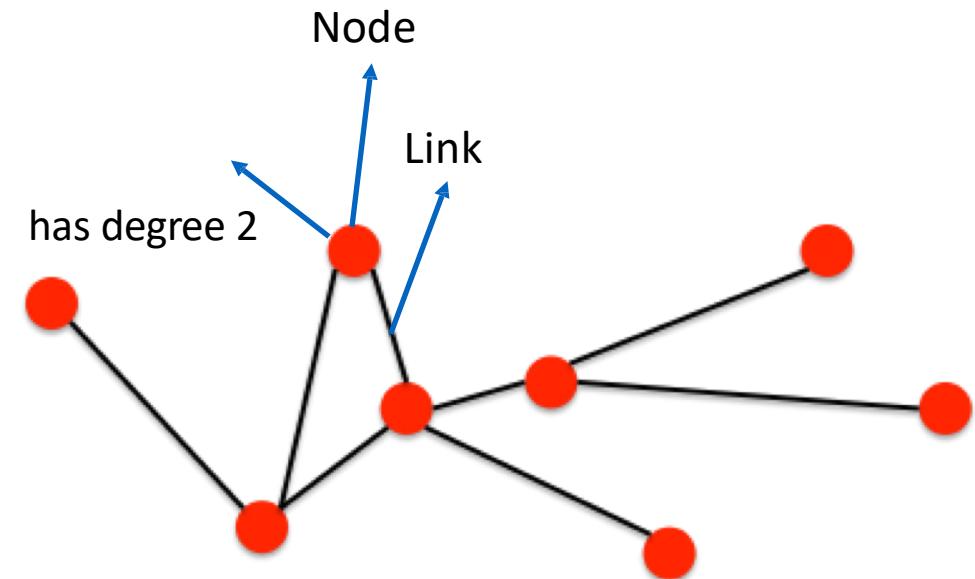
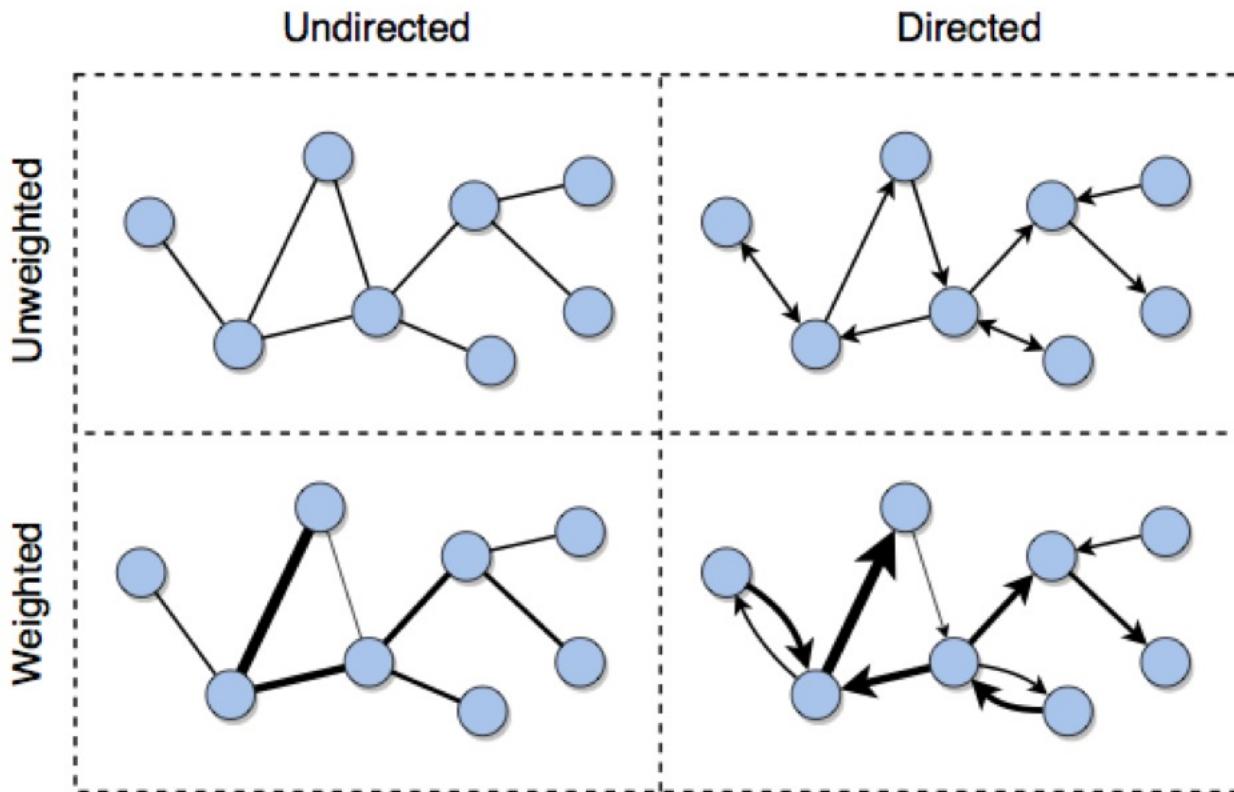


Lecture2: Network Elements

Definition

- A **network** (graph) is a structure used to model pairwise relations between objects. A network is made up of entities (aka **nodes**, vertices) and the relationships between them (aka **links**, edges)
- Number of edges of incident to the vertex is **the node degree**





