

## Chapter 12

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### The Marascuilo Procedure for $\chi^2$

- Used when the null hypothesis of equal proportions is rejected
- Enables you to make comparisons between all pairs
- Start with the observed differences,  $p_j - p_{j'}$ , for all pairs (for  $j \neq j'$ ) then compare the absolute difference to a calculated critical range  
Critical Range for the Marascuilo Procedure:
- Critical Range =  $\sqrt{\chi^2} \sqrt{\frac{p_j(1-p_j)}{n_j} + \frac{p_{j'}(1-p_{j'})}{n_{j'}}}$

(Note: the critical range is different for each pairwise comparison)

A particular pair of proportions is significantly different if:

$$|p_j - p_{j'}| > \text{critical range for } j \text{ and } j'$$

### Marascuilo Procedure Example

A University is thinking of switching to a trimester academic calendar.

A random sample of 100 administrators, 50 students, and 50 faculty members were surveyed:

Opinion	Administrators	Students	Faculty	Total
Favor	63	20	37	120
Opposed	37	30	13	80
Total	100	50	50	200

Using a 1% level of significance, which groups have a different attitude?

### Chi-Square Test Results

$H_0 : \pi_1 = \pi_2 = \pi_3$   $H_1$ : Not all of the  $\pi_j$  are equal ( $j = 1, 2, 3$ )

Opinion	Administrators	Students	Faculty	Total
Favor	o=63, e=60	o=20, e=30	o=37, e=30	120
Opposed	o=37, e=40	o=30, e=20	o=13, e=20	80
Total	100	50	50	200

$$\chi^2_{STAT} = \sum_{All \text{ cells}} \frac{(f_o - f_e)^2}{f_e} = 12.792$$

*Marascuilo Procedure: Solution*

Marascuilo Procedure						
Group	Sample Proportion	Sample Size	Comparison	Absolute Difference	Std. Error of Difference	Critical Range Results
1	0.63	100	1 to 2	0.23	0.084445249	0.2563 Means are not different
2	0.4	50	1 to 3	0.11	0.078606615	0.2386 Means are not different
3	0.74	50	2 to 3	0.34	0.092994624	0.2822 Means are different
Other Data						
Level of significance		0.01	Chi-sq Critical Value		9.2103	
d.f		2				
Q Statistic		3.034854				