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a. $[X, Y \mid Z]$ and $[a, b, c \mid [d, e, Y]]$

LHS: $[X, Y \mid Z]$

RHS: $[a, b, c \mid [d, e, Y]] = [a, b, c, d, e, Y]$

Therefore, this pair is identical as $X = a, Y = b, Z = [c, d, e, b] \Rightarrow$ match

b. $[q, [A \mid [r, s]], t]$ and $[q, [r, [r, s]] \mid B]$

LHS: $[q, [A \mid [r, s]], t] = [q, [A, r, s], t]$

RHS: $[q, [r, [r, s]] \mid B]$ already in simplest form

$q = q$

$[r, [r, s]] = [A, r, s] \Rightarrow$ right side has 2 elements and left side has 3 so

\Rightarrow no match

c. $[[Cow \mid [cat, dog]], bird, bug, chicken]$ and $[[ant, [cat, dog]] \mid Horse]$

LHS: $[[Cow \mid [cat, dog]], bird, bug, chicken] = [[Cow, cat, dog], bird, bug, chicken]$

RHS: $[[ant, [cat, dog]] \mid Horse]$ already in simplest form

Left side has the list of $[Cow, cat, dog]$ where as right side has the nested list of $[cat, dog]$

\Rightarrow no match

d. $[1, A, 2 \mid [A, 3, 4]]$ and $[B \mid [2, C \mid [D \mid E]]]$

LHS: $[1, A, 2 \mid [A, 3, 4]] = [1, A, 2, A, 3, 4]$

RHS: $[B \mid [2, C \mid [D \mid E]]] = [B \mid [2, C, D \mid E]] = [B, 2, C, D \mid E]$

Identical pair with $A=2, B=1, C=2, D=2, E=[3,4] \Rightarrow$ match

e. $[A \mid [A \mid [[A \mid [A]]]]]$ and $[b \mid C]$

LHS: $[A \mid [A \mid [[A \mid [A]]]]] = [A \mid [A \mid [A, [A]]]] = [A \mid [A, [A, [A]]]]$

$= [A, A, [A, [A]]]$

RHS: $[b \mid C]$ simplest form

$A = b$ then left side is $[b, b, [b, [b]]]$ and $C = [b, [b, [b]]] \Rightarrow$ match

f. $[X \mid [Y \mid [Z \mid [X]]]]$ and $[all, around, the, world, Y]$

LHS: $[X | [Y | [Z | [X]]]] = [X | [Y | [Z, X]]] = [X | [Y, Z, X]] = [X, Y, Z, X]$

RHS: [all, around, the, world, Y] already in simplest form

Left side has 4 elements in the list whereas right side has 5 elements => no match

g. $[1, 2 | [X | [Y, Z | X]]]$ and $[Q | [R, S, [], [Y]]]$

LHS: $[1, 2 | [X | [Y, Z | X]]] = [1, 2 | [X, Y, Z | X]] = [1, 2, X, Y, Z | X]$

RHS: $[Q | [R, S, [], [Y]]] = [Q, R, S, [], [Y]]$

$Q = 1, R = 2, X = S, Y = [], Z = [Y] = [[]]$ => last element of left side needs to be empty too so $X = S = []$ => match

h. $[Lions, [[and], tigers], [and], bears, oh | [[my]]]$ and $[[I, have], [[A], Bad], Feeling | [About | This]]$

LHS: $[Lions, [[and], tigers], [and], bears, oh | [[my]]] =$

$[Lions, [[and], tigers], [and], bears, oh, [my]]$

RHS: $[[I, have], [[A], Bad], Feeling | [About | This]] =$

$[[I, have], [[A], Bad], Feeling, About | This]$

$Lions = [I, have]$

$[[and], tigers] = [[A], Bad] \Rightarrow A = and, Bad = tigers$

$[and] = Feeling$

$bears = About$

$[oh, [my]] = This$

Identical pair => match