

# Plane fitting with least squares

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Find:  $\underline{a}x + \underline{b}y + \underline{c}z + \underline{d} = 0$

Given: points  $P = n \begin{bmatrix} x & y & z \\ \vdots & \vdots & \vdots \end{bmatrix}$

Use Least Squares:  $Ax = b$

① Four variables are too many! They're connected...

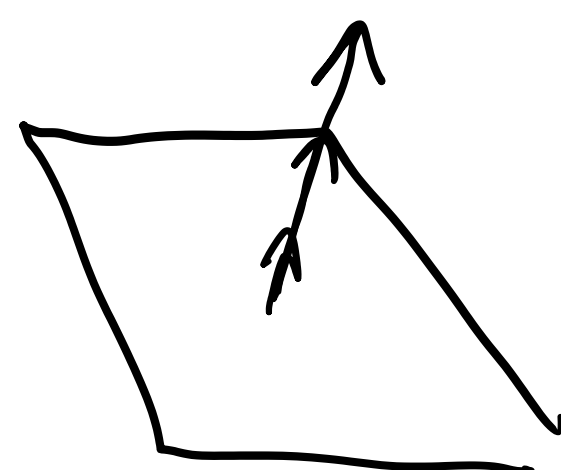
ex)  $[a, b, c, d]$  and  $[-a, -b, -c, -d]$  are the same!

② Normal can be scaled

$$[a, b, c, d] = [2a, 2b, 2c, ?]$$

$$2(ax + by + cz + d = 0)$$

$$2ax + 2by + 2cz + 2d = 0$$



Therefore ... assume  $c = -1$

$$ax + by - z + d = 0$$

$$ax + by + d = z$$

$$\begin{bmatrix} x & y & 1 \\ \vdots & \vdots & \vdots \end{bmatrix} \begin{bmatrix} a \\ b \\ d \end{bmatrix} = \begin{bmatrix} z \\ \vdots \end{bmatrix}$$

$$\begin{bmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ \vdots & \vdots & \vdots \\ x_N & y_N & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ d \end{bmatrix} = \begin{bmatrix} z_1 \\ \vdots \\ z_N \end{bmatrix}$$

$$\begin{matrix} \downarrow \\ A \\ \downarrow \end{matrix} \quad x = b$$

$$a = x(b)$$

$$b = x(c)$$

$$d = x(z)$$

$$c = -1$$