al. 2011). They are characterized by high densities with typical half-light radii of  $\leq$ 10 pc (van den Bergh 2010), and typical masses ranging from  $10^4$ – $10^5$  M $_{\odot}$  (Brodie & Strader 2006) — though some GCs are significantly larger than these typical values EXAMPLE. GCs provide a unique way to probe stellar evolution (Baumgardt & Makino 2003), galaxy formation models (Boylan-Kolchin 2018; Kravtsov & Gnedin 2005), and dark matter halo structure (Hudson & Robison 2018). BRING IN SOME MORE RECENT CITATIONS.

The traditional view of Globular Clusters was, for a long time, that they consisted of a single stellar popusion (SSP, in some publications this is referred to as

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37 a Simple Stellar Population). This view was supported 38 by spectroscopically uniform heavy element abundances 39 (Carretta et al. 2010; Bastian & Lardo 2018) accross  $_{40}$  most clusters (M54 and  $\omega$ Cen are notable exceptions, see 41 Marino et al. (2015) for further details), and the lack of 42 evidence for multiple stellar populations (MPs) in past 43 color-magnitude diagrams of GCs (i.e. Sandage 1953; 44 Alcaino 1975). However, over the last 40 years non-45 trivial star-to-star light-element abundance variations 46 have been observed (i.e. Smith 1987) and, in the last 47 two decades, it has been definitively shown that most if 48 not all Milky Way GCs have MPs (Gratton et al. 2004, 49 2012; Piotto et al. 2015). The lack of photometric evi- $_{50}$  dence for MPs can be attributed to the short color throw 51 available to ground based photometric surveys (Milone 52 et al. 2017); specifically, lacking UV filters. While MPs 53 are chemically distinct from one another, that distinc-54 tion is most prominent when observing with U and B55 filters (Sbordone et al. 2011).

The prevalence of multiple populations in GCs is so distinct that the proposed definitions for what constitutes a globular cluster now often center the existence

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59 of MPs. Whereas, people have have often tried to cate60 gorized objects as GCs through relations between half61 light radius, density, and surface brightness profile, in
62 fact many objects which are generally thought of as GCs
63 don't cleanly fit into these cuts (Peebles & Dicke 1968;
64 Brown et al. 1991, 1995; Bekki & Chiba 2002). Con65 sequently, Carretta et al. (2010) proposed a definition
66 of GC based on observed chemical inhomogeneities in
67 their stellar populations. The modern understanding of
68 GCs then is not simply one of a dense cluster of stars
69 which may have chemical inhomogeneities and multiple
70 populations; rather, it is one where those chemical in71 homogeneities and multiple populations themselves are
72 the defining element of a GC.

All Milky Way globular clusters older than 2 Gyr studied in detail show populations enriched in He, N, and Na while also being deplete in O and C (Piotto et al. 2015; Bastian & Lardo 2018). These light element abundance patterns also are not strongly correlated with variations in heavy element abundance, resulting in spectroscopically uniform Fe abundances between populations. Further, high-resolution spectral studies reveal anti-correlations between N-C abundances, Na-O abundances, and potentially Al-Mg (Sneden et al. 1992; Gratton et al. 2012). Typical stellar fusion reactions can deplete core oxygen; however, the observed abundances of Na, Al, and Mg cannot be explained by the likes of the CNO cycle (Prantzos et al. 2007).

Formation channels for these multiple populations remain a point of debate among astronomers. Most proposed formation channels consist of some older, more
massive, population of stars polluting the pristine cluster media before a second population forms, now enriched in heavier elements which they themselves could
not have generated (for a detailed review see Gratton
et al. 2012). The four primary candidates for these polluters are asymptotic giant branch stars (AGBs, Ventura
et al. 2001; D'Ercole et al. 2010), fast rotating massive stars (FRMSs, Decressin et al. 2007), super massive stars (SMSs, Denissenkov & Hartwick 2014), and
massive interacting binaries (MIBs, de Mink et al. 2009;
Bastian & Lardo 2018).

Hot hydrogen burning (proton capture), material transport to the surface, and material ejection into the intra-cluster media are features of each of these models and consequently they can all be made to qualitatively agree with the observed elemental abundances. Howto ever, none of the standard models can currently account for all specific abundances (Gratton et al. 2012). AGB and FRMS models are the most promising; however, both models have difficulty reproducing severe O depletion (Ventura & D'Antona 2009; Decressin et al. 2007).