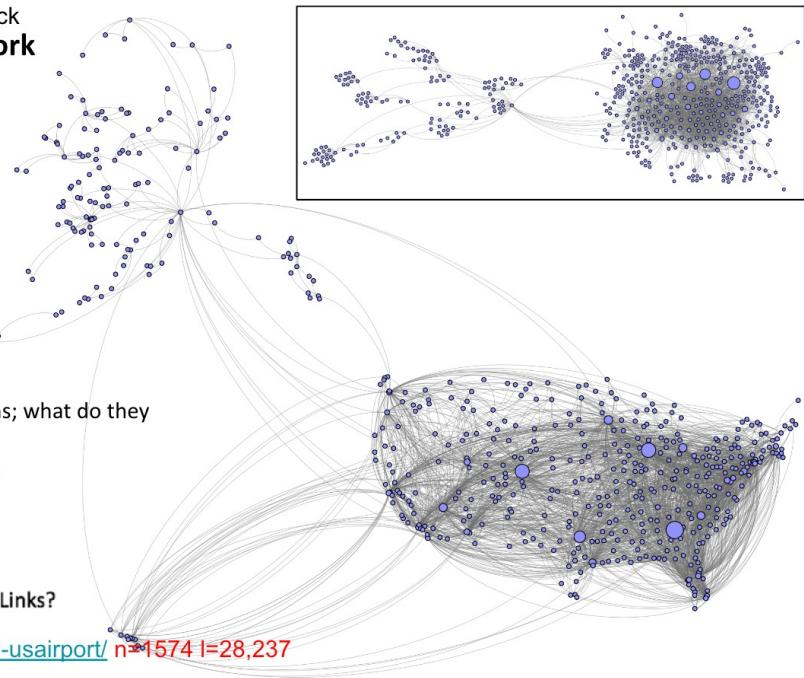
Can you think of a few examples in each of these categories?

Group 6: Alan, Jovon, Daniel, Nick
US air transportation network

- What do nodes represent?
Airports
- What do links represent?
Flights from Point A to B
- Do links have direction?
Yes, based on the nature of flights
- Do links have weights?
How frequently the route is flown
- Larger nodes have more connections; what do they represent?
More flights to/from other airports
- What do the layouts represent?
The locations of airports

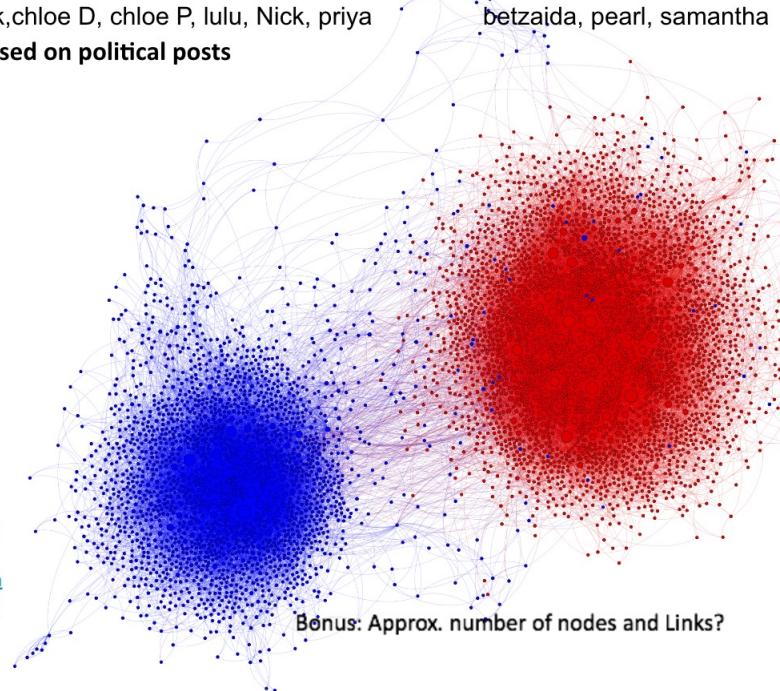
Bonus: Approx. number of nodes and Links?

<http://konect.cc/networks/opsahl-usairport/> n=1574 l=28,237

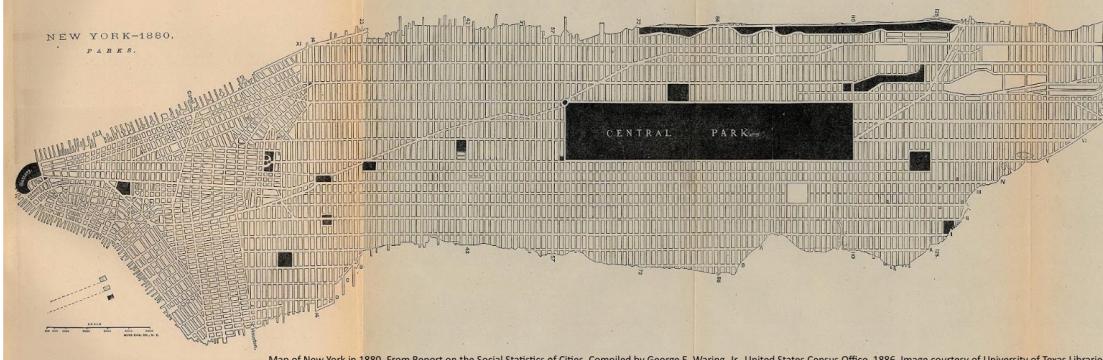


Group 2 - Ice Cream Group - Isaak, chloe D, chloe P, lulu, Nick, priya
Retweet network on Twitter, based on political posts during 2010 US election

- What do nodes represent?
twitter users
- What do links represent?
A retweet
- Do links have direction?
Yes (i (origin) is retweeted by j(destination))
 - Do links have weights?
No
- Larger nodes have more connections; what does that mean?
users that received more retweets
- What do the clusters and colors represent?
Colors represent two political parties
- Bonus:
<https://cnets.indiana.edu/groups/nan/truthy/visualizing-the-political-discourse-on-twitter/>
1000 users, 250,000 tweets , no information about retweets



Street Networks Group 10 Lulu, Yonghe, Nick, Clara, Geeta, Yara, Madison, Jocelyn



Map of New York in 1880. From Report on the Social Statistics of Cities, Compiled by George E. Waring, Jr., United States Census Office, 1886. Image courtesy of University of Texas Libraries

- What do nodes represent?
Street intersections.
- What do links represent?
Streets
- Do links have direction? What does it represent?
Direction of traffic
- Do links have weights? What do they represent?
Yes, how wide the streets are (number of lanes)

Bonus: Approx. number of nodes and Links? <https://arxiv.org/abs/1308.1533>

n=1047 l=4617

Remember: always consult Networkx

<https://networkx.github.io/>

NetworkX

[Stable \(notes\)](#)

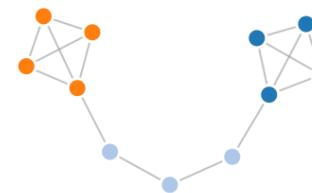
2.4 – October 2019
[download](#) | [doc](#) | [pdf](#)

[Latest \(notes\)](#)

2.5 development
[github](#) | [doc](#) | [pdf](#)

Software for complex networks

NetworkX is a Python package for the creation,
manipulation, and study of the structure, dy-
namics, and functions of complex networks.



