

Semantic Web

— to Artificial Intelligence

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Outline

OWL ontology from a formal perspective : Description Logics (DLs)

Components of an ontology

A basic DL : syntax

A basic DL : semantics

Ontology reasoning tasks

History of Description Logics

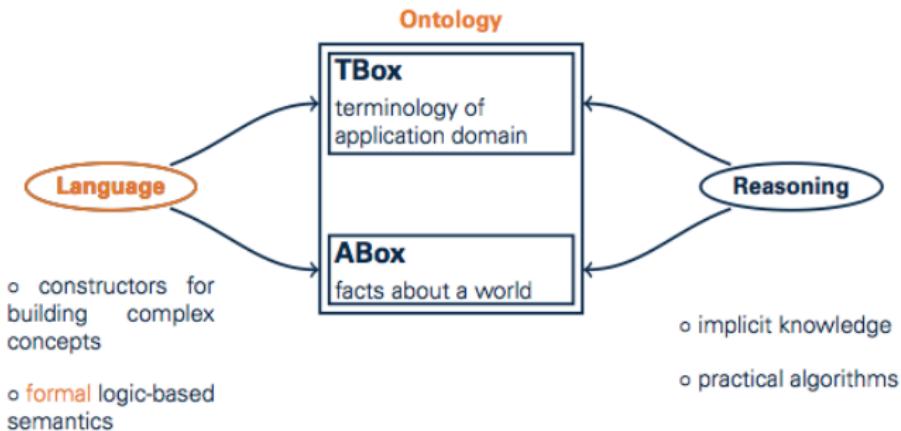
OWL ontology from a formal perspective :
Description Logics (DLs)

Expressing knowledge

- ▶ Heart disease is a kind of mediastinum disorder.
- ▶ Heart disease happens in heart structure.
- ▶ Smoking or alcoholism is bad for health.
- ▶ Parents are people who have at least one child.
- ▶ Each student can register at most two study programs each semester.
- ▶ Man and woman are disjoint.

How we can express these pieces of knowledge in a way computers can understand ?

Structure of an ontology



Correspondence between Ontology and NL

Semantic Web Ontology	\longleftrightarrow	Natural Language
names in N_C, N_R		single words
complex concepts		phrases
axioms		sentences (statements) expressing knowledge ¹

A step further towards ontologies...

1. like "There is a wash basin in either a kitchen or a bathroom", but not emotional sentences "What a nice day!"

DL ontology

Formalize the terminology (names) of the application domain :

- ▶ define important notions of the domain (classes, relations, objects)
- ▶ constrain the interpretations of these notions
- ▶ deduce consequences : subclass, instance relationships

Example :

- **classes (concepts)** : Person, Teacher, Course, Student, HeartDisease, HeartStructure, ...
- **relations (roles)** : gives, attends, likes, findingSite, ...
- **objects (individuals)** : CourseSemanticweb, John, Jim, ...
- **constraints/knowledge** :

every course is given by a teacher,

every student must attend at least one course

heart disease is a kind of mediastinum disorder

heart disease happens in heart structure

happy parents are those whose children are happy

John is a happy boy

John's father is Jim

A basic Description Logic \mathcal{ALC} : syntax

- ▶ concept names are also called **atomic concepts**
- ▶ all other concepts are called **complex**
- ▶ N_C : a set of concept names
- ▶ N_R a set of role name

Example.

Let $N_C = \{Female, Parent, Student\}$ and $N_R = \{hasChild\}$.

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Female $\sqcap \exists \text{hasChild}.\text{Student}$

How about “female whose children are students” :

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How about “female whose children are students” :

$\text{Female} \sqcap \forall \text{hasChild}.\text{Student}$

Syntax of \mathcal{ALC} : constructing complex concepts

Let N_C and N_R two disjoint sets of concept names and role names, respectively. \mathcal{ALC} concepts are defined by induction :

- ▶ if $A \in N_C$, then A is an \mathcal{ALC} concept
- ▶ if C, D are \mathcal{ALC} concepts and $r \in N_R$, then the following are \mathcal{ALC} concepts :
 - $C \sqcap D$ (conjunction)
 - $C \sqcup D$ (disjunction)
 - $\neg C$ (negation)
 - $\exists r.C$ (existential restriction)
 - $\forall r.C$ (value restriction)
- ▶ Abbreviations :
 - $\top = A \sqcup \neg A$ (top)
 - $\perp = A \sqcap \neg A$ (bottom)

Example. $\text{Female} \sqcap \exists \text{hasChild}.\text{Student}$

For you : try to write down your (atom, complex) \mathcal{ALC} concepts.

$\text{Female} \sqcap \forall \text{hasChild}.(\text{Student} \sqcap \exists \text{hasScore}.\text{GoodScore})$

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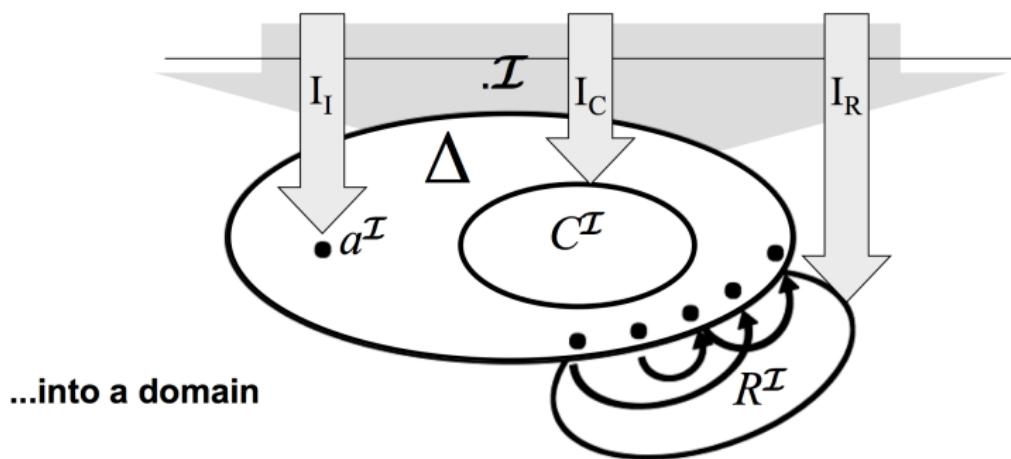
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Semantics of Description Logics

- model-theoretic semantics
- starts with interpretations
- an interpretation \mathcal{I} maps
individual names, class names and property names...