Moreover, AGB and FRMS models require significant mass loss ( $\sim 90\%$ ) between cluster formation and the current epoch — implying that a significant fraction of halo stars formed in GCs (Renzini 2008; D'Ercole et al. 2008; Bastian & Lardo 2015).

In addition to the light-element anti-correlations ob-117 served it is also known that younger populations are sig-118 nificantly enhanced in Helium (Piotto et al. 2007, 2015; 119 Latour et al. 2019). Depending on the cluster, Helium  $_{120}$  mass fractions as high as Y = 0.4 have been inferred 121 (e.g Milone et al. 2015a). However, due to the relatively 122 high and tight temperature range of partial ionization 123 for He it cannot be observed in globular clusters; conse-124 quently, the evidence for enhanced He in GCs originates 125 from comparison of theoretical stellar isochrones to the 126 observed color-magnitude-diagrams of globular clusters. 127 Therefore, a careful handling of chemistry is essential 128 when modeling with the aim of discriminating between 129 MPs; yet, only a very limited number of GCs have yet 130 been studied with chemically self-consistent (structure 131 and atmosphere) isochrones (e.g. Dotter et al. 2015, 132 NGC 6752).

NGC 2808 is the prototype globular cluster to host 134 Multiple Populations. Various studies since 2007 have 135 identified that it may host anywhere from 2-5 stellar 136 populations. These populations have been identified 137 both spectroscopically (i.e. ) and photometrically (i.e. 138 ). Note that recent work (Valle et al. 2022) calls into 139 question the statistical significance of the detections of 140 more than 2 populations in the spectroscopic data. Here 141 we present new, chemically self-consistent modeling of 142 the photometry of the two extreme populations of NGC 143 2808 identified by Milone et al. (2015a), populations 144 A and E. We use archival photometry from the Hub-145 ble UV Globular Cluster Survey (HUGS) (Piotto et al. 146 2015; Milone et al. 2017) in the F275W and F814W passbands to charecterize multiple populations in NGC 2808 148 (Milone et al. 2015a,b). Additionally, we present a like-149 lihood analysis of the photometric data of NGC 2808 150 to determine the number of populations present in the 151 cluster.

#### 2. CHEMICAL CONSISTENCY

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There are three primary areas in which must the stellar models must be made chemically consistent: the atmospheric boundary conditions, the opacities, and interior abundances. The interior abundances are relatively easily handled by adjusting parameters within our stellar evolutionary code. However, the other two areas are more complicated to bring into consistency. Atmospheric boundary conditions and opacities must both be calculated with a consistent set of chemical abundances use the Dartmouth Stellar Evolution Program (DSEP) (Dotter et al. 2008), a well tested 1D stellar evolution rode which has a particular focus on modelling low mass stars ( $\leq 2~{\rm M}_{\odot}$ )

# 2.1. Atmospheric Boundary Conditions

Certain assumptions, primarily that the radiation field at equilibirum and radiative transport is diffusive 169 IS (Salaris & Cassisi 2005), made in stellar structure codes, such as DSEP, are valid when the optical depth of a star 172 is small. However, in the atmospheres of stars, the number density of particles drops low enough and the optical depth consequently becomes large enough that these asumptions break down, and separate, more physically 176 motivated, plasma modeling code is required. Generally structure code will use tabulated atmospheric boundary 178 conditions generated by these specialized codes ATLAS9 (Kurucz 1993), PHEONIX (Husser et al. 2013), MARCS Gustafsson et al. 2008), and MPS-ATLAS (Kostogryz et al. 2023). Often, as the boundary conditions are both expensive to compute and not the speciality of stellar 183 structure researchers, the boundary conditions are not updated as as light-element interior abundance varies. 184

One key element when chemically consistently mod-185 186 eling NGC 2808 modeling is the incorporation of new 187 atmospheric models with the same elemental abundances as the structure code. We use atmospheres 189 generated from the MARCS grid of model atmospheres 190 (Plez 2008). MARCS provides one-dimensional, hydrostatic, plane-parallel and spherical LTE atmospheric 192 models (Gustafsson et al. 2008). Model atmospheres 193 are made to match the spectroscopically measured elemental abundances of populations A and E. Moreover, 195 for each populations, atmospheres with various helium mass fractions are generated. These range from Y=0.24 197 to Y=0.36 in steps of 0.02. All atmospehric models are 198 computed to an optical depth of  $\tau = 100$  where their temperature and pressures serves as boundary condi-200 tions for the strudcure code. A comparison of the pressure and temperature throughout the atmospheres of the two populations with helium abundances representative of literature values is shown in Figure 2.1.