Network Elements Learning Objectives

1. Degree
2. Solution MyFirstNetwork_Exercise-Soln.ipynb
3. Clustering Coefficient
4. Shortest path lengths

For each of the 3 metrics you can calculate:

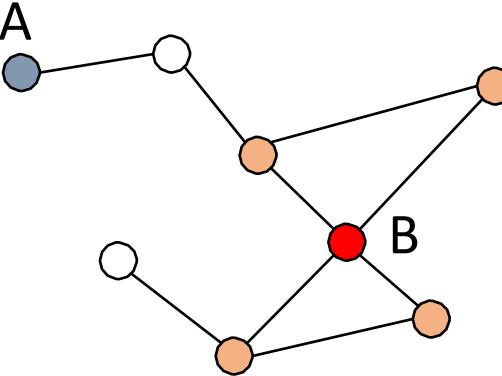
Average in the network, and histogram of the properties

Notebook Scripts for the Class

1. MyFirstNetwork_Exercise-Soln.ipynb
2. Example_ShortestPath_and_CC.ipynb
3. Reading_SocialNetwork.ipynb with data: SchoolEdges.csv

NODE DEGREES

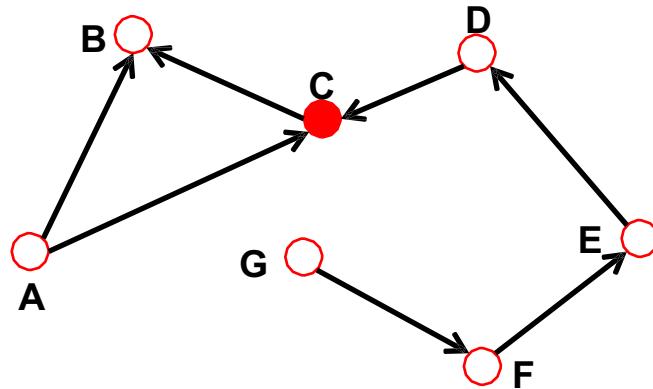
Undirected



Node degree: the number of links connected to the node.

$$k_A = 1 \quad k_B = 4$$

Directed

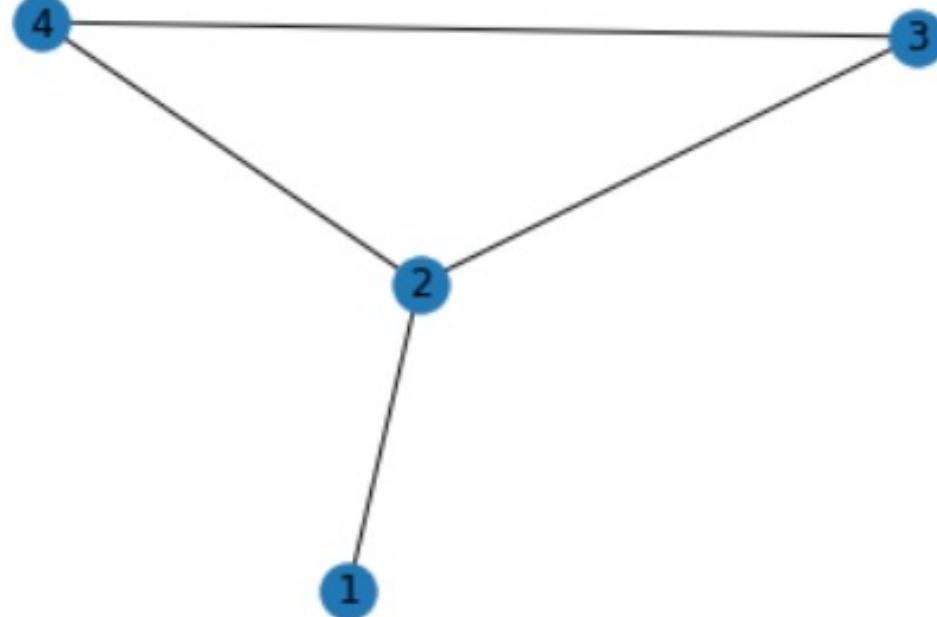


In *directed networks* we can define an **in-degree** and **out-degree**. The (total) degree is the sum of in- and out-degree.

$$k_C^{in} = 2 \quad k_C^{out} = 1 \quad k_C = 3$$

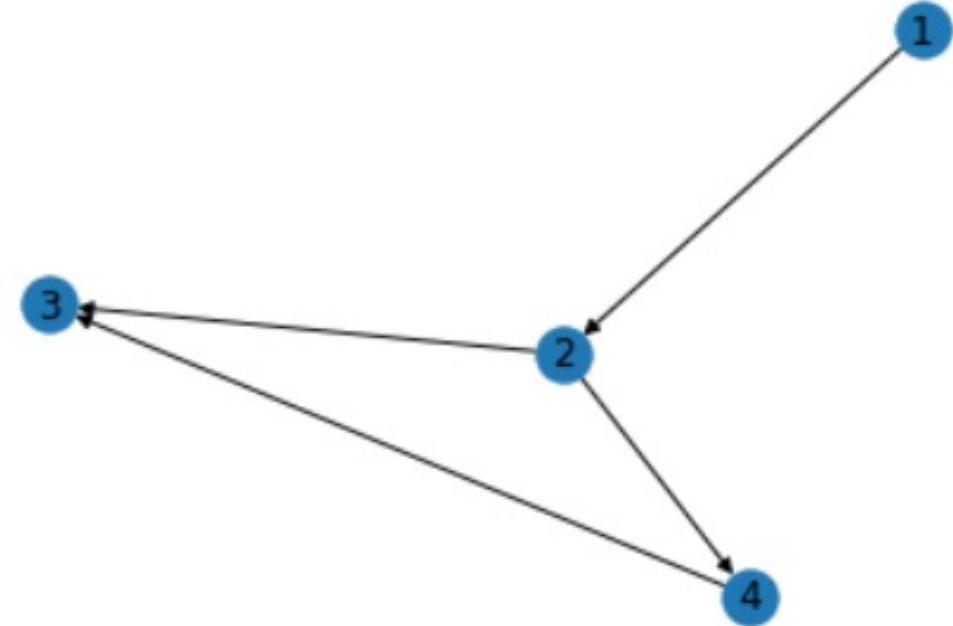
MyFirstNetwork_Exercise-Soln.ipynb

- 1) Nodes
- 2) Edges
- 3) Number of Nodes
- 4) Number of Edges
- 5) Number of Neighbors per node
- 6) Degree of each node
- 7) Average degree calculation
with number of links and nodes