Semantics of \mathcal{ALC}

An interpretation $I = (\Delta^I, \cdot^I)$ consists of :

- ▶ a non-empty domain Δ^I , and
- ▶ an extension mapping \cdot^I (also called interpretation function) :
 - $A^I \subseteq \Delta^I$ for all $A \in N_C$ (concepts interpreted as sets)
 - $r^I \subseteq \Delta^I \times \Delta^I$ for all $r \in N_R$ (roles interpreted as binary relations)
 - $a^I \in \Delta^I$ (individuals interpreted as an element of Δ^I)

The extension mapping is extended to complex concepts :

$$(C \sqcap D)^I := C^I \cap D^I$$

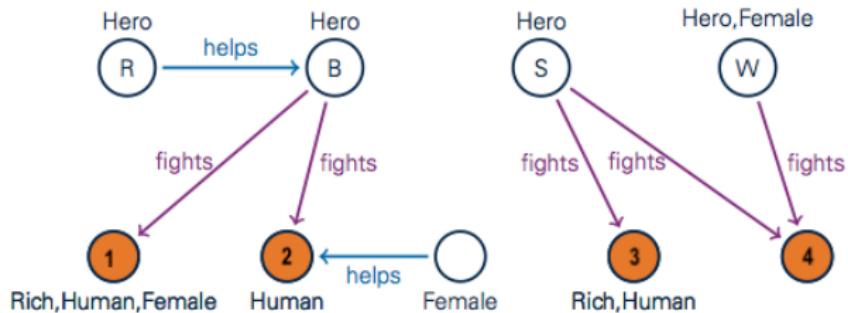
$$(C \sqcup D)^I := C^I \cup D^I$$

$$(\neg C)^I := \Delta^I \setminus C^I$$

$$(\exists r.C)^I := \{d \in \Delta^I \mid \text{there is } e \in \Delta^I \text{ with } (d, e) \in r^I \text{ and } e \in C^I\}$$

$$(\forall r.C)^I := \{d \in \Delta^I \mid \text{for all } e \in \Delta^I \text{ with } (d, e) \in r^I, \text{ it holds } e \in C^I\}$$

Interpretation Example



$$(Hero \sqcap \exists \text{fights}.\text{Human})^I = \{B, S\}$$

$$(Hero \sqcap \forall \text{fights}.(\text{Rich} \sqcup \neg \text{Human}))^I = \{R, S, W\}$$

$$(\forall \text{helps}.\text{Human})^I = \Delta^I \setminus \{R\}$$

Interpretation Example

Can you give an interpretation for the following concept ?

Female $\sqcap \exists hasChild. Student$

To define what is an ontology, we need the following definitions :

- ▶ TBox and ABox axioms
 - ▶ TBox : terminology box containing concept definitions and/or GCIs
 - ▶ ABox : assertion box, containing individual information.

Defining a Concept (aka. Concept Definitions)

Definitions.

- ▶ A concept definition is of the form $A = C$ where
 - ▶ A is a concept name.
 - ▶ C is a concept description.
- ▶ An interpretation I satisfies, also called a model of, the concept definition $A = C$ if $A' = C'$.

Examples.

$$\text{Heroine} = \text{Hero} \sqcap \text{Female}$$

$$\text{Student} = \text{People} \sqcap \exists \text{registes}.(\text{School} \sqcup \text{University})$$

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Does the following interpretation I satisfy this concept definition?

$$\Delta^I = \{a, b\}$$

$$\text{Heroine}^I = \{a\}$$

$$\text{Hero}^I = \{a, b\}$$

$$\text{Female}^I = \{b\}$$

If yes, why?

If no, modify I to make it satisfy the concept definition.

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For you : give a model of this concept definition

GCI s (General Concept Inclusions) and TBoxes

Definitions.

- ▶ A general concept inclusion (GCI) is of the form $C \sqsubseteq D$, where C, D are concepts.
- ▶ A TBox \mathcal{T} is a finite set of GCIs and/or concept definitions.
- ▶ An interpretation I satisfies the GCI $C \sqsubseteq D$ if $C^I \subseteq D^I$. I is a model of a TBox \mathcal{T} if it satisfies all GCIs in \mathcal{T} .
- ▶ Two TBoxes are equivalent if they have the same models.

Examples.

$\text{Hero} \sqcap \text{Villain} \sqsubseteq \perp$: two concepts are disjoint

$\text{Heroine} = \text{Hero} \sqcap \text{Female}$

$\text{Kitchen} \sqcup \text{Bathroom} \sqsubseteq \exists \text{hasWashbasin}.\top$

$\text{Cold} \sqcap \exists \text{causedBy}.\text{Virus} \sqsubseteq \text{Disease}$

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For you : give a model for these GCIs and definitions. **How many models does each of them have ?**

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Equivalent or not ?

- (1) $T_1 : \{A = A_1 \sqcap A_2\}$ and $T_2 : \{A = A_1, A = A_2\}$?
- (2) $T'_1 : \{A \sqsubseteq A_1 \sqcap A_2\}$ and $T'_2 : \{A \sqsubseteq A_1, A \sqsubseteq A_2\}$?

Assertions and ABoxes

Definitions.

