

✦ AL FM Discrete

Mixed Strategies, (TeX)

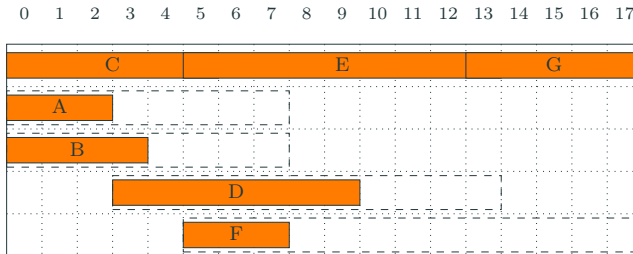
April 28, 2021

Gantt Chart

Definition

A Gantt Chart (also known as a Cascade Chart) has the following features:

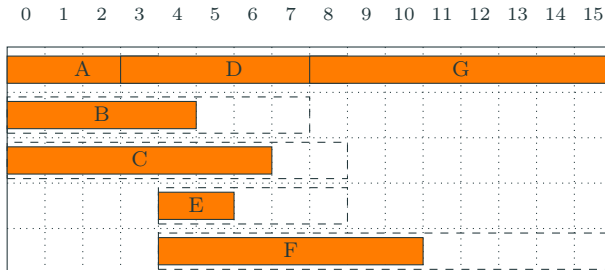
- * Activities are represented by horizontal bars, beginning at their earliest start times.
- * Critical activities are drawn on a single line and all other activities should be drawn on a separate line.
- * the bars are divided into two parts:
 - * The first is the duration of the activity and is usually shaded solidly
 - * The second is the float which is usually given a dotted border
- * Sometimes the number of workers required for each activity may be shown on the bar.



Example

You might have to draw an Activity Network so that you know which activities are on the critical path and the earliest start and slack for the others. For smaller problems though you might be able to do this by inspection.

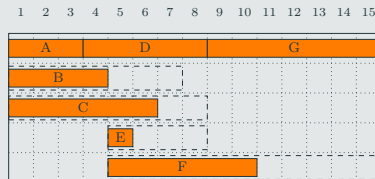
Task	Duration	Immediate predecessors
A	3	
B	4	
C	6	
D	5	A
E	1	B
F	6	B
G	7	C,D,E



Interpreting a Gantt Chart

Problem

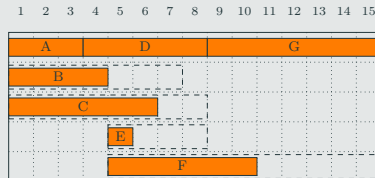
The following Gantt chart represents a project. It transpires that A and B both require use of the same equipment. Can the project still be completed in 15 hours. Give your reasons.



Interpreting a Gantt Chart

Problem

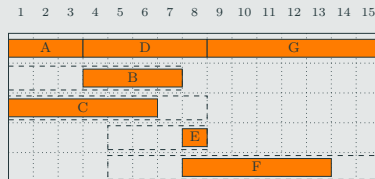
The following Gantt chart represents a project. It transpires that A and B both require use of the same equipment. Can the project still be completed in 15 hours. Give your reasons.



Solution

A and B are originally both scheduled at the same time. Since A is critical, moving A would result in a delay. So consider moving B. This means that E and F must also move.

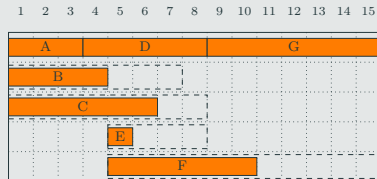
The new cascade diagram shows that moving B so that it starts after A ends, and moving E and F so that they still start after B ends, so the project can still be completed in 15 hours.



Interpreting a Gantt Chart

Problem

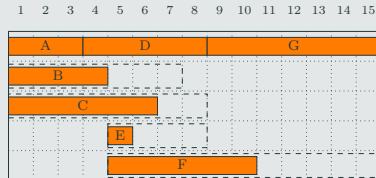
The following Gantt chart represents a project. It now transpires that A and C must be done by a qualified person and there is only one available. Can the project still be completed in 15 hours. Give your reasons.



Interpreting a Gantt Chart

Problem

The following Gantt chart represents a project. It now transpires that A and C must be done by a qualified person and there is only one available. Can the project still be completed in 15 hours. Give your reasons.

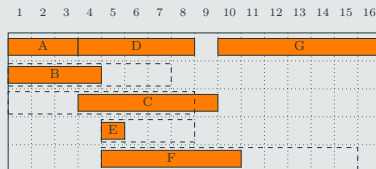


Solution

A and C are currently scheduled together. Again, as A is a critical activity, it is probably better to move C. Note that G depends on C.

In this case, C only has 2 hours of float so moving it by 3 hours means that G is moved by 1 hour. So the whole project is delayed by 1 hour.

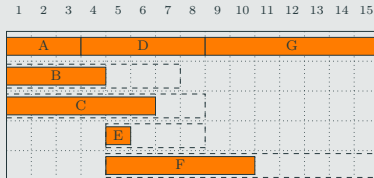
Notice that in the situation above, the critical path has changed. It is now ACG.



Interpreting a Gantt Chart

Problem

The following Gantt chart represents a project. It now transpires that A and C must be done by a qualified person and there is only one available. Can the project still be completed in 15 hours. Give your reasons.