MyFirstNetwork_Exercise-Soln.ipynb

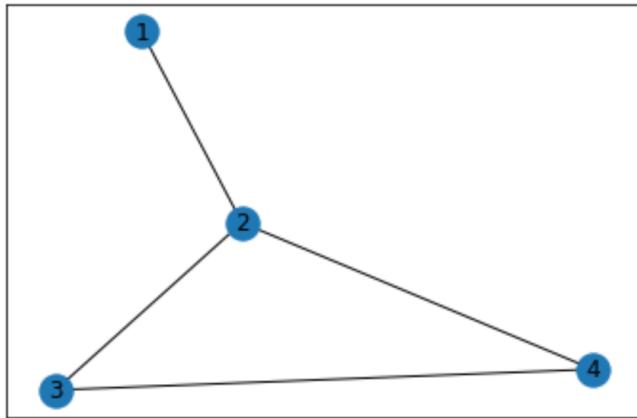
- 1) Nodes
- 2) Edges
- 3) Number of Nodes
- 4) Number of Edges
- 5) Number of Neighbors per node
- 6) Degree of each node
 - In-degree of each node
 - out-degree of each node
- 7) Average indegree outdegree and degree calculation with short equation
- 8) Histogram



Exercise: Create the 4 node network of Lecture 1 and respond the following questions (use networkx documentation or Google the questions)

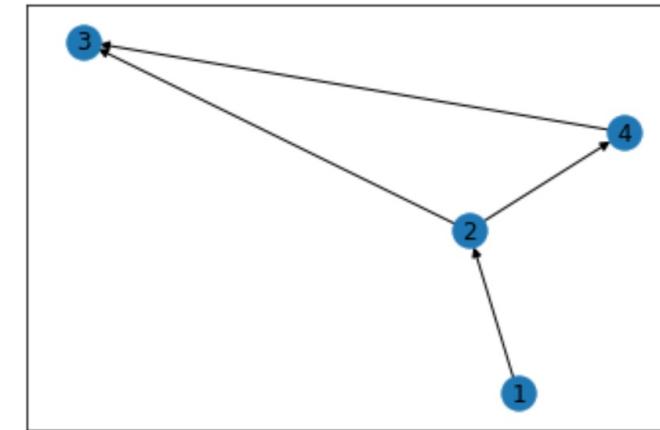
```
g = nx.Graph() #Graph base class for undirected graphs. See also:DiGraph  
g.add_edge('1','2',weight=1.0) #Nodes can be arbitrary (hashable) Python  
g.add_edge('2','3',weight=1.0) #Edges are represented as links between n  
g.add_edge('2','4',weight=1.0) #We create a network by adding 11 edges t  
g.add_edge('4','3',weight=1.0)
```

```
nx.draw_networkx(g) #The draw_networkx function is called (check online
```



```
gd = nx.DiGraph() #Graph base class for undirected graphs. See also:DiG  
gd.add_edge('1','2',weight=1.0) #Nodes can be arbitrary (hashable) Pytho  
gd.add_edge('2','3',weight=1.0) #Edges are represented as links between  
gd.add_edge('2','4',weight=1.0) #We create a network by adding 11 edges  
gd.add_edge('4','3',weight=1.0)
```

```
nx.draw_networkx(gd)
```



Note the Difference between Graph and DiGraph, they create Undirected and Dierected Graphfs respectively
Here the Weight of each link is the same

Question 1, Print Nodes

```
: 1 print("Nodes: ",list(gd.nodes))  
Nodes: ['1', '2', '3', '4']
```

Question 2, Print Edges

```
: 1 print("Edges: ",list(gd.edges))  
Edges: [('1', '2'), ('2', '3'), ('2', '4'), ('4', '3')]
```

Question 3, Number of Nodes

```
: 1 print("Number of Nodes: ",gd.number_of_nodes())  
Number of Nodes: 4
```

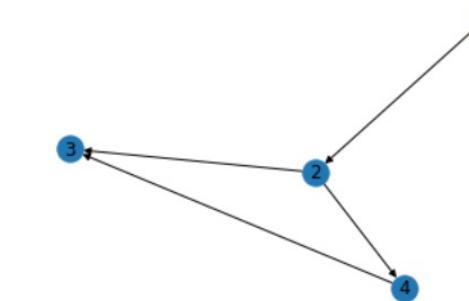
Question 4, Number of Edges

```
: 1 print("Number of Edges: ",gd.number_of_edges())  
Number of Edges: 4
```

Question 5, Neighbors of each Node

```
: 1 for node in g.nodes():  
    print ("Neighbors of ", node, " are : ", list(gd.neighbors(node)))  
  
Neighbors of 1 are : ['2']  
Neighbors of 2 are : ['3', '4']  
Neighbors of 3 are : []  
Neighbors of 4 are : ['3']
```

```
: 1 for node in g.nodes():  
    print ("Predecessors of ", node, " are : ", list(gd.predecessors(node)))  
  
Predecessors of 1 are : []  
Predecessors of 2 are : ['1']  
Predecessors of 3 are : ['2', '4']  
Predecessors of 4 are : ['2']
```



```
: 1 for node in g.nodes():  
    print ("Sucessors of ", node, " are : ", list(gd.successors(node)))  
  
Sucessors of 1 are : ['2']  
Sucessors of 2 are : ['3', '4']  
Sucessors of 3 are : []  
Sucessors of 4 are : ['3']
```