# 2.2. Opacities

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In addition to the atmospheric boundary conditions, both the high and low temperature opacities used by DSEP must be made chemically consistent. Here we use OPLIB high temperature opacity tables (Colgan et al. 209 2016) retrieved using the TOPS web-interface. Low temperature opacity tables are retrieved from the Aesopus 2.0 web-interface (Marigo & Aringer 2009; Marigo

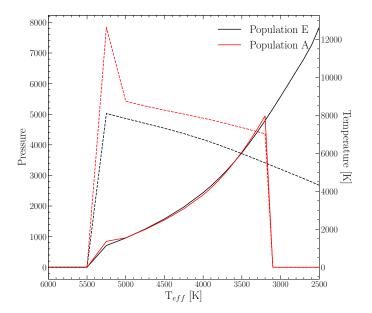


Figure 1. Comparison of the MARCS model atmospheres generated for the two extreme populations of NGC 2808. These lines shows population A and E with the same Helium abundance; though, we fit a grid of models over various helumn abundances. Dashed lines show the temperature of the boundary condition while sold lines show the pressure.

212 et al. 2022). Ideally, these opacities would be the same 213 used in the atmospheric models. However, the opacities 214 used in the MARCS models are not publicly available. 215 As such, we use the opacities provided by the TOPS and 216 Aesopus 2.0 web-interfaces.

# 3. STELLAR MODELS

We use the Dartmouth Stellar Evolution Program (DSEP, Dotter et al. 2008) to generate stellar modeline els. DSEP is a well-tested, one-dimensional stellar evolution code which includes a mixing length model of convection, gravitational settling, and diffusion. Using the solar composition presented in (Grevesse et al. 2007) (GAS07), MARCS model atmosphers, OPLIB high temperature opacities, and AESOPUS 2.0 low temperature opacities we find a solar calibrated mixing length parameter,  $\alpha_{MLT}$ , of  $\alpha_{MLT} = 1.901$ .

We use DSEP to evolve stellar models ranging in mass from 0.3 to 2.0 solar masses from the zero-age main sequence (ZAMS) to the tip of the red giant branch. Below 0.7  $M_{\odot}$  we evolve a model every 0.03  $M_{\odot}$  and above 0.7 we evolve a model every 0.5  $M_{\odot}$ . Additionally, we evolve models over a grid of mixing length parameters from  $\alpha_{MLT}=1.0$  to  $\alpha_{MLT}=2.0$  in steps of 0.1. In addition to the mixing length grid the evolved grid of models also has dimensions population (A or E) (Table 1) and helium abundance (Y=0.24,0.27,0.3,0.33,0.36,0.39).

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Each model is evolved in DSEP with typical numeric tolerences of one part in WHAT, and an average of WHAT shells. Each model is allowed a maximum time step of Myr.

For each combination of population, Y, and  $\alpha_{MLT}$  we use the isochrone generation code first presented in Dotter (2016) to generate a grid of isochrones. The isochrone generation code identified equivalent evolutionary points (EEPs) over a series of masses and interpolates between them. The grid of isochrones generated for this work is avalible as a digital supplement to this paper. Given the complexity of the parameter space when fitting multiple populations along with the recent warnings in the liteerature regarding overfitting datasets (e.g. Valle et al. 2022) we want to develop a more objective way of fitting isochrones to photometry than if we were to mark median ridge line positions by hand.

#### 4. FIDANKA

When fitting isochrones to the data we have four main criteria for any method

- The method must be robust enough to work along the entire main sequence, turn off, and much of the subgiant and red giant branchs.
- Any method should consider photometric uncertainty in the fitting process.
- The method should be model independent, weighting any n number of populations equally.
  - The method should be automated and require minimal intervention from the user.

We do not believe that any currently available software is a match for our use case. Therefore, we elect
to develop our own software suite, Fidanka. Fidanka
fi is a python package designed to automate much of the
process of measuring fiducial lines in CMDs, adhering to
the four criteria we lay out above. Primary features of
Fidanka may be separated into three categories: fidutial line measurement, stellar population synthesise, and
isochrone optimization/fitting. Additionally, there are
tillity functions which are detailed in the Fidanka doctime that the series of the series was a suite of the series of t

# 4.1. Fiducial Line Measurement

Fidanka takes a iterative approach to measuring fidu-281 cial lines, the first step of which is to make a "guess" 282 as to the fiducial line. This initial guess is calculated