- ▶ An assertion is of the form $C(a)$ (concept assertion) or $r(a, b)$ (role assertion) where C is a concept, r a role, and a, b are individual names from a set N_I (disjoint with N_C, N_R)
- ▶ An ABox \mathcal{A} is a finite set of assertions
- ▶ An interpretation I is a model of the ABox \mathcal{A} if it satisfies all its assertions :
 - $a' \in C'$ for all $C(a) \in \mathcal{A}$.
 - $(a', b') \in R'$ for all $R(a, b) \in \mathcal{A}$.

Examples.

$Kitchen(room1)$: the room1 is a kitchen

$locatedIn(whitechair1, room1)$: the whitechair1 is in the room1

$\neg Student(Jean)$: Jean is not a student

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Examples.

Kitchen(room1) : the room1 is a kitchen

locatedIn(whitechair1, room1) : the whitechair1 is in the room1

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For you : name some models for these ABox assertions. How many models does each of them have ?

Ontology

Definitions.

- ▶ An ontology $O = (\mathcal{T}, \mathcal{A})$ consists of a TBox \mathcal{T} and an ABox \mathcal{A} .
- ▶ The interpretation I is a model of the ontology $O = (\mathcal{T}, \mathcal{A})$ if it is a model of \mathcal{T} and a model of \mathcal{A} .

Examples.

Many ontologies from <http://swoogle.umbc.edu> and
<http://bioportal.bioontology.org>

TBox or ABox axioms ?

```
:Mary rdf:type :Woman .
```

```
:John :hasWife :Mary .
```

```
:John owl:differentFrom :Bill .
```

{John} ⊓ {Bill} ⊑ ⊥

```
:James owl:sameAs :Jim.
```

{John} ≡ {Jim}

```
:John :hasAge "51"^^xsd:nonNegativeInteger .
```

```
[] rdf:type owl:NegativePropertyAssertion ;  
owl:sourceIndividual :Bill ;  
owl:assertionProperty :hasWife ;  
owl:targetIndividual :Mary .
```

¬hasWife(Bill,Mary)

```
[] rdf:type owl:NegativePropertyAssertion ;  
owl:sourceIndividual :Jack ;  
owl:assertionProperty :hasAge ;  
owl:targetValue 53 .
```

TBox or ABox axioms ?

```
:Woman rdfs:subClassOf :Person .  
:Person owl:equivalentClass :Human .
```

```
[] rdf:type owl:AllDisjointClasses ;  
owl:members ( :Woman :Man ) .
```

Woman \sqcap Man $\sqsubseteq \perp$

```
:hasWife rdfs:subPropertyOf :hasSpouse .
```

```
:hasWife rdfs:domain :Man ;  
rdfs:range :Woman .
```

TBox or ABox axioms ?

```
:Mother owl:equivalentClass [  
    rdf:type owl:Class ;  
    owl:intersectionOf ( :Woman :Parent )  
] .
```

$$\text{Mother} \equiv \text{Woman} \sqcap \text{Parent}$$

```
:Parent owl:equivalentClass [  
    rdf:type owl:Class ;  
    owl:unionOf ( :Mother :Father )  
] .
```

$$\text{Parent} \equiv \text{Mother} \sqcup \text{Father}$$

```
:ChildlessPerson owl:equivalentClass [  
    rdf:type owl:Class ;  
    owl:intersectionOf ( :Person [ owl:complementOf :Parent ] )  
] .
```

$$\text{ChildlessPerson} \equiv \text{Person} \sqcap \neg \text{Parent}$$

```
:Grandfather rdfs:subClassOf [  
    rdf:type owl:Class ;  
    owl:intersectionOf ( :Man :Parent )  
] .
```

TBox or ABox axioms ?

```
:Jack rdf:type [  
    rdf:type owl:Class ;  
    owl:intersectionOf ( :Person  
        [ rdf:type owl:Class ;  
          owl:complementOf :Parent ]  
    )  
] .
```

Person ⊓ ¬Parent (Jack)

TBox or ABox axioms ?

```
:Parent owl:equivalentClass [  
    rdf:type          owl:Restriction ;  
    owl:onProperty   :hasChild ;  
    owl:someValuesFrom :Person  
] .
```

Parent $\equiv \exists \text{hasChild}.\text{Person}$

```
:Orphan owl:equivalentClass [  
    rdf:type          owl:Restriction ;  
    owl:onProperty   [ owl:inverseOf :hasChild ] ;  
    owl:allValuesFrom :Dead  
] .
```

Orphan $\equiv \forall \text{hasChild}^-.\text{Dead}$

TBox or ABox axioms ?

```
:JohnsChildren owl:equivalentClass [  
    rdf:type          owl:Restriction ;  
    owl:onProperty   :hasParent ;  
    owl:hasValue     :John  
] .
```

$$\text{JohnsChildren} \equiv \exists \text{hasParent}.\{\text{John}\}$$

```
:NarcisticPerson owl:equivalentClass [  
    rdf:type          owl:Restriction ;  
    owl:onProperty   :loves ;  
    owl:hasSelf      "true"^^xsd:boolean .  
] .
```

$$\text{NarcisticPerson} \equiv \exists \text{loves}.\text{Self}$$

TBox or ABox axioms ?

$\leq 4 \text{ hasChild.} \text{Parent (John)}$

```
:John rdf:type [  
    rdf:type owl:Restriction ;  
    owl:maxQualifiedCardinality "4"^^xsd:nonNegativeInteger ;  
    owl:onProperty :hasChild ;  
    owl:onClass :Parent  
] .
```

$\geq 2 \text{ hasChild.} \text{Parent (John)}$

```
:John rdf:type [  
    rdf:type owl:Restriction ;  
    owl:qualifiedCardinality "3"^^xsd:nonNegativeInteger ;  
    owl:onProperty :hasChild ;  
    owl:onClass :Parent  
] .
```

$= 3 \text{ hasChild.} \text{Parent (John)}$

TBox or ABox axioms ?

```
:John rdf:type [  
    rdf:type owl:Restriction ;  
    owl:cardinality "5^^xsd:nonNegativeInteger ;  
    owl:onProperty :hasChild  
] .
```