Note that in a directed graph neighbors are only the Out degree node but
 $\text{degree}(\text{node}) = \text{in_dgree}(\text{node}) + \text{out_degree}(\text{node})$

Example extracting the degree, in_degree and out_degree of node 4 in Graph dg

```
1 gd.degree('4')
```

```
2
```

```
1 gd.out_degree('4')
```

```
1
```

```
1 gd.in_degree('4')
```

```
1
```

```
for node in gd.nodes():
    print ("Degree of ", node, " is : ", gd.degree(node))
```

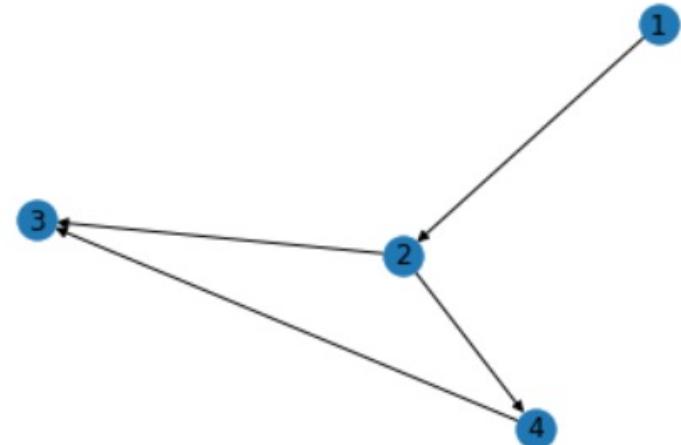
```
Degree of 1 is : 1
Degree of 2 is : 3
Degree of 3 is : 2
Degree of 4 is : 2
```

```
for node in gd.nodes():
    print ("In-Degree of ", node, " is : ", gd.in_degree(node))
```

```
In-Degree of 1 is : 0
In-Degree of 2 is : 1
In-Degree of 3 is : 2
In-Degree of 4 is : 1
```

```
for node in gd.nodes():
    print ("Out-degree of ", node, " is : ", gd.out_degree(node))
```

```
Out-degree of 1 is : 1
Out-degree of 2 is : 2
Out-degree of 3 is : 0
Out-degree of 4 is : 1
```

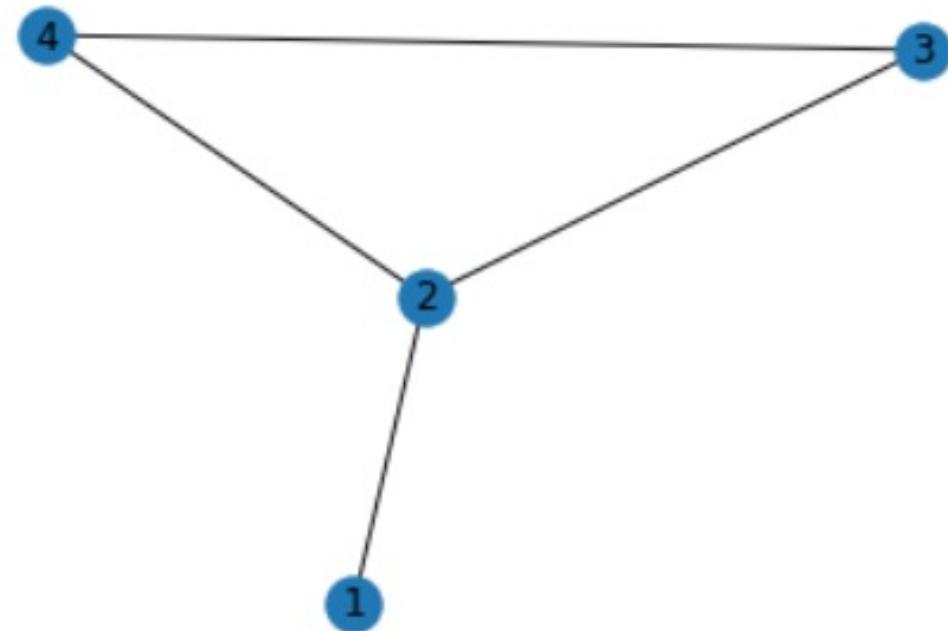


Note $\text{degree}(\text{node}) = \text{in_degree}(\text{node}) + \text{out_degree}(\text{node})$

6) Iterate through nodes and print degree

```
for node in g.nodes():
    print ("Degree of ", node, " is : ", len(list(g.neighbors(node))), "or ", g.degree(node))
```

```
Degree of 1 is : 1 or 1
Degree of 2 is : 3 or 3
Degree of 3 is : 2 or 2
Degree of 4 is : 2 or 2
```



Formula of the Average Degree

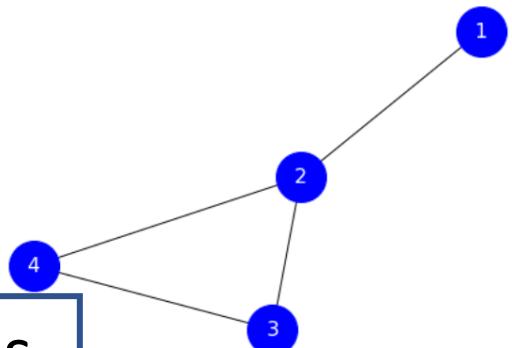
Average Degree for an Undirected Graph

- It is the sum of the degree of each node divided by the number of nodes

$$\langle \text{degree} \rangle = (1+3+2+2)/4 = 2$$

- It can be also written as the $2 \times (\text{Number of Links})/\#\text{Nodes}$

$$\langle \text{degree} \rangle = 2 \times (4)/4 = 2$$



```
undirected graph = ", np.mean(list(dict(g.degree()).values())), ", or: ", 2.0*g.number_of_edges()/g.number_of_nodes()
```

Average degree of undirected graph = 2.0 , or: 2.0

```
np.mean(list(dict(g.degree()).values()))
```