Table 1. Population Composition

Element	Pop A	Pop E	Element	Pop A	Pop E
Li	-0.08		In	-1.46	
Be	0.25	_	Sn	-0.22	_
В	1.57	_	Sb	-1.25	_
$^{\mathrm{C}}$	6.87	5.91	Те	-0.08	
N	6.42	6.69	I	-0.71	
O	7.87	6.91	Xe	-0.02	_
$\mathbf{F}$	3.43	_	Cs	-1.18	
Ne	7.12	6.7	Ba	1.05	_
Na	5.11	5.7	La	-0.03	_
Mg	6.86	6.42	Се	0.45	
Al	5.21	6.61	Pr	-1.54	
Si	6.65	6.77	Nd	0.29	
P	4.28	_	Pm	-99.0	_
$\mathbf{S}$	6.31	5.89	Sm	-1.3	_
Cl	-1.13	4.37	Eu	-0.61	_
$\operatorname{Ar}$	5.59	5.17	Gd	-1.19	_
K	3.9	_	Tb	-1.96	_
Ca	5.21	_	Dy	-1.16	_
$\operatorname{Sc}$	2.02	_	Но	-1.78	_
Ti	3.82	_	Er	-1.34	_
V	2.8	_	Tm	-2.16	
$\operatorname{Cr}$	4.51	_	Yb	-1.42	
Mn	4.3	_	Lu	-2.16	_
Fe	6.37	_	Hf	-1.41	
Co	3.86	_	Ta	-2.38	
Ni	5.09	_	W	-1.41	_
Cu	3.06	_	Re	-2.0	_
Zn	2.3	_	Os	-0.86	_
Ga	0.78	_	Ir	-0.88	_
Ge	1.39	_	Pt	-0.64	
As	0.04	_	Au	-1.34	_
Se	1.08	_	Hg	-1.09	_
$\operatorname{Br}$	0.28	_	Tl	-1.36	_
Kr	0.99	_	Pb	-0.51	
Rb	0.26	_	Bi	-1.61	
$\operatorname{Sr}$	0.61	_	Po	-99.0	
Y	1.08	_	At	-99.0	
$\operatorname{Zr}$	1.45	_	Rn	-99.0	
Nb	-0.8	_	Fr	-99.0	_
Мо	-0.38	_	Ra	-99.0	_
$\operatorname{Tc}$	-99.0	_	Ac	-99.0	_
Ru	-0.51	_	Th	-2.2	_
Rh	-1.35	_	Pa	-99.0	
Pd	-0.69	_	U	-2.8	

Note—Relative Metal composition used where a(H) = 12. Where the relative composition is the the same for both populations A and E it is only listed in the population A colum for the sake of visual clarity.

References—Milone et al. (2015a)

283 by splitting the CMD into magnitude bins, with uni-284 form numbers of stars per bin (so that bins are cover a 285 small magnitude range over densely populated regions 286 of the CMD while covering a much larger magnitude <sup>287</sup> range in sparsely populated regions of the CMD, such 288 as the RGB). A unimodal Gaussian distribution is then 289 fit to the color distribution of each bin, and the resulting 290 mean color is used as the initial fiducial line guess. This 291 rough fiducial line will approximately trace the area of 292 highest density. The initial guess will be used to verti-293 calze the CMD so that further algorithms can work in -D magnitude bins without worrying about weighting issues caused by varying projections of the evolutionary sequence onto the magnitude axis. Verticalization is pre-297 formed taking the difference between the guess fiducial 298 line and the color of each star in the CMD.

If Fidanka were to simply apply the same algorithm 300 to the verticalized CMD then the resulting fiducial line would likely be a re-extraction of the initial fiducial line 302 guess. To avoid this, we take a more robust, number 303 density based approach, which considers the distribu-304 tion of stars in both color and magnitude space simul-305 taneously. For each star in the CMD we first using introselect partitioning algorithm to select the 50 nearest stars in F814W vs. F275W-F814W space. To 308 account for the case where the star is at an extreme 309 edge of the CMD, those 50 stars include the star it- $_{310}$  self (such that we really select 49 stars + 1). We use 311 qhull<sup>1</sup>(Barber et al. 1996; ?) to calculate the convex 312 hull of those 50 points. The number density at each star then is defined as  $50/A_{hull}$ , where  $A_{hull}$  is the area of the 314 convex hull. Because we use a fixed number of points per star, and a partitioning algorithm as opposed to a 316 sorting algorithm, this method scales like  $\mathcal{O}(n)$ , where is the number of stars in the CMD. This method also 318 intrinsically weights the density of of each star equally 319 as the counting statistics per bin are uniform. We are 320 left with a CMD where each star has a defined number 321 density (Figure 4.1).

