

# VE203 Assignment 8

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## Exercise 8.1

By the hint, we can guess that it is about the attack on the Pearl Harbour, and we can find 19 17 19 19, so they are probably “ATTA” in the word “attack”. If we make a deeper guess, the list from 19 in the first column and 8 in the fourth column is “ATTACK PEARL HARBOR”. Then I find on the wiki that the attack happened on Dec 7th, and it just fit the other numbers. So the complete message is “ATTACK PEARL HARBOR DECEMBER SEVEN”.

## Exercise 8.2

$$c = m^e \bmod n = 23^7 \bmod 77 = 23(23 - 77 \times 7)^3 \bmod 77 = 23$$

## Exercise 8.3

Suppose  $g^a, g^b$  are two elements in  $G$

$$g^a \circ g^b = g^{a+b} = g^{b+a} = g^b \circ g^a$$

## Exercise 8.4

$$3^a \equiv 6 \pmod{7}$$

$$3^b \equiv 5 \pmod{7}$$

$$a = 3, b = 5$$

$$5^3 \equiv 6^5 \equiv 6 \pmod{7}$$

So their common secret key is 6

## Exercise 8.5

i) vertices: 6

edges: 6

degrees:  $a_1 = 2, a_2 = 4, a_3 = 1, a_4 = 3, a_5 = 2, a_6 = 0$

	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	$a_6$
$a_1$	0	1	0	1	0	0
$a_2$	1	0	1	1	1	0
$a_3$	0	1	0	0	0	0
$a_4$	1	1	0	0	1	0
$a_5$	0	1	0	1	0	0
$a_6$	0	0	0	0	0	0

- ii) vertices: 6  
edges: 12  
degrees:  $a_1 = 6, a_2 = 5, a_3 = 0, a_4 = 3, a_5 = 5, a_6 = 5$

	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	$a_6$
$a_1$	2	3	0	1	0	0
$a_2$	3	0	0	1	1	0
$a_3$	0	0	0	0	0	0
$a_4$	1	1	0	0	1	0
$a_5$	0	1	0	1	0	3
$a_6$	0	0	0	0	3	2

- iii) vertices: 9  
edges: 10  
degrees:  $a_1 = 2, a_2 = 2, a_3 = 2, a_4 = 0, a_5 = 2, a_6 = 3, a_7 = 2, a_8 = 4, a_9 = 5$

	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	$a_6$	$a_7$	$a_8$	$a_9$
$a_1$	0	0	0	0	0	1	0	0	1
$a_2$	0	0	0	0	0	0	1	0	1
$a_3$	0	0	0	0	0	1	0	1	0
$a_4$	0	0	0	0	0	0	0	0	0
$a_5$	0	0	0	0	0	0	0	0	0
$a_6$	1	0	1	0	0	0	1	0	0
$a_7$	0	1	0	0	0	1	0	0	0
$a_8$	0	0	1	0	0	0	0	0	3
$a_9$	1	1	0	0	0	0	0	3	0

## Exercise 8.6

- i)

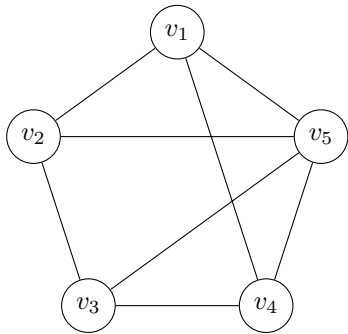
$$V_1 = a, c, V_2 = b, d, e$$

So it is bipartite.

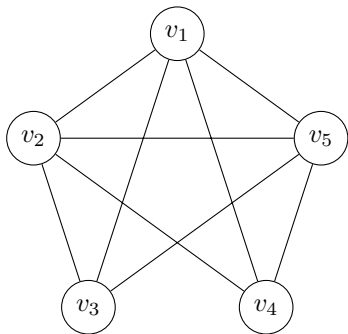
- ii) Since  $b, f, c$  forms a triangle, it is not bipartite.  
iii) Since  $b, e, f$  forms a triangle, it is not bipartite.

## Exercise 8.7

i)



ii)



iii)