2.0

Average Degree for a Directed Graph

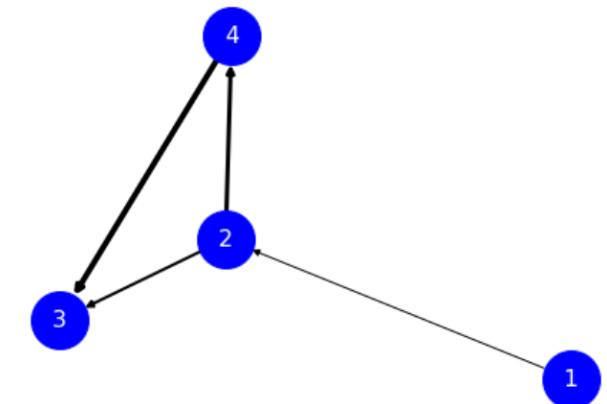
- It is the sum of the degree of each node divided by the number of nodes

$$\langle \text{in-degree} \rangle = (0+1+2+1)/4 = 1$$

$$\langle \text{out-degree} \rangle = (1+2+0+1)/4 = 1$$

- It can be also written as (Number of Links)/#Nodes

$$\langle \text{in-degree} \rangle = (4)/4 = 1 \quad \langle \text{out-degree} \rangle = (4)/4 = 1$$



- Finally, the average degree is

$$2 \times (\text{Number of Links})/\#\text{Nodes} \quad \text{or}$$

$$\langle \text{degree} \rangle = \langle \text{out-degree} \rangle + \langle \text{in-degree} \rangle = 2$$

(Number of Links)/#Nodes

```
print ("Average out-degree of directed graph = ",np.mean(list(dict(gd.out_degree()).values())))," or: ",gd.number_of_
```

Average out degree of directed graph = 1.0 , or: 1.0

(Number of Links)/#Nodes

```
print ("Average in-degree of directed graph = ",np.mean(list(dict(gd.in_degree()).values())))," or: ",gd.number_of_ec
```

Average in-degree of directed graph = 1.0 , or: 1.0

```
print ("Average degree of directed graph = ",np.mean(list(dict(gd.degree()).values())))," or: ",np.mean(list(dict(gd.
```

Average degree of directed graph = 2.0 , or: 2.0

$\langle \text{degree} \rangle = \langle \text{out-degree} \rangle + \langle \text{in-degree} \rangle = 2$

```
np.mean(list(dict(gd.in_degree()).values()))+np.mean(list(dict(gd.out_degree()).values()))
```

2.0

```
np.mean(list(dict(gd.degree()).values()))
```

2.0

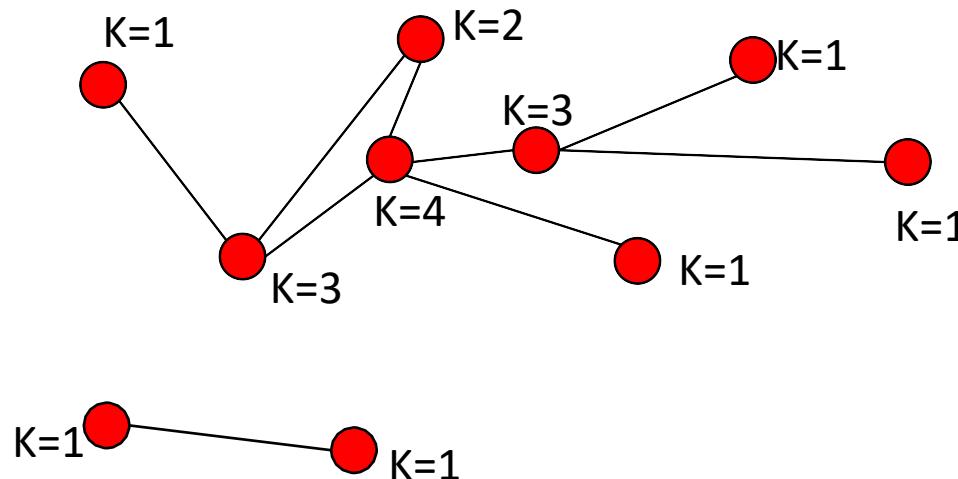
Building a Histogram of the properties of the nodes

DEGREE DISTRIBUTION

Degree distribution $P(k)$: probability that a randomly chosen vertex has degree k

$N_k = \# \text{ nodes with degree } k$

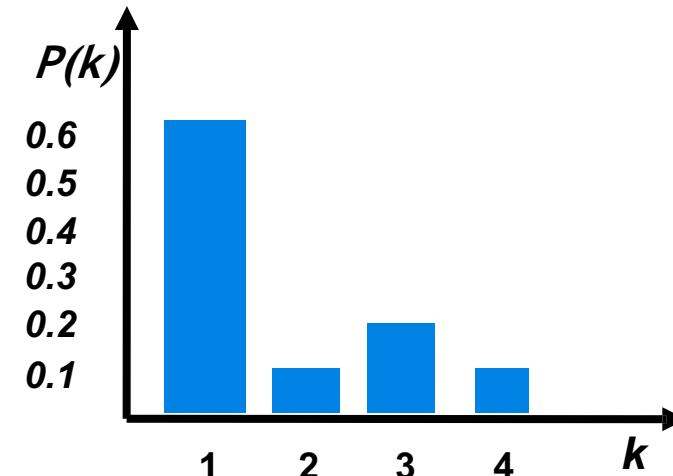
$P(k) = N_k / N \rightarrow \text{plot}$



The degree distribution is the normalized Histogram, it gives the probability to find a node with degree k

K=1 $N_1=6$
K=2 $N_2=1$
K=3 $N_3=2$
K=4 $N_4=1$

$$N = 10$$



```

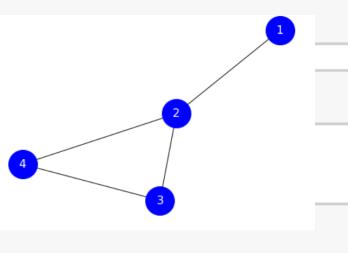
1 degree_list=list(dict(g.degree()).values())
1 degree_list
[1, 3, 2, 2]
1 Bins = range(1,max(degree_list)+2) ##Note the range max +2
1
1 for n in Bins:
    print(n)
1
2
3
4

1 counts,k = np.histogram(degree_list, bins=Bins)
1 counts #counts the occurrence of degree_list in Bins
array([1, 2, 1])

1 k #Note that k the vector is larger than count that is why we use k[:-1] in the bar plot
array([1, 2, 3, 4])

