

Solutions for Assignment 2

1(a)

NFA - aabba:

$$S_0 = \{1\}$$

$$S_1 = \varepsilon\text{-closure}(\{1\}) = \{1, 2, 6\}$$

$$S_2 = \varepsilon\text{-closure}(\text{move}(\{1, 2, 6\}, a)) = \varepsilon\text{-closure}(\{2, 3, 7\}) = \{2, 3, 7, 10\}$$

$$S_3 = \varepsilon\text{-closure}(\text{move}(\{2, 3, 7, 10\}, a)) = \varepsilon\text{-closure}(\{2, 3, 5\}) = \{2, 3, 5, 6, 8\}$$

$$S_4 = \varepsilon\text{-closure}(\text{move}(\{2, 3, 5, 6, 8\}, b)) = \varepsilon\text{-closure}(\{4, 8, 9\}) = \{4, 5, 6, 8, 9\}$$

$$S_5 = \varepsilon\text{-closure}(\text{move}(\{4, 5, 6, 8, 9\}, b)) = \varepsilon\text{-closure}(\{2, 8, 9\}) = \{2, 8, 9\}$$

$$S_6 = \varepsilon\text{-closure}(\text{move}(\{2, 8, 9\}, a)) = \varepsilon\text{-closure}(\{2, 3, 9\}) = \{2, 3, 9\}$$

$$\{2, 3, 9\} \cap \{9, 10\} = \{9\} \Rightarrow \text{Accept}$$

1(b)

NFA - aabab:

$$S_0 = \{1\}$$

$$S_1 = \varepsilon\text{-closure}(\{1\}) = \{1, 2, 6\}$$

$$S_2 = \varepsilon\text{-closure}(\text{move}(\{1, 2, 6\}, a)) = \varepsilon\text{-closure}(\{2, 3, 7\}) = \{2, 3, 7, 10\}$$

$$S_3 = \varepsilon\text{-closure}(\text{move}(\{2, 3, 7, 10\}, a)) = \varepsilon\text{-closure}(\{2, 3, 5\}) = \{2, 3, 5, 6, 8\}$$

$$S_4 = \varepsilon\text{-closure}(\text{move}(\{2, 3, 5, 6, 8\}, b)) = \varepsilon\text{-closure}(\{4, 8, 9\}) = \{4, 5, 6, 8, 9\}$$

$$S_5 = \varepsilon\text{-closure}(\text{move}(\{4, 5, 6, 8, 9\}, a)) = \varepsilon\text{-closure}(\{7, 9\}) = \{7, 9, 10\}$$

$$S_6 = \varepsilon\text{-closure}(\text{move}(\{7, 9, 10\}, b)) = \varepsilon\text{-closure}(\{10\}) = \{10\}$$

$$\{10\} \cap \{9, 10\} = \{10\} \Rightarrow \text{Accept}$$

2(a)

DFA - aabba

S0 = 1

S1 = move(S0, a) = move(1, a) = 2

S2 = move(S1, a) = move(2, a) = 2

S3 = move(S2, b) = move(2, b) = 4

S4 = move(S3, b) = move(4, b) = 7

S5 = move(S4, a) = move(7, a) = 7

7 is in {7, 8} => Accept

2(b)

DFA - aabab

S0 = 1

S1 = move(S0, a) = move(1, a) = 2

S2 = move(S1, a) = move(2, a) = 2

S3 = move(S2, b) = move(2, b) = 4

S4 = move(S3, a) = move(4, a) = 8

S5 = move(S4, b) = move(8, b) = 8

8 is in {7, 8} => Accept