Fidanka can now exploit this density map to fit a better fiducial line to the data, as the density map is far more robust to outliers. There are multiple algorithms we implement to fit the fiducial line to the color-density profile in each magnitude bin (Figure 4.1); they are explained in more detail in the Fidanka documentation. However, of most relevance here is the Bayesian Gaussian Mixture Modeling (BGMM) method. BGMM is a clustering algorithm which, for some fixed number of n-dimensional Gaussian distributions, K, determines the

332 mean, covariance, and mixing probability (somewhat analogous to amplitude) of each  $k^{th}$  distribution, such 334 that the local lower bound of the evidence of each star 335 belonging strongly to a single distribution is maximized. Maximization is preformed using the Dirichlet pro-337 cess, which is a non-parametric Bayesian method of  $_{338}$  determining the number of Gaussian distributions, K, 339 which best fit the data (Ferguson 1973; Pedregosa et al. 340 2011). Use of the Dirichlet process allows for dynamic 341 variation in the number of inferred populations from 342 magnitude bin to magnitude bin. Specifically, popula-343 tions are clearly visually separated from the lower main 344 sequence through the turn off; however, at the turn off 345 and throughout much of the subgiant branch, the two 346 visible populations overlap due to their extremely simi-<sup>347</sup> lar ages (i.e. Jordán et al. 2002). The Dirichlet process 348 allows for the BGMM method to infer a single popula-349 tion in these regions, while inferring two populations in 350 regions where they are clearly separated. More gener-351 ally, the use of the Dirichlet process removes the need 352 for a prior on the exact number of populations to fit. 353 Rather, the user specifies a upper bound on the num-354 ber of populations within the cluster. An example bin  $_{355}$  (F814W = 20.6) is shown in Figure 4.

Fidanka 's BGMM method first breaks down the ver-357 ticalized CMD into magnitude bins with uniform num-358 bers of stars per bin (here we adopt 250). Any stars 359 left over are placed into the final bin. For each bin a 360 BGMM model with a maximum of 5 populations is fit 361 to the color density profile. The number of populations 362 is then inferred from the weighting parameter (the mix-363 ing probability) of each population. If the weighting parameter of any  $k^{th}$  components less than 0.05, then that 365 component is considered to be spurious and removed. 366 Additionally, if the number of populations in the bin 367 above and the bin below are the same, then the num-368 ber of populations in the current bin is forced to be the 369 same as the number of populations in the bin above. Fi-370 nally, the initial guess fiducial line is added back to the 371 BGMM inferred line. Figure 5 shows the resulting fidu-<sup>372</sup> cial line(s) in each magnitude bin for both a verticalized 373 CMD and a non verticalized CMD.

This method of fiducial line extraction effectively discriminated between multiple populations long the main sequence and RGB of a cluster, while simultaneously allowing for the presence of a single population along the MSTO and subgiant branch.

We can adapt this density map based BGMM method to consider photometric uncertainties by adopting a simple Monte Carlo approach. Instead of measuring the fiducial line(s) a single time, Fidanka can measure the fiducial line(s) many times, resampling the data with re-

<sup>&</sup>lt;sup>1</sup> https://www.qhull.com

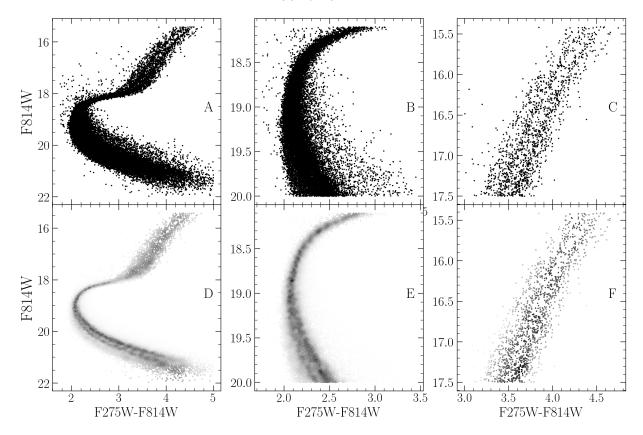
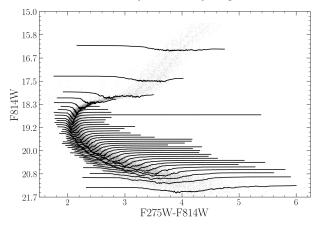


Figure 2. Density map demo showing density estimate over different parts of the evolutionary sequence. The left panel shows the density map over the entire evolutionary sequence, while the middle panel shows the density map over the main sequence and the right most panel shows the density map over the RGB. Figures in the top row are the raw CMD, while figures in the bottom row are colored by the density map.