```

Range=[min,max+2]



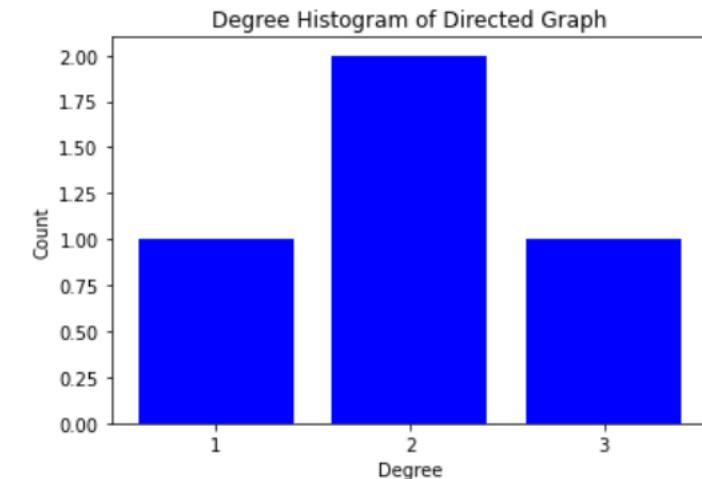
We need to plot

```

1 fig, ax = plt.subplots()
2 plt.bar(k[:-1],counts,width=0.80, color='b')
3 plt.title("Degree Histogram of Directed Graph")
4 plt.ylabel("Count")
5 plt.xlabel("Degree")
6 ax.set_xticks([d for d in k[:-1]])
7 ax.set_xticklabels(k[:-1])

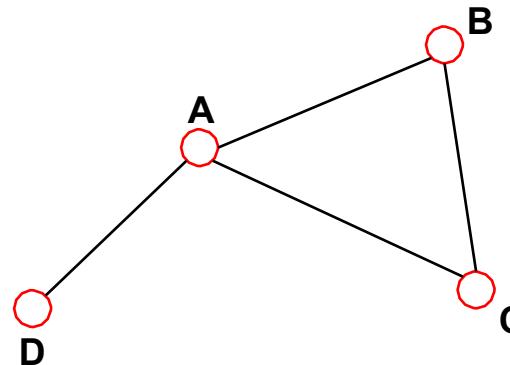
```

```
: [Text(1, 0, '1'), Text(2, 0, '2'), Text(3, 0, '3')]
```



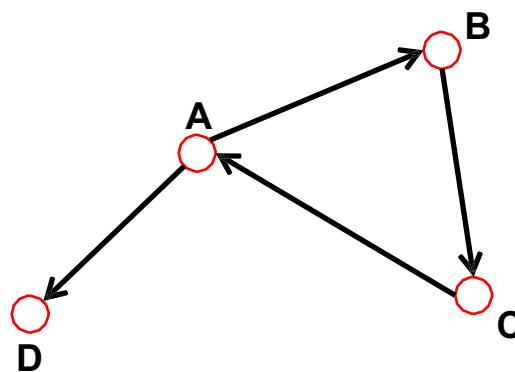
Shortest Path length

SHORTEST PATH LENGTH



The *distance (shortest path, geodesic path)* between two nodes is defined as the number of edges along the **shortest path** connecting them.

*If the two nodes are disconnected, the distance is infinity.



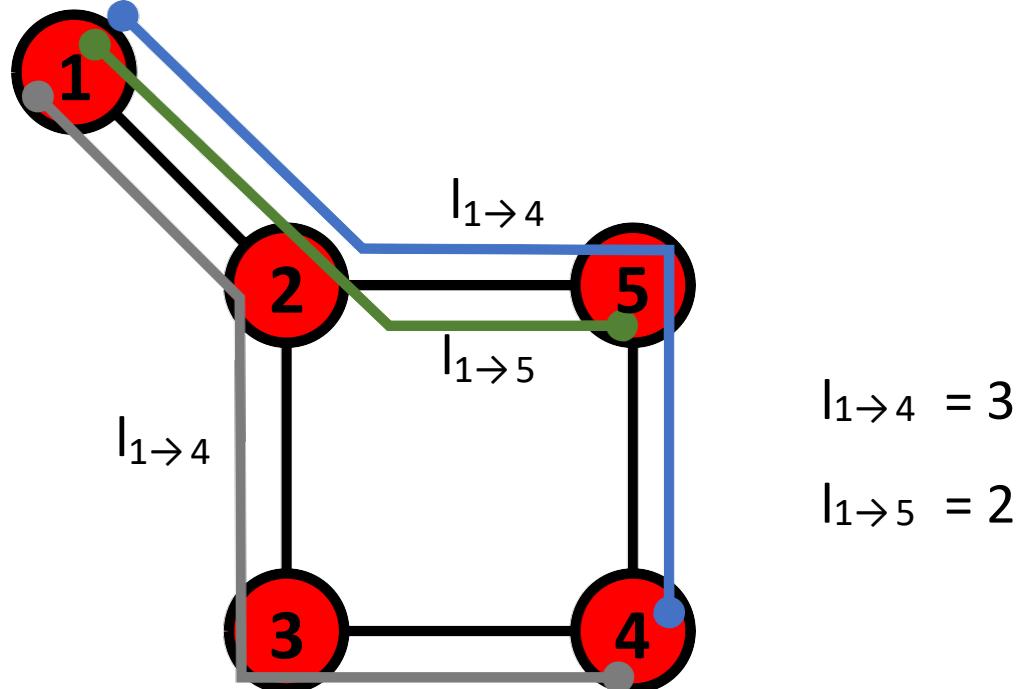
In **directed graphs** each path needs to follow the direction of the arrows.

Thus in a digraph the distance from node A to B (on an AB path) is generally different from the distance from node B to A (on a BCA path).

SHORTEST PATH LENGTH

Shortest Path

The path with the shortest length between two nodes (distance).