=5 hasChild.T (John)

```
:MyBirthdayGuests owl:equivalentClass [  
    rdf:type owl:Class ;  
    owl:oneOf ( :Bill :John :Mary )  
] .
```

MyBirthdayGuests ≡ {Bill, John, Mary}

TBox or ABox axioms ?

```
:hasParent owl:inverseOf :hasChild .  
  
:Orphan owl:equivalentClass [  
    rdf:type owl:Restriction ;  
    owl:onProperty [ owl:complementOf :hasChild ] ;  
    owl:allValuesFrom :Dead  
] .  
  
:hasSpouse rdf:type owl:SymmetricProperty .  
:hasChild rdf:type owl:AsymmetricProperty .  
:hasParent owl:propertyDisjointWith :hasSpouse .  
:hasRelative rdf:type owl:ReflexiveProperty .  
:parentOf rdf:type owl:IrreflexiveProperty .  
:hasHusband rdf:type owl:FunctionalProperty .  
:hasHusband rdf:type owl:InverseFunctionalProperty .  
:hasAncestor rdf:type owl:TransitiveProperty .
```

$$\text{Orphan} \equiv \forall \text{ hasChild } . \text{Dead}$$

TBox or ABox axioms ?

```
:hasGrandparent owl:propertyChainAxiom ( :hasParent :hasParent ).
```

hasParent \circ hasParent \sqsubseteq hasGrandParent

```
:Person owl:hasKey ( :hasSSN ) .
```

In OWL 2 a collection of (data or object) properties can be assigned as a key to a class expression. This means that each named instance of the class expression is uniquely identified by the set of values which these properties attain in relation to the instance.

TBox or ABox axioms ?

```
:personAge owl:equivalentClass
[ rdf:type rdfs:Datatype;
  owl:onDatatype xsd:integer;
  owl:withRestrictions (
    [ xsd:minInclusive "0"^^xsd:integer ]
    [ xsd:maxInclusive "150"^^xsd:integer ]
  )
].

```

Datatype facets

```
:majorAge owl:equivalentClass
[ rdf:type rdfs:Datatype;
  owl:intersectionOf (
    :personAge
    [ rdf:type rdfs:Datatype;
      owl:datatypeComplementOf :minorAge ]
  )
].
```

Let us now define the interesting reasoning services that we can benefit from ontologies

Inconsistency and incoherency

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Incoherency Example

Lab2 : reasoning with the ontology Pizza via protégé

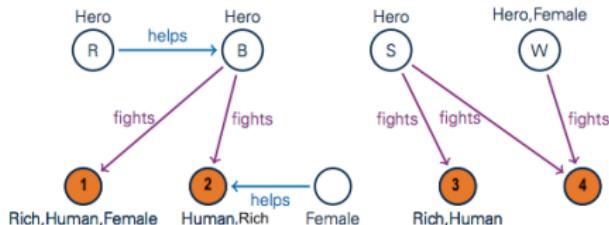
That ontology is consistent but incoherent !

Next : more reasoning tasks...

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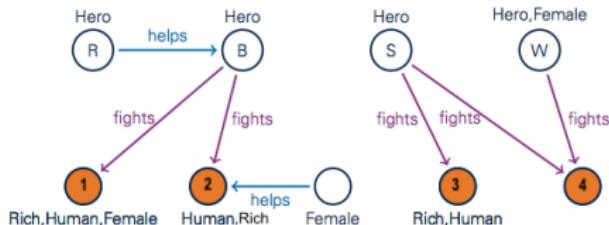


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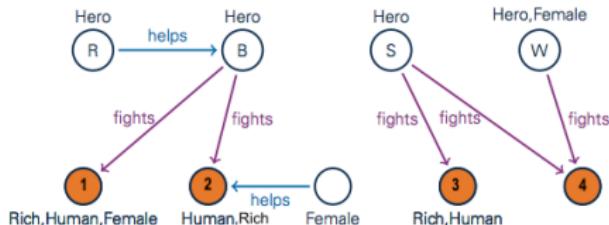


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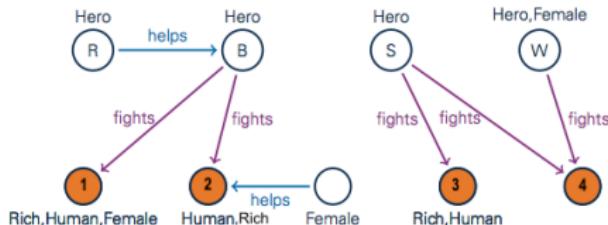


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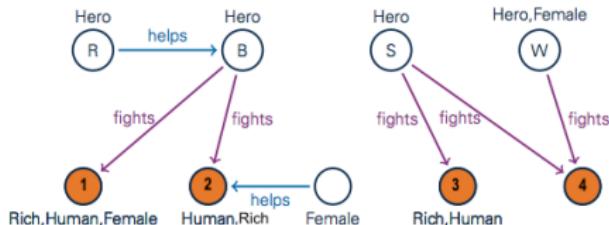


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Terminological Reasoning of an Ontology

How about

$$\exists r. A \sqcap \exists r. B \sqsubseteq \exists r. (A \sqcap B) ???$$

and

$$\forall r. A \sqcap \forall r. B \sqsubseteq \forall r. (A \sqcap B) ???$$

Assertional Reasoning of an Ontology

Let $O = (\mathcal{T}, \mathcal{A})$ be an ontology with TBox \mathcal{T} and ABox \mathcal{A} .

