

Sol. for the cascode amp...

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1 The basics

$$M_1: K_n = 10 \text{ mA/V}^2, V_{TN} = 2 \text{ V}, \lambda = 0.02 \text{ V}^{-1}$$

$$Q_2: \beta_F = 150, V_A = 80 \text{ V}, V_{BE} = 0.7 \text{ V}$$

$$Q_3: \beta_F = 80, V_A = 60 \text{ V}, V_{BE} = 0.7 \text{ V}$$

Analyze this multistage amplifier.

Q-points

$$M_1: Q(I_D, V_{DS}) = (5.00 \text{ mA}, 10.9 \text{ V})$$

$$V_{GS} = -I_D R_{S1} = -0.2 I_D$$

$$I_D = \frac{K_n}{2} (V_{GS} - V_{TN})^2 = 5 (V_{GS} - V_{TN})^2$$

$$V_{GS}^2 + 5V_{GS} + 4 = 0$$

$$V_{GS} = -1$$

$$I_D = 5 (V_{GS} - V_{TN})^2 = 5 (-1 - (-2))^2 = 5 \text{ mA}$$

$$V_{DS} = 15 - I_D (R_{D1} + R_{S1}) = 15 - 5 (0.62 + 0.2) = 10.9 \text{ V}$$

$$Q_2: Q(I_{C2}, V_{CE2}) = (1.51 \text{ mA}, 5.47 \text{ V})$$

$$15 \frac{R_2}{R_1 + R_2} = I_{B2} (R_1 \parallel R_2) + V_{BE2} + (\beta_{F2} + 1) I_{B2} R_{E2}$$

$$I_{B2} = \frac{15 \frac{22}{22+78} - 0.7}{(22 \parallel 78) + (150+1)1.6} \approx 1.005 \times 10^{-2} \text{ mA} \quad I_{C2} = \beta_{F2} I_{B2} = 150 \cdot 1.005 \times 10^{-2} \approx 1.51 \text{ (mA)}$$

$$I_{E2} = I_{B2} + I_{C2} = 1.005 \times 10^{-2} + 1.51 \approx 1.52 \text{ (mA)}$$

$$V_{CE2} = 15 - I_{C2} R_{C2} - I_{E2} R_{E2} = 15 - 1.51 \cdot 4.7 - 1.52 \cdot 1.6 \approx 5.47 \text{ V}$$

$$Q_3: Q(I_{C3}, V_{CE3}) = (1.96 \text{ mA}, 8.45 \text{ V})$$

$$15 \frac{R_4}{R_3 + R_4} = I_{B3} (R_3 \parallel R_4) + V_{BE3} + (\beta_{F3} + 1) I_{B3} R_{E3}$$

$$I_{B3} = \frac{15 \frac{120}{91+120} - 0.7}{(91 \parallel 120) + (80+1)3.3} \approx 2.454 \times 10^{-2} \text{ mA} \quad I_{C3} = \beta_{F3} I_{B3} = 80 \cdot 2.454 \times 10^{-2} \approx 1.96 \text{ (mA)}$$

$$I_{E3} = I_{B3} + I_{C3} = 2.454 \times 10^{-2} + 1.96 \approx 1.98 \text{ (mA)}$$

$$V_{CE3} = 15 - I_{E3} R_{E3} = 15 - 1.98 \cdot 3.3 = 8.45 \text{ V}$$

Small Signal Parameters

$$M_1: g_{m1} = \frac{2I_D}{V_{GS} - V_{TN}} = \frac{2 \cdot 5}{-1 - (-2)} = 10 \text{ mS}$$

$$r_{01} = \frac{1/\lambda + V_{DS}}{I_D} = \frac{1/0.02 + 10.9}{5} \approx 12.2 \text{ k}\Omega$$

$$Q_2: q_{m2} = \frac{I_{C2}}{V_T} = \frac{1.51}{25 \text{ m}} = 60.4 \text{ mS}$$

$$r_{\pi 2} = \frac{\beta_{o2}}{g_{m2}} = \frac{150}{60.4} = 2.48 \text{ k}\Omega$$

$$\begin{aligned}
r_{o2} &= \frac{V_{A2} + V_{CE2}}{I_{C2}} = \frac{80 + 5.47}{1.51} = 56.6k\Omega \\
Q_3 : g_{m3} &= \frac{I_{C3}}{V_T} = \frac{1.96}{25m} = 78.4mS \\
r_{\pi3} &= \frac{\beta_{o3}}{g_{m3}} = \frac{80}{78.4} = 1.02\Omega \\
r_{o3} &= \frac{V_{A3} + V_{CE3}}{I_{C3}} = \frac{60 + 8.45}{1.96} = 34.9k\Omega
\end{aligned}$$

Voltage gain

$$\begin{aligned}
A_v &= \frac{v_o}{v_i} = \frac{v_1}{v_i} \frac{v_2}{v_1} \frac{v_3}{v_2} \frac{v_o}{v_3} = \frac{R_G}{R_I + R_G} A_{vt1}^{CS} A_{vt2}^{CE} A_{vt3}^{CC} \\
A_{vt1}^{CS} &= \frac{v_2}{v_1} \approx -g_{m1}(R_{D1} \parallel R_{B2} \parallel r_{\pi2}) = -10(0.62 \parallel (78 \parallel 22) \parallel 2.48) = -4.82 \\
\mu_{f1} &= -g_{m1}r_{o1} = 10 \cdot 12.2 = 122 \\
A_{vt2}^{CE} &= \frac{v_3}{v_2} \approx -g_{m2}(R_{C2} \parallel R_{B3} \parallel r_{\pi3} + (1 + \beta_{o3})(R_{E3} \parallel R_L)) \\
&= -60.4(4.7 \parallel (91 \parallel 120) \parallel [1.02(1 + 80)(3.3 \parallel 0.25)]) \approx -213 \\
\mu_{f2} &= -g_{m2}r_{o2} = 60.4 \cdot 56.6 = 3419 \\
A_{vt3}^{CC} &= \frac{v_o}{v_3} \approx \frac{(g_{m3}(R_{E3} \parallel R_L))}{1 + g_{m3}(R_{E3} \parallel R_L)} = \frac{78.4(3.3 \parallel 0.25)}{1 + 78.4(3.3 \parallel 0.25)} = 0.95 \\
A_v &= \frac{1000}{10 + 1000} (-4.82)(-213)(.95) = 966
\end{aligned}$$

Input Resistance

$$R_{in} = R_{in1}^{CS} = R_G = 1M\Omega$$

Output resistance

$$\begin{aligned}
R_{out} &= R_{out3}^{CC} = R_{E3} \parallel (r_{\pi3} + R_{th3})/(\beta_{o3} + 1) = 3.3 \parallel (1.02 + 4)/(80 + 1) = 61\Omega \\
R_{th3} &= R_{B3} \parallel (R_{C2} \parallel r_{o2}) = (91 \parallel 120) \parallel (4.7 \parallel 56.6) = 4k\Omega
\end{aligned}$$

Current Gain

$$A_i = \frac{i_o}{i_i} = \frac{V_o(R_I + R_{in})}{v_i R_L} = A_v \frac{R_I + R_{in}}{R_L} = 966 \frac{10 + 1000}{0.25} = 3.90 \times 10^6$$

Power Gain

$$A_p = \frac{v_o i_o}{v_i i_i} = A_v A_i = 966 \cdot 3.90 \times 10^6 = 3.99 \times 10^9$$