

Calderon-Tianna-PS5

May 13, 2025

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[1]: import numpy as np
import matplotlib.pyplot as plt
import pandas as pd
from my_linear_regression import *
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[2]: #open file -> converted to csv for easier readings..
df = pd.read_csv('SNe_least_squares.csv')
# Clean column names
df.columns = df.columns.str.strip().str.replace(',', '')

#filter data to keep low redshifts
df.drop(df[df['z (redshift)'] >= 0.05].index, inplace=True)

#get the distance modulus and convert from megaparsecs
df['distance modulus (mu)'] = pd.to_numeric(df['distance modulus (mu)'],
    errors='coerce')
mu = df['distance modulus (mu)']
distance = distance_modulus(mu, 'megaparsecs')

df #to check the the df update..

#transform filtered data
l_distance = len(distance)
y_obs = np.zeros(l_distance)
x_obs = np.zeros(l_distance)

y_obs = np.log10(distance.to_numpy())
x_obs = np.log10(df['z (redshift)'].to_numpy())

#model y= mx+b' find m 1st make X -> its [xi, 1] and Y -> y_obs
X = np.column_stack((x_obs, np.ones_like(x_obs)))

#call fit_linear model
beta, cov = fit_linear_model (X, y_obs)
m, b0 = beta
```

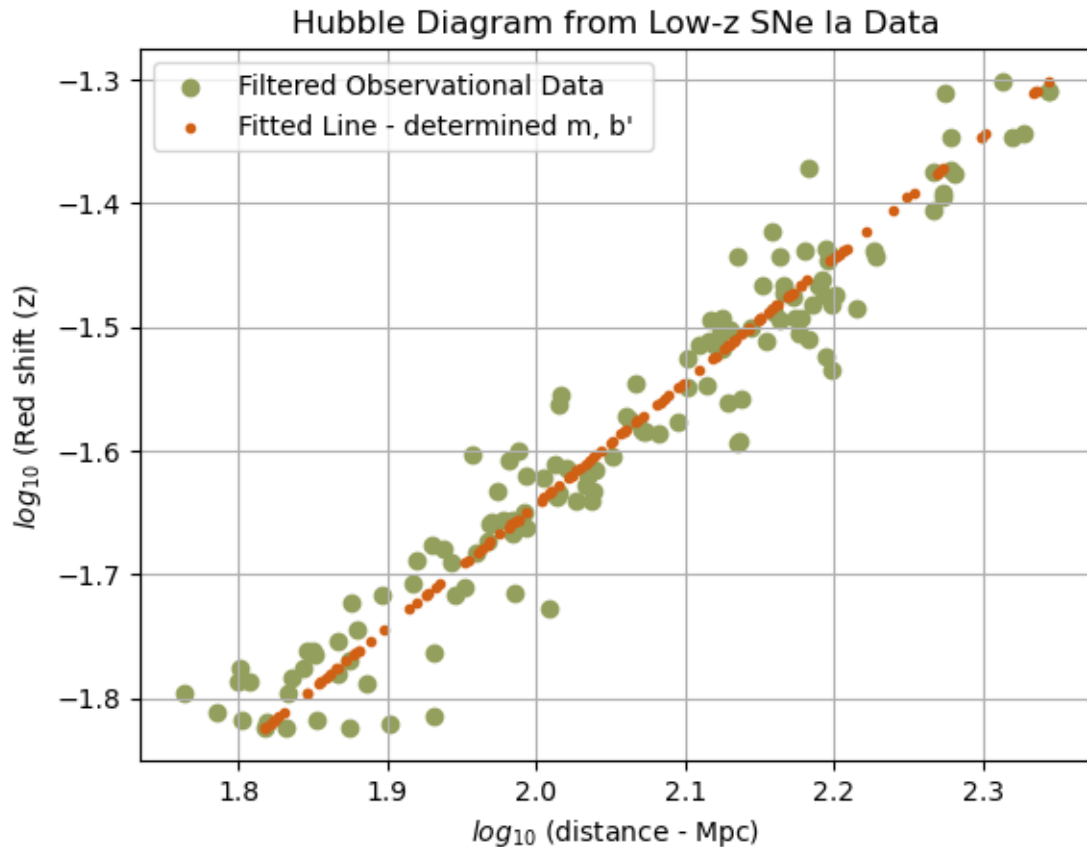
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[3]: #calculate h_0 and uncertainty
se_m, se_b0 = np.sqrt(np.diag(cov))
h0, se_h0 = hubbles_constant(b0, se_b0)

#calc y based on m, b' gathered
y_pred = m*x_obs + b0

fig, ax = plt.subplots() # Correct usage
ax.scatter(y_obs, x_obs, c = '#939F5C', label = "Filtered Observational Data" )
ax.scatter(y_pred, x_obs, c = '#D16014', marker = '.', label = "Fitted Line -
↳determined m, b' " )
ax.grid()
ax.legend()
ax.set_ylabel("$\log_{10}$ (Red shift (z))")
ax.set_xlabel("$\log_{10}$ (distance - Mpc)")
ax.set_title("Hubble Diagram from Low-z SNe Ia Data")

print(f"Slope:{m: .3f} +/- {se_m: .3f} \n Intercept:{b: .3f} +/- {se_b0: .3f}")
print(f"H_0 = {h0:.3f} ± {se_h0:.3f}")
```

```
Slope: 1.006 +/- 0.023
Intercept: 0.290 +/- 0.037
H_0 = 66.607 ± 29.533
```



0.1 Purpose of plot

To see the correlation of distance vs redshift and see how much it deviates from the theoretical

0.2 Analysis

1)

0.2.1 Based on your visual inspection of the plot, does the linear model appear to be a good fit to the filtered data? Explain your reasoning. For instance, do the points generally follow the line? Are there any obvious systematic deviations or outliers?

Based on my visual inspection of the plot the linear does appear to be a good fit to the filtered data. It's actually interesting because there really isn't any high deviation on the plot (for example like a point at the extremities (1.8, -1.0)). The points generally follow the line there may be deviations towards the middle at (2.2, -1.4) but beyond that the points mostly follow the line.

2)

0.2.2 Discussion 1 (Slope): The simplified theoretical model predicts a slope $m = 1$. Does your fitted slope (using the low- z data) significantly deviate from 1 (e.g., is 1 within $m \pm \delta m$, where δm is the standard error of the slope)? Briefly discuss.

Surprisingly, yes the theoretical model matches pretty well to my fitted slope. My result for m was 1.015 which on order of magnitude is the same there is just round-off errors with .015.. I think some of the errors that could have happened to make a value for the slope for m to go higher/lower would probably be unit conversions.

3)

0.2.3 Discussion 2 (H0 Value): Compare your value of H_0 to currently accepted values, which are typically in the range of 67-74 km/s/Mpc). Discuss any discrepancies and potential reasons (e.g., the simplicity of the model even for low z , data limitations, statistical uncertainties, impact of the chosen z -cut).

My H_0 was lower than the accepted value initially (when I had the redshift values at >0.1 but I made a second attempt to lower the accepted values to >0.05). This increased my H_0 Value to 66.607 from 64.651. I think because the data was larger with the >0.1 there was more acceptable uncertainty which led H_0 to be lower. The impact of the chosen z -cut has a large impact overall the output of H_0 being found. I think also because I defined c - speed of light, as $3E10$ from my `astro_constants` module this also made an impact on how the final output H_0 became based on rounding errors.