Assertional reasoning refers to deciding the following problems :

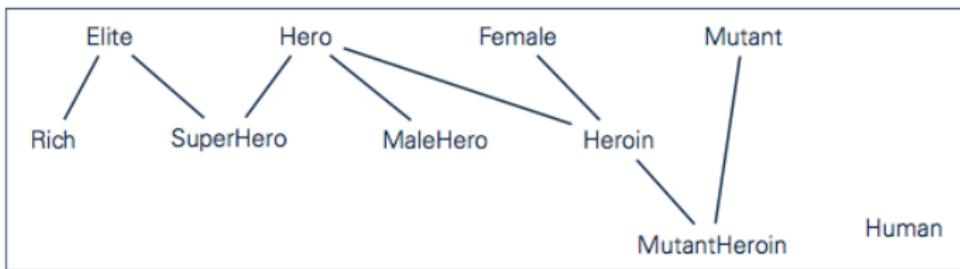
- ▶ a is an instance of a concept C w.r.t O if $a^I \in C^I$ for all models I of O
- ▶ $r(a, b)$ holds w.r.t O if $(a^I, b^I) \in r^I$ for all models I of O .

Let $O = \{A \sqsubseteq B, A(a)\}$. Then we have $O \models B(a)$.

TBox Classification

Computing the **subsumption relations** between all **concept names** in \mathcal{T} :

$$\begin{aligned} \text{Heroine} &\equiv \text{Hero} \sqcap \text{Female} \\ \text{MaleHero} &\equiv \text{Hero} \sqcap \neg\text{Female} \\ \text{MutantHeroine} &\equiv \text{Heroine} \sqcap \text{Mutant} \\ \text{Elite} &\equiv \text{Rich} \sqcup \neg\text{Human} \\ \text{Superhero} &\equiv \text{Hero} \sqcap \text{Elite} \end{aligned}$$



Description Logics for Concept Modeling

DLs have been used to formalize different variants of conceptual modeling formalisms, and to provide automated reasoning in such formalisms (see also [Borgida & Brachman 2003]).

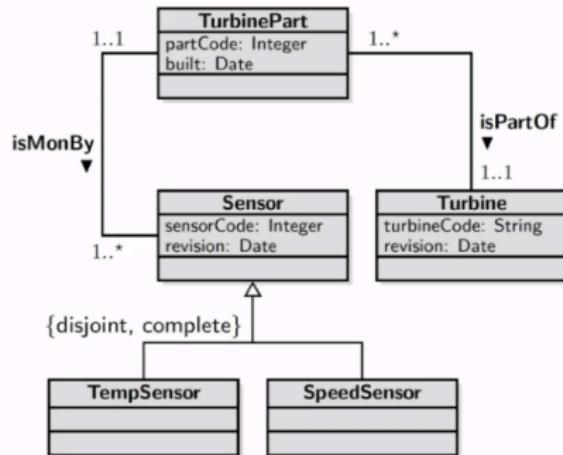
- ER schemas with cardinality constraints (but no hierarchies) [Lenzerini & Nobile 1990]
- Acyclic ER schemas with hierarchies [Bergamaschi & Sartori 1992]
- Arbitrary (possibly cyclic) ER schemas with hierarchies [C., Lenzerini, et al. 1994, 1999]
- UML Class Diagrams [Berardi et al. 2005], with OCL constraints [Queralt et al. 2012]
- ORM [Fillottrani, Keet, et al. 2015; Franconi, Mosca, et al. 2012; Sportelli & Franconi 2016]

In this way, DL reasoning can be used to provide support for various conceptual modeling activities.

While most of the work has been theoretical, also some prototype systems that provide reasoning support for conceptual modeling have been developed:

- ICOM conceptual modeling tool [Fillottrani, Franconi, et al. 2012, 2006; Franconi & Ng 2000]

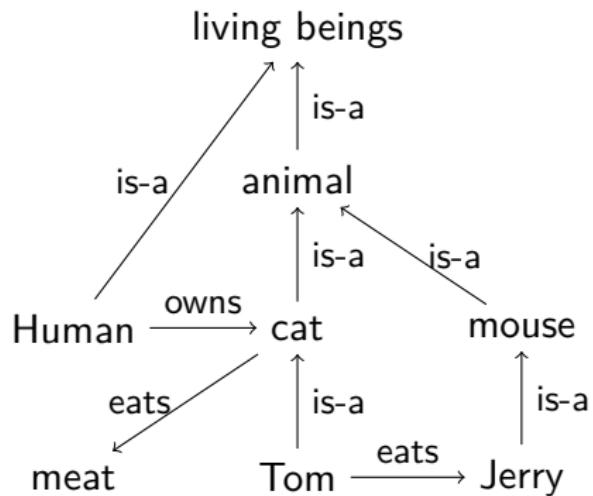
Description Logics vs UML



Relationships and constraints:

- $\text{TempSensor} \sqsubseteq \text{Sensor}$
- $\text{SpeedSensor} \sqsubseteq \text{Sensor}$
- $\text{TempSensor} \sqsubseteq \neg \text{SpeedSensor}$
- $\text{Sensor} \sqsubseteq \text{TempSensor} \sqcup \text{SpeedSensor}$
- $\text{Turbine} \sqsubseteq \forall \text{turbineCode}. \text{String} \sqcap \exists \text{turbineCode} \sqcap \leq 1 \text{ turbineCode}$
- $\exists \text{isMonBy} \sqsubseteq \text{TurbinePart}$
- $\exists \text{isMonBy}^- \sqsubseteq \text{Sensor}$
- $\text{TurbinePart} \sqsubseteq \exists \text{isMonBy}$
- $\text{Sensor} \sqsubseteq \exists \text{isMonBy}^-$
- $\exists \text{isPartOf} \sqsubseteq \text{TurbinePart}$
- $\exists \text{isPartOf}^- \sqsubseteq \text{Turbine}$
- (funct isMonBy^-)
- (funct isPartOf)
- ...

