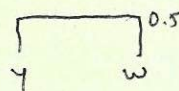


① a) X: TACCCGAT
 Y: TAAACGAT
 Z: AAAACGCG
 W: AAAACGAT

Hamming Distance Matrix

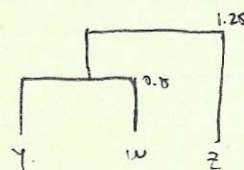
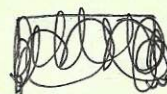
	X	Y	Z	W
X	0	2	5	3
Y		0	3	1
Z			0	2
W				0



	X	Z	YW
X	0	5	2.5
Z		0	2.5
YW			0

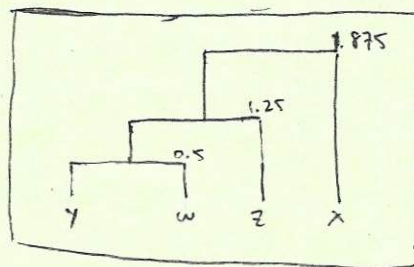
$$d(YW, X) = \frac{d(Y, X) + d(W, X)}{2} = \frac{2+3}{2} = 2.5$$

$$d(YW, Z) = \frac{d(Y, Z) + d(W, Z)}{2} = \frac{3+2}{2} = 2.5$$



	X	ZYW
X	0	3.75
ZYW		0

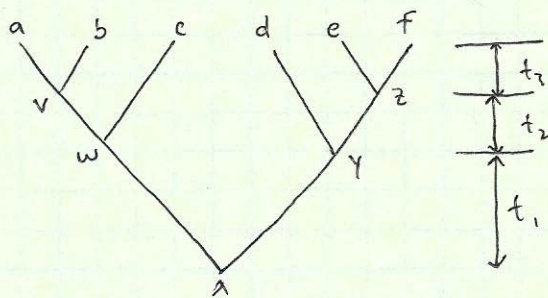
$$d(ZYW, X) = \frac{d(Z, X) + d(YW, X)}{2} = \frac{5+2.5}{2} = 3.75$$



This tree is not ultrametric

* See part b) on bootstrapping in the attached matlab code

② Show the expression for obtaining $\Pr(a, b, c, d, e, f | T, M)$



$P_{xy}(t_1) \sim$ prob of going from x to y in time, t_1

$$\Pr(a, b, c, d, e, f | T, M) = \sum_x \sum_y \sum_z \sum_w \sum_v \Pr(x) \left[P_{xy}(t_1) \cdot P_{yd}(t_2 + t_3) \cdot P_{yz}(t_2) \cdot P_{ze}(t_3) \cdot P_{zf}(t_3) \cdot P_{xw}(t_1) \cdot P_{wc}(t_2 + t_3) \cdot P_{wv}(t_2) \cdot P_{vb}(t_3) \cdot P_{va}(t_3) \right]$$