

## —·交大密西根学院·





## **VE230 HW1**

Due: Tuesday 28th May, 2019

P.2-11 Prove that an angle inscribed in a semicircle is a right angle.

**P.2-17** A field is expressed in spherical coordinates by  $E = a_R(25/R^2)$ .

- a) Find  $|\mathbf{E}|$  and  $E_x$  at the point P(-3, 4, -5).
- **b)** Find the angle that **E** makes with the vector  $\mathbf{B} = \mathbf{a}_x 2 \mathbf{a}_y 2 + \mathbf{a}_z$  at point P.

**P.2-21** Given a vector function  $\mathbf{E} = \mathbf{a}_x y + \mathbf{a}_y x$ , evaluate the scalar line integral  $\int \mathbf{E} \cdot d\ell$  from  $P_1(2, 1, -1)$  to  $P_2(8, 2, -1)$ 

- a) along the parabola  $x = 2y^2$ ,
- b) along the straight line joining the two points.

Is this **E** a conservative field?

P.2-26 Find the divergence of the following radial vector fields:

- $\mathbf{a)} \ f_1(\mathbf{R}) = \mathbf{a}_R R^n,$
- $\mathbf{b)} \ f_2(\mathbf{R}) = \mathbf{a}_R \, \frac{k}{R^2}.$

**P.2-29** For vector function  $\mathbf{A} = \mathbf{a_r} r^2 + \mathbf{a_z} 2z$ , verify the divergence theorem for the circular cylindrical region enclosed by r = 5, z = 0, and z = 4.

P.2-33 For two differentiable vector functions E and H, prove that

$$\nabla \cdot (\mathbf{E} \times \mathbf{H}) = \mathbf{H} \cdot (\nabla \times \mathbf{E}) - \mathbf{E} \cdot (\nabla \times \mathbf{H}).$$

**P.2-35** Use the definition in Eq. (2-126) to derive the expression of the  $\mathbf{a}_R$ -component of  $\nabla \times \mathbf{A}$  in spherical coordinates for a vector field  $\mathbf{A} = \mathbf{a}_R A_R + \mathbf{a}_{\theta} A_{\theta} + \mathbf{a}_{\phi} A_{\phi}$ .

$$(\nabla \times \mathbf{A})_{u} = \mathbf{a}_{u} \cdot (\nabla \times \mathbf{A}) = \lim_{\Delta s_{u} \to 0} \frac{1}{\Delta s_{u}} \left( \oint_{C_{u}} \mathbf{A} \cdot d\ell \right), \tag{2-126}$$

**P.2-39** Given a vector function  $\mathbf{F} = \mathbf{a}_x(x + c_1 z) + \mathbf{a}_y(c_2 x - 3z) + \mathbf{a}_z(x + c_3 y + c_4 z)$ .

- a) Determine the constants  $c_1$ ,  $c_2$ , and  $c_3$  if F is irrotational.
- b) Determine the constant  $c_4$  if F is also solenoidal.
- c) Determine the scalar potential function V whose negative gradient equals F.