Example : Semantic Network



Conclusions

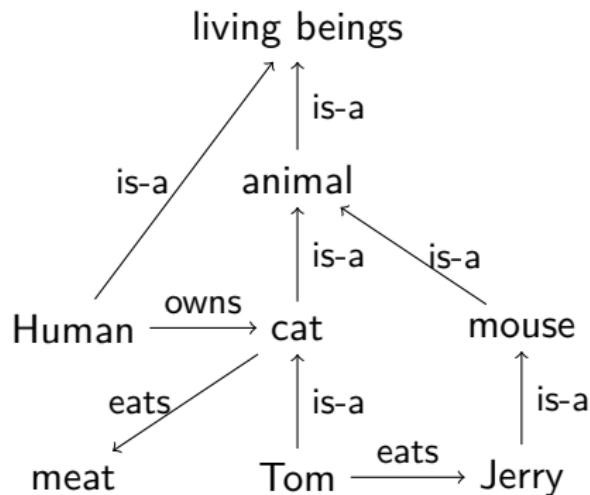
- ▶ Tom is an animal
- ▶ Tom eats a mouse
- ▶ similarities

Living beings
Eats and owns the animals
Humans and mice are
living beings

Difficulties

Tom is a cat
Tom is a mouse
Tom is a living being
Tom is a human
Tom is meat
Tom eats meat
Tom eats a mouse
Tom eats a cat
Tom eats a living being
Tom eats a human
Tom eats meat
Tom eats a meat
Tom eats a Tom
Tom eats a Jerry

Example : Semantic Network



Conclusions

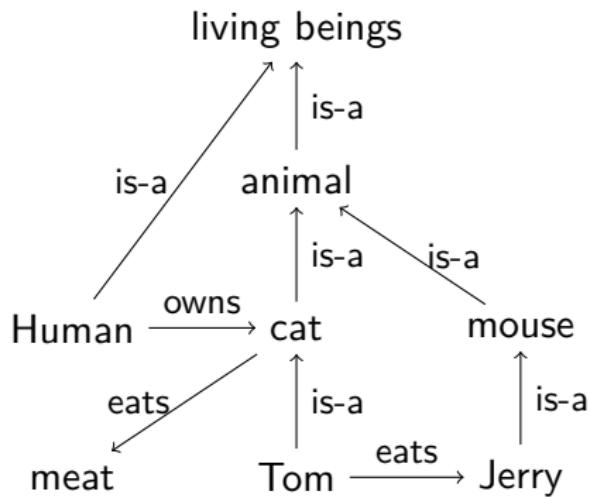
- ▶ Tom is an animal
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▶ Cats and mice are animals
▶ Humans and mice are living beings

Difficulties

▶ How can we distinguish between the two types of "is-a" relationships?
▶ How can we distinguish between the two types of "eats" relationships?
▶ How can we distinguish between the two types of "living beings"?

Example : Semantic Network

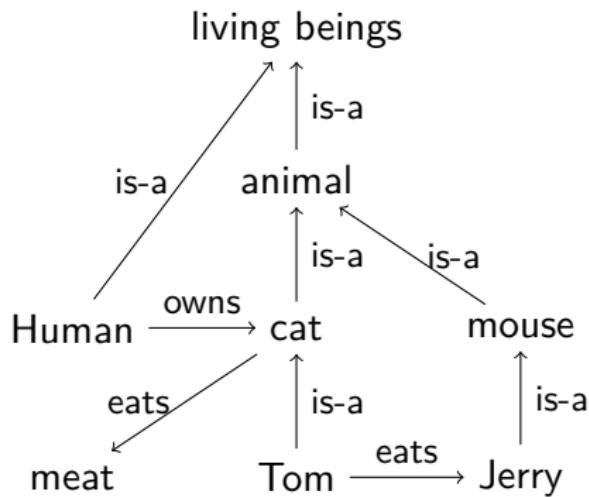


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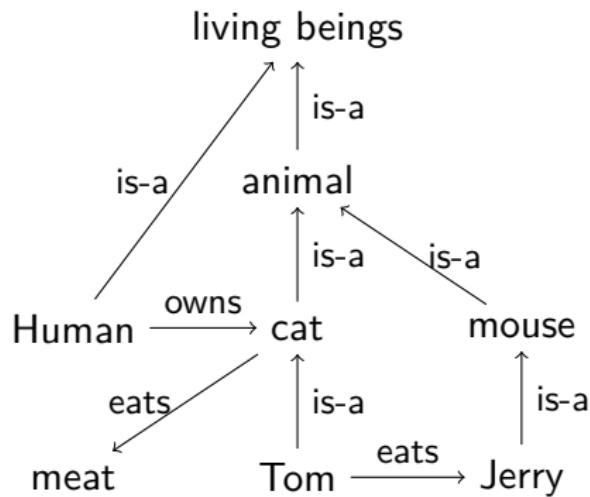


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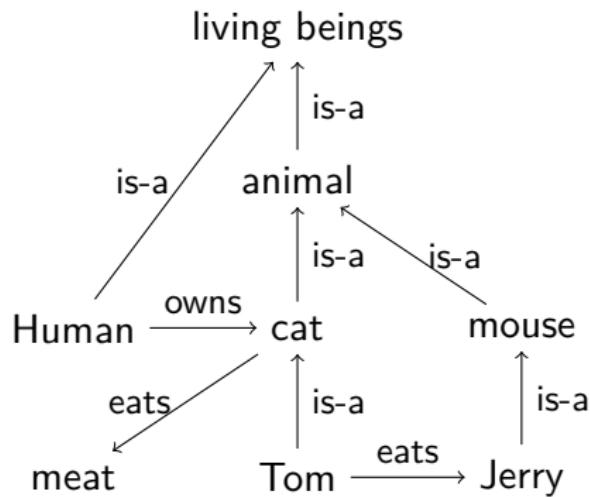
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- ▶ Does everyone own a cat?
- ▶ Can a mouse talk to a human?
- ▶ Is Jerry meat?
- ▶ Do all eat meat, including mice or meaty meat?
- ▶ What does "eat" mean?