**Figure 3.** CMD where points are colored by density. Lines show the density-color profile in each magnitude bin. In this figure adaptive binning targeted 1000 stars per bin

placement each time. For each resampling Fidanka adds arandom offset to each filter based on the photometric uncertainties of each star. From these n measurments the mean fiducial line for each sequence can be identified along with upper and lower bound confidence intervals in each magnitude bin.

### 4.2. Stellar Population Synthesis

In addition to measuring fiducial lines, Fidanka also includes a stellar population synthesise module. This module is used to generate synthetic CMDs from a given set of isochrones. This is of primary importance for binary population modelling. The module is also used to generate synthetic CMDs for the purpose of testing the fiducial line extraction algorithms against priors.

Fidanka uses MIST formatted isochrones (Dotter 2016) as input along with distance modulus, B-V color excess, binary mass fraction, and bolometric corrections. An arbitrarily large number of isochrones may be used to define an arbitrary number of populations. Synthetic stars are samples from each isochrone based on a definable probability (for example it is believed that  $\sim 90\%$  of stars in globular clusters are younger population (e.g. Suntzeff & Kraft 1996; Carretta 2013)). Based on the metallicity,  $\mu$ , and E(B-V) of each isochrone, bolometric corrections are taken from bolometric correction tables. Where bolometric correction tables do not include exact metallicities or extinctions a linear interpolation is preformed between the two bounding values.

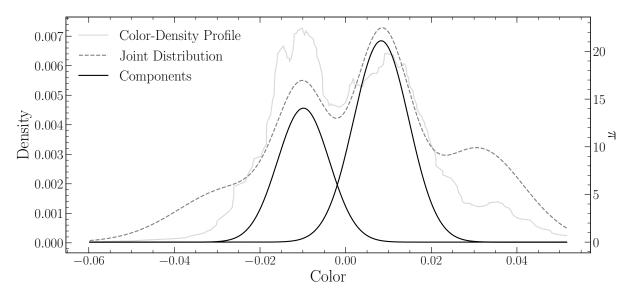


Figure 4. Example of BGMM fit to a magnitude bin. The grey line shows the underlying color-density profile, while the black dashed-line shows the joint distribution of each BGMM component. The solid black lines show the two selected components.

# 4.3. Isochrone Optimization

The optimization routines in Fidanka will find the best fit distance modulus, B-V color excess, and binary number fraction for a given set of isochrones. If a sin- gle isochrone is provided then the optimization is done by minimizing the  $\chi^2$  of the perpendicular distances between an isochrone and a fiducial line. If multiple isochrones are provided then those isochrones are first used to run stellar population synthesis and generate a synthetic CMD. The optimization is then done by min- imizing the  $\chi^2$  of both the perpendicular distances between and widths of the observed fiducial line and the fiducial line of the synthetic CMD.

# 4.4. Fidanka Testing

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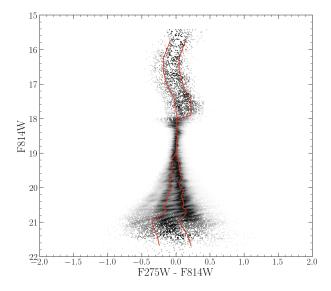
In order to validate fidanka we have run an series of 426 injection recovery tests using Fidanka's population syn-427 thesis routines to build various synthetic populations and Fidanka 's fiducial measurement routines to recover 430 these populations. Each population was generated using the initial mass function given in (Milone et al. 2012) for the redmost population ( $\alpha = -1.2$ ). Further, every 433 population was given a binary population fraction of 10%, distance uniformly sampled between 5000pc and 435 15000pc, and a B-V color excess uniformly sampled be-436 tween 0 and 0.1. Finally, each synthetic population was generated using a fixed age uniformly sampled between Gyr and 14 Gyr. An example synthetic population along with its associated best fit isochrone are shown in 440 Figure 6.

