## Dissertation Topic Ideas

### Approximating a Differential Model from Data

**Goal:** Identify best approximation techniques for constructing models of a truth function  $f : \mathbb{R}^d \to \mathbb{R}^b$  of the forms:

```
\hat{f}: \mathbb{R}^{d+\nabla d} \to \mathbb{R}^b
Position + change \to new response value.
\hat{f}: \mathbb{R}^{d+b} \to \mathbb{R}^{\nabla d}
Position + new response \to necessary change.
```

where  $\mathbb{R}^{d+\nabla d}$  denotes the real vector space  $\mathbb{R}^{2d}$  in which the fist half of the vector is the current position and the second half of the vector is the "change" in position. The approximation techniques will be constructed given a row-vector matrix of n nodes  $X^{(n\times d)}$  and response values  $Y^{(n\times b)}$  associated with each node.

**Target:** either TOMS or Mathematics journal depending on which is more feasible (provable properties or quality math software).

#### **Steps:**

- Analyze basic theoretical properties of a model with this form given minimal assumptions (real vector space, Lipschitz continuous truth function, well spaced nodes)
- Pick data (VarSys) to do initial empirical study and convert data into differential form (distance between all pairs)
- Construct models with different approximation techniques
   (Delaunay, Voronoi, Box, NN) and analyze results
- Use empirical results to write a (few) paper(s)
- Develop deeper theory on performance of models and what model

characteristics lead to what outcomes.

 If theoretical results are interesting enough, begin targeting math journal publication, otherwise target math software implementation.

# Provable Properties of Box/Voronoi Meshes for Functional Approximation

**Goal:** Extend my existing mesh-based approximation techniques to functional interpolation and study meaningful provable properties about them.

**Target:** a Mathematics journal publication.

#### **Steps:**

- Establish new method for approximating functions with a function as response value other than forcing weights to be convex (or perhaps not, if it turns out that my current approach is acceptable?)
- Study theoretical properties of the various approximations, what can be maintained and what can't?

## Box/Voronoi Meshes for Functional Approximation Math Software

**Goal:** Extend my existing mesh-based approximation techniques to functional interpolation and generating an optimized and robust code-base for computing them.

Target: TOMS publication.

#### **Steps:**

 Establish new method for approximating functions with a function as response value other than forcing weights to be convex (or perhaps not, if it turns out that my current approach is acceptable?)

 Identify most likely use-case scenario for the routines, develop robust optimized and stable implementation of algorithms (studying potential optimizations in the process)

## Mixed Integer Programming for $L_0$

**Goal:** Use mixed integer programming and real math-software to perform the same optimization tasks as being done in the Machine Learning (ML) community for reducing model size.

**Target:** a series of publications (conferences, journal) in the ML community.

#### **Steps:**

- Read on recently literature surrounding  $L_0$ , standard use case, assumptions about the problem at hand
- Read up on mixed integer programming, identify connection to current work
- Identify optimal approach to solving the standard  $L_0$  problem being faced by the current ML community
- Identify and apply existing math software to the  $L_0$  problem