Example : Semantic Network



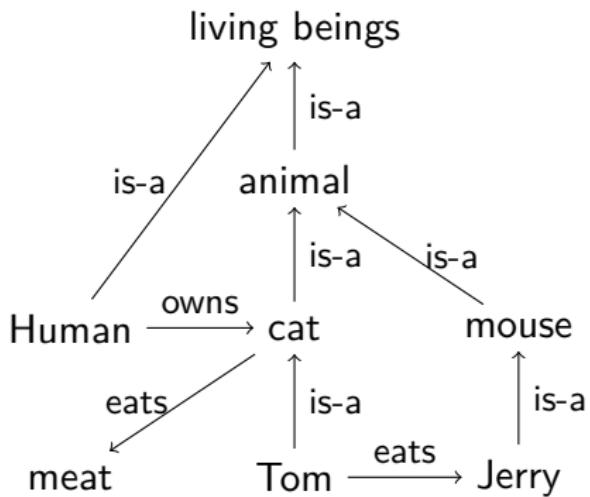
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Example : Semantic Network



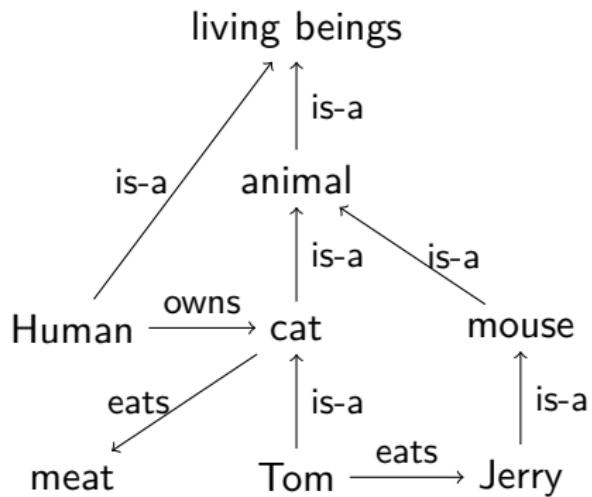
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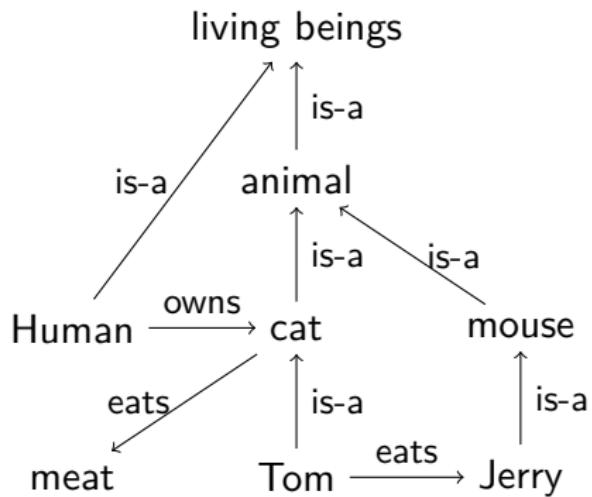
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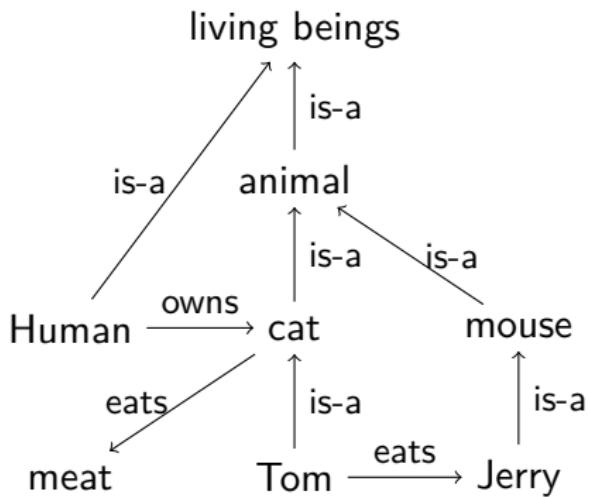
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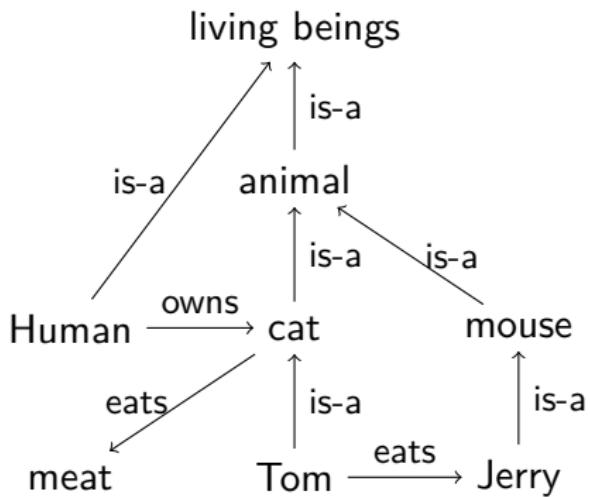
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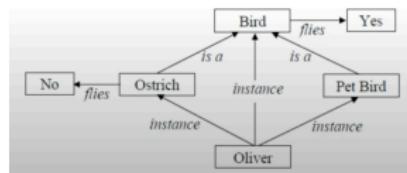
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Problems of Semantic Networks

- ▶ ambiguity of is-a
 - ▶ individual → class : element
 - ▶ class → class : subset
 - ▶ "What is-a is and isn't" (Ron Brachman, 1983)

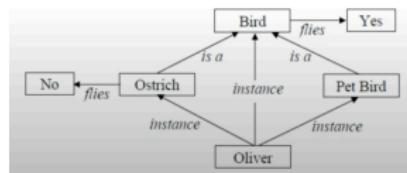
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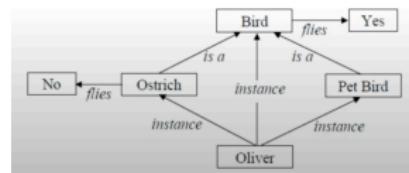
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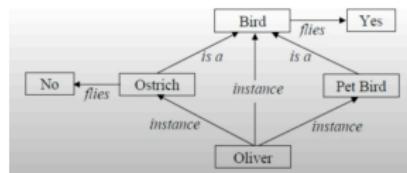
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Frames : Origin and Intention