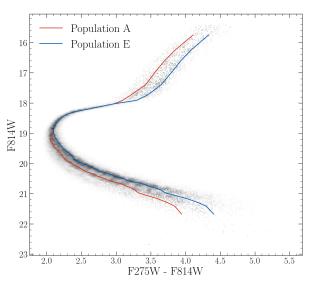
For each trial we use Fidanka to measure the fiducial line and then optimize that fiducial line against the originating isochrone to esimate distance modulus, age, and color B-V excess. Figure 7 is built from 1000 runs of these trials and show the mean and width of the percent error distributions for  $\mu$ , E(B-V), and age. In general Fidanka is able to recover distance modulii effectively with age and E(B-V) reovery falling in line with other literature that does not cosider the CMD outside of the main sequence, main sequence turn off, sub giant, and red giant branches; specifically, it should be noted that Fidanka is not setup to model the horizontal branch.

# 5. ISOCHRONE FITTING

We fit pairs of isochrones to the HUGS data for NGC 2808 using Fidanka , as described in §FIDANKA SEC-TION. Two isochrones, one for Population A and one for Population E are fit simultaneously. These isochrones are constrained to have distance modulus,  $\mu$ , and color excess, E(B-V) which agree to within 1%. Moreover, we constrain the mixing length,  $\alpha_{ML}$ , for any two isochrones in a set to be within 0.5 of one and other. For every isochrone in the set of combination of which fulfilling these constraints  $\mu$ , E(B-V),  $Age_A$ , and  $Age_B$  are optimized to reduce the  $\chi^2$  distance between the fiducial lines and the isochrones. Because we fit fiducial lines directly, we do not need to consider the binary population fraction,  $f_{bin}$ , as a free parameter.

The best fit isochrones are shown in Figure 5 and optimized parameters for these are presented in Table 5. We find helium mas fractions which are consistent with those identified in past literature (e.g. Milone et al. Note that our helium mass fraction gird has a spacing of 0.03 between grid points and we are therefore unable to resolve between certain proposed helium mass





**Figure 5.** CMD where points are colored by density. Line trace the infered fiducial line(s) in each magnitude bin.

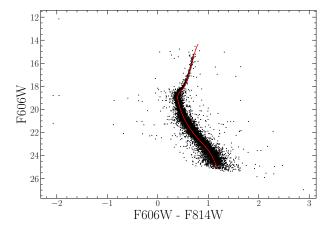
fractions for the younger sequence (for example between 0.37 and 0.39).

Past literature (e.g. Milone et al. 2015a, 2018) have found helium mass fraction variation from the low red-most to bluemost populations of  $\sim 0.12$ . Here we find a helium mass fraction variation of 0.15 which, given the spacing of the helium grid we use is consistent with these past results.

# 5.1. The Number of Populartions in NGC 2808

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In order to estimate the number of populations which ideally fit the NGC 2808 F275W-F814W photometry without overfitting the data we make use of silhouette analysis (Rousseeuw 1987, and in a similar manner to how Valle et al. (2022) preform their analysis of spectro-



**Figure 6.** Synthetic population generated by fidanka at 10000pc with E(B-V) = 0, and an age of 12 Gyr along with the best fitting isochrone. The best fit paremeters are derived to be mu = 15.13, E(B-V) = 0.001, and an age of 12.33 Gyr.

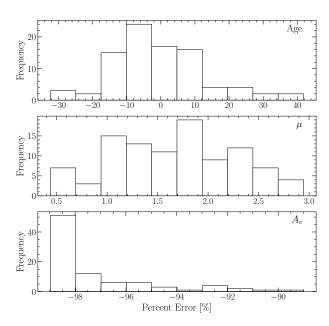


Figure 7. Percent Error distribution for each of the three deriver parameters. Note that these values will be sensitive to the magnitude uncertainties of the photometry. Here we made use of the ACS artificial star tests to estimate the uncertanties. Note that currently this is built with 100 runs, these take a long time so currently re running with 1000 runs.

489 scopic data). We find the average silhouette score for all 490 tagged clusters identified using BGMM in all magnitude 491 bins over the CMD using the standar python module 492 sklearn. Figure 9 shows the silhouette analysis results 493 and that 2 populations fit the photometry most ideally. 494 This is in line with what our BGMM model predicts for 495 the majority of the the CMD.