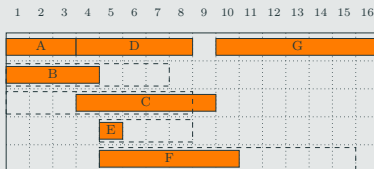


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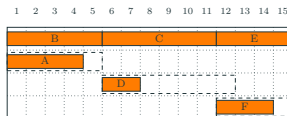
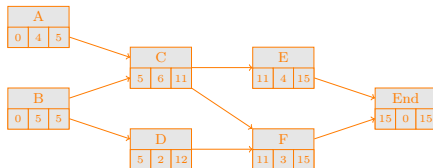
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Resource Histograms

Definition

A resource histogram is based on the Gantt chart but it also shows the number of workers required at each time.



Problem

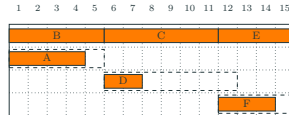
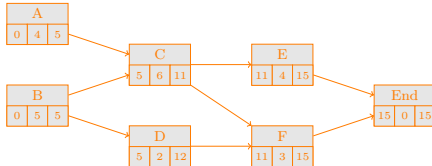
Now also suppose that the activities require the following number of workers:

A:2, B:3, C:1, D:5, E:2, F:4

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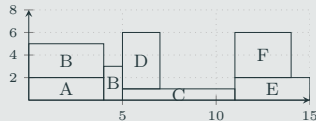


Problem

Now also suppose that the activities require the following number of workers:

A:2, B:3, C:1, D:5, E:2, F:4

Solution



A company is likely to employ a fixed number of people on a full time basis. Hiring people on a temporary basis is expensive and so while a plan showing the minimum possible time in which a project can be completed may be feasible, it might not be practical.

In particular the lumpier the resource histogram, the more likely it is to go above the number of staff available.

Definition

Therefore it is desirable to smooth out the resource histogram as much as possible. This referred to as resource levelling. It is an example of a heuristic procedure meaning that the result is likely to be good but not optimal.

The ideal scenario would be if the resource histogram was entirely flat (i.e. rectangular).

In this case the number of man hours required would be the sum of the areas of all the rectangles and we could then divide by the critical time to find the number of people required.

Resource Levelling I

Problem

The table below shows the activities required to complete a project, with their durations, immediate predecessors and number of workers required.

- * Draw a Gantt Diagram in which all activities are scheduled to start as early as possible.
- * Draw the corresponding Resource Histogram and state how many workers are required.

Task	Duration	Immediate predecessors	Number of workers
A	3		2
B	4		1
C	6		2
D	5	A	2
E	1	B	2
F	6	B	2
G	7	C,D,E	2

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Solution



Resource Levelling I

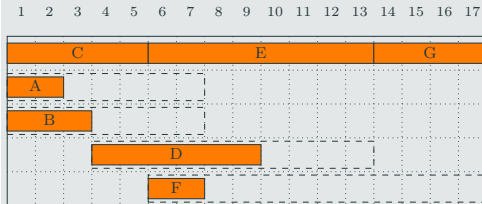
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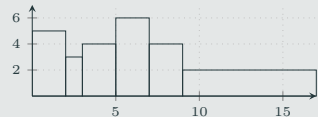
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Solution



Solution



6 Workers required.

Problem

- * Only four workers are available. Is it possible to complete the project in the same amount of time?

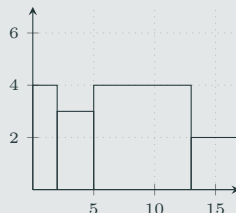
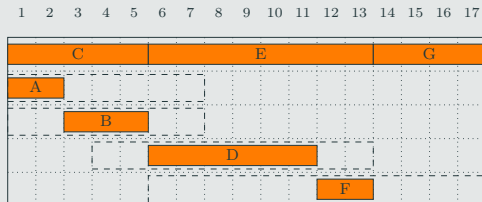
Resource Levelling II

Problem

- ✱ Only four workers are available. Is it possible to complete the project in the same amount of time?

Solution

- ✱ Activity B can be moved forwards to start after A finishes. This means that D must also move forward.
- ✱ Also F can move forward to start after D finishes.



The project can be completed in the same amount of time using 4 Workers.

Problem

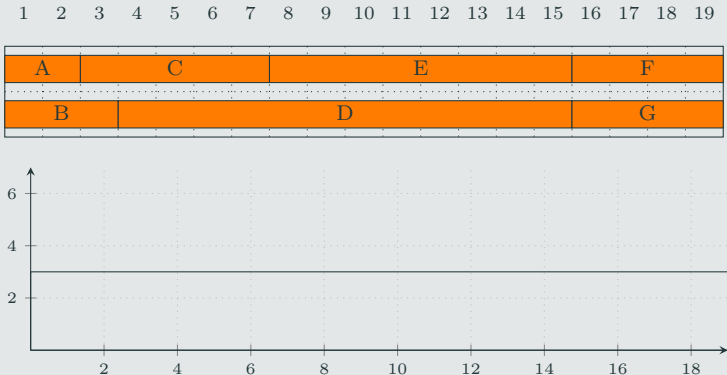
Only three workers are now available. However, both activities D and F can be done by one person, but taking double the amount of time. What is the shortest possible time in which the project can be completed?

Resource Levelling III

Problem

Only three workers are now available. However, both activities D and F can be done by one person, but taking double the amount of time. What is the shortest possible time in which the project can be completed?

Solution



Therefore the project can be completed in 19 days with 3 workers.