- ▶ KR formalism for describing entities
- ▶ developed in 1975 by Marvin Minsky
- ▶ Goal : Imitation of human categorization



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Minsky
(1927-2016)

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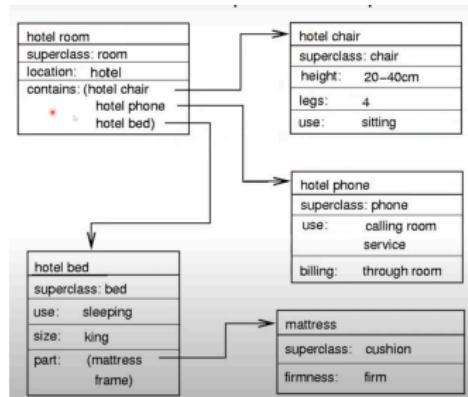
Frames : syntax and conclusions

► Syntax :

- ▶ Class Frame describes class of entities
- ▶ Instance Frame describes specific entities
- ▶ Frame contains slots for certain attributes
- ▶ value of a slot is called filler
- ▶ Defaults for filler are possible
- ▶ Sub-frames for specialization (\leadsto is-a)

► Reasoning procedure

- ▶ Inheritance : Sub-frames inherit default fillers
- ▶ Criteria : If an instance frame I has suitable fillers for all slots of a class frame C , I is an instance C
- ▶ Matching : Test whether an instance of a frame C_1 is also an instance of another frame C_2



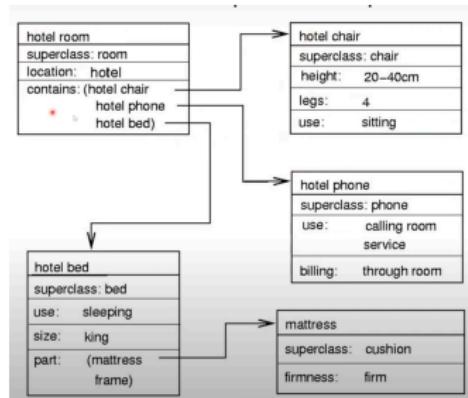
Frames : syntax and conclusions

▶ Syntax :

- ▶ Class Frame describes class of entities
- ▶ Instance Frame describes specific entities
- ▶ Frame contains slots for certain attributes
- ▶ value of a slot is called filler
- ▶ Defaults for filler are possible
- ▶ Sub-frames for specialization (\leadsto is-a)

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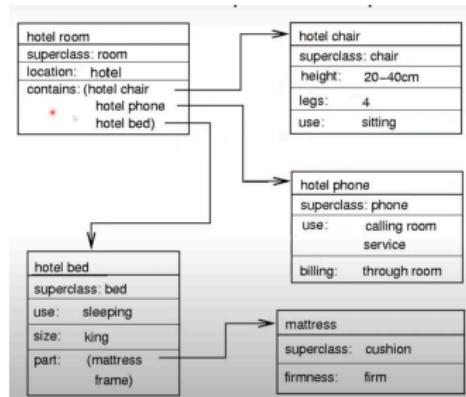
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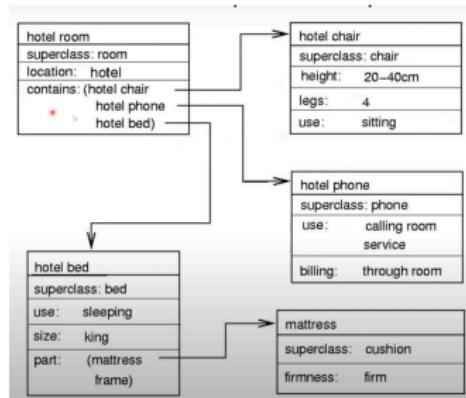
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Problems of frames

- ▶ Frame inferences can be expressed in predicate logic (Pat Hayes, 1979)
- ▶ Same as semantic networks
 - ▶ No taxonomy if all properties are just defaults
 - ▶ Without formal semantics, there is no "right" and "wrong"
- ▶ AI as a collection of heuristics
 - ▶ Incomplete knowledge base
 - ▶ Incomplete inference rules

See also a lecture on Semantic Networks and Frames :

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Lack of formal semantics unclear meaning of the network
unreliable reasoning procedures
incompatibility

Graph-based algorithms Result depends on irrelevant information

Consequence : logic-based KR systems

• more precise meaning of knowledge

• more reliable reasoning

• more compatible with other systems

• more robust against irrelevant information

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Consequence : logic-based KR systems

- formal semantics based on mathematical logic
- Semantic Technologies
- often decidable fragments of predicate logic
- often simpler, intuitive syntax, e.g. no variables

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Prehistory of Description Logics

a class of logic-based knowledge representation formalisms for representing terminological knowledge

early approaches for representing terminological knowledge

- ▶ semantic networks (Quillian, 1968)
- ▶ frames (Minsky, 1975)

problems with missing semantics led to

- ▶ structured inheritance networks
- ▶ the first DL system KL-ONE

History of Description Logics

- ▶ Phase 1
 - implementation of systems based on incomplete structural subsumption algorithms
- ▶ Phase 2
 - tableau-based algorithms and complexity results
 - first tableau-based systems (Kris, Crack)
 - first formal study of optimization methods
- ▶ Phase 3
 - tableau-based algorithms for very expressive DLs
 - highly-optimized tableau-based systems (FaCT, Racer)
 - relationship to modal logic and FOL

History of Description Logics

- ▶ Phase 4
 - Web Ontology Language (OWL) based on DL
 - industrial-strength reasoners and ontology editors
 - light-weight (tractable) DLs
- ▶ Phase 5
 - non-standard reasoning
 - ontology management
 - semantic extensions

We will study some of these algorithms...

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Summary

- ▶ Introduction to DLs
- ▶ Decidability, complexity, reasoning algorithms (following lectures)