5.2. ACS-HUGS Photometric Zero Point Offset

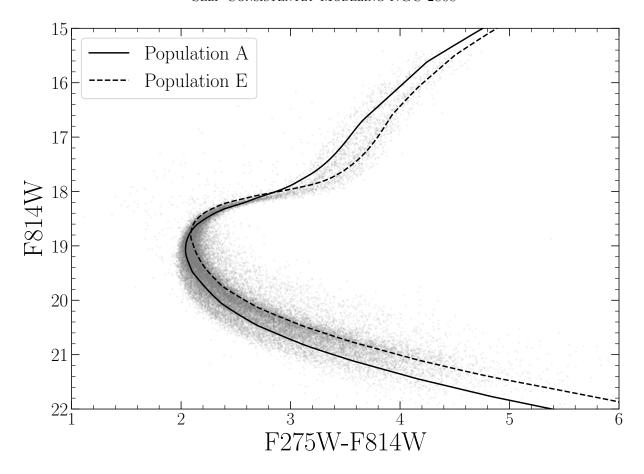


Figure 8. Best fit isochrone results for NGC 2808.

population	age	distance modulus	extinction	Y	$\alpha_{ML}$	$\chi^2_{\nu}$
	[Gyr]		[mag]			
A	12.3	14.91	0.54	0.24	1.901	0.014
E	14.3	14.96	0.54	0.39	1.750	0.017

Table 1. Best fit parameters derived from fitting isochrones to the fiducual lines derived from the NCG 2808 photometry.

The Hubble legacy archive photometry used in this work is calibrated to the Vega magnitude system. How- ever, we have found that the photometry has a system- atic offset of  $\sim 0.026$  magnitudes in the F814W band when compared to the same stars in the ACS survey (Figure 5.2). The exact cause of this offset is unknown, but it is likely due to a difference in the photometric zero point between the two surveys. A full correction of this offset would require a careful re-reduction of the HUGS photometry, which is beyond the scope of this work. We instead recognize a 0.02 inherent uncertainty in the inferred magnitude of any fit when comparing to the ACS survey. This uncertainty is small when compared to the uncertainty in the distance modulus and should not affect the conclusion of this paper.

The oberved photometric offset between ACS and HUGS reductions introduces a systematic uncertainity when comparing parameters derived from isochrone fits to ACS data vs those fit to HUGS data. Specifically, this offset introduces a ~AGE Gyr uncertainity. More-over, for two isochrone of the same age, only seperated by helium mass fraction, a shift of the main sequence turn off of is also expected. Figure 11 shows this shift. Note a change in the helium mass fraction of a model by 0.03 results in an approximate 0.08 magnitude shift to the main sequence turn off location. This means that the mean 0.026 magnitude offset we find in between ACS and HUGS data corresponds to an additional approaximate 0.01 uncertainity in the derived helium mass fraction when comparing between these two datasets.

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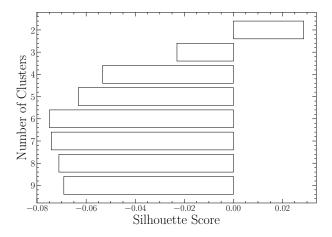


Figure 9. Silhouette analysis for NGC 2808 F275W-F814W photometry. The Silhouette scores are an average of score for each magnitude bin. Positive scores incidate that the clustering algorithm produced well distinguised clusters while negative scores indicate clusters which are not well distinguised.

#### 6. CONCLUSION

Here we have preformed the first chemically self-529 consistnent modeling of the Milky Way Globular Cluster 530 NGC 2808. We find that, updated atmospheric bound-531 ary conditions and opacity tables do not have a signifi-532 cant effect on the inferred helium abundances of multiple 533 populations.

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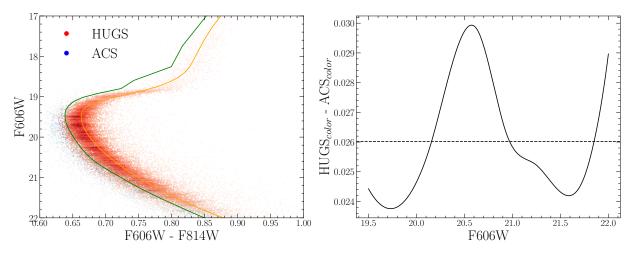


Figure 10. (left) CMD showing the photometric offset between the ACS and HUGS data for NGC 2808. CMDs have been randomly subsampled and colored by point density for clarity. (right) Mean difference between the color of the HUGS and ACS fiducual lines at the same magnitude. Note that the ACS data is systematically bluer than the HUGS data.

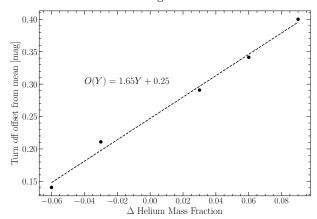


Figure 11. Main sequence turn off magnitude offset from a guage helium mass fraction (Y=0.30 chosen). All main sequence turn off locations are measured at 12.3 Gyr Should I make these contour surfaces for various ages?

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