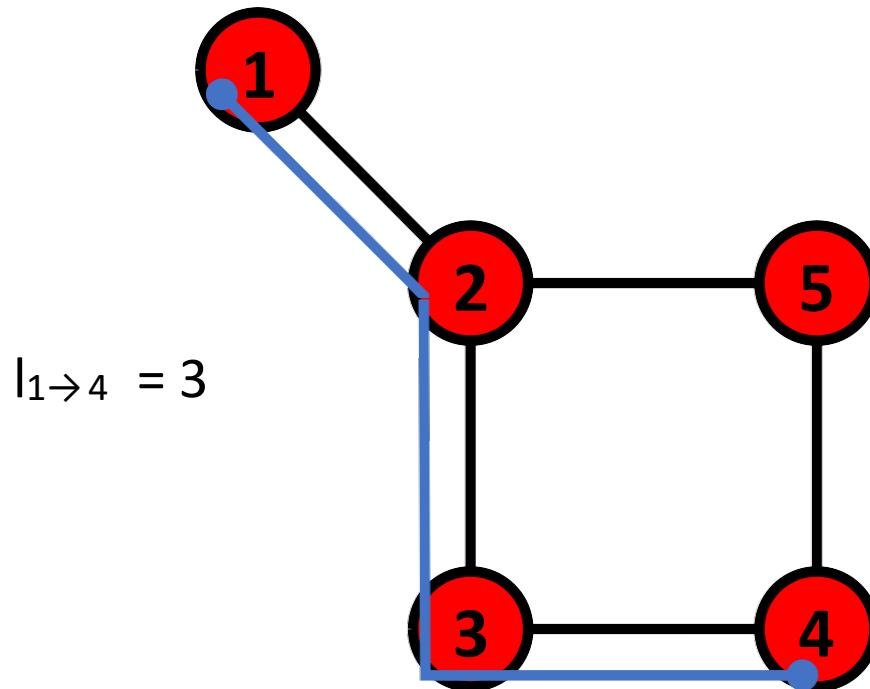
Average Shortest Path Length

$$\begin{aligned} &(|_{1 \rightarrow 2} + |_{1 \rightarrow 3} + |_{1 \rightarrow 4} + \\ &+ |_{1 \rightarrow 5} + |_{2 \rightarrow 3} + |_{2 \rightarrow 4} + \\ &+ |_{2 \rightarrow 5} + |_{3 \rightarrow 4} + |_{3 \rightarrow 5} + \\ &+ |_{4 \rightarrow 5}) / 10 = 1.7 \end{aligned}$$

The average of the shortest paths for all pairs of nodes.

Important Note: Numbers of pairs for a network of size N is $N(N-1)$

$$\begin{aligned} &2*(1+2+3 \\ &+ 2+1+2 \\ &+ 1+1+2 \\ &+ 1) / 20 = 1.6 \end{aligned}$$



$$N(N-1)=20$$

`shortest_path(G, source=None, target=None, weight=None)` [source]

Compute shortest paths in the graph.

Parameters:

- **G** (*NetworkX graph*)
- **source** (*node, optional*) – Starting node for path. If not specified, compute shortest paths for each possible starting node.
- **target** (*node, optional*) – Ending node for path. If not specified, compute shortest paths to all possible nodes.
- **weight** (*None or string, optional (default = None)*) – If None, every edge has weight/distance/cost 1. If a string, use this edge attribute as the edge weight. Any edge attribute not present defaults to 1.

Returns:

path – All returned paths include both the source and target in the path.

shortest_path_length(*G*, source=None, target=None, weight=None) [\[source\]](#)

Compute shortest path lengths in the graph.

- Parameters:**
- **G** (*NetworkX graph*)
 - **source** (*node, optional*) – Starting node for path. If not specified, compute shortest path lengths using all nodes as source nodes.
 - **target** (*node, optional*) – Ending node for path. If not specified, compute shortest path lengths using all nodes as target nodes.
 - **weight** (*None or string, optional (default = None)*) – If None, every edge has weight/distance/cost 1. If a string, use this edge attribute as the edge weight. Any edge attribute not present defaults to 1.

- Returns:** **length** – If the source and target are both specified, return the length of the shortest path from the source to the target.

`average_shortest_path_length(G, weight=None)` [source]

Return the average shortest path length.

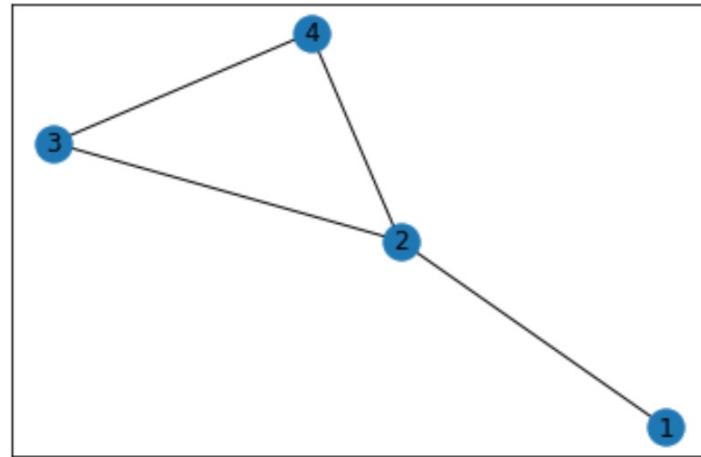
The average shortest path length is

$$a = \sum_{s,t \in V} \frac{d(s, t)}{n(n - 1)}$$

where `v` is the set of nodes in `G`, `d(s, t)` is the shortest path from `s` to `t`, and `n` is the number of nodes in `G`.

Example 1, Average Shortest Path

```
1 has 3 paths
['1', '2'] length 1
['1', '2', '3'] length 2
['1', '2', '4'] length 2
2 has 3 paths
['2', '1'] length 1
['2', '3'] length 1
['2', '4'] length 1
3 has 3 paths
['3', '2'] length 1
['3', '4'] length 1
['3', '2', '1'] length 2
4 has 3 paths
['4', '2'] length 1
['4', '3'] length 1
['4', '2', '1'] length 2
```



$$\langle L \rangle = 16/12$$

Number of Paths in Undirected Graph:
nodes(nodes-1)

See: [Example_ShortestPath_and_CC.ipynb](#)



In the social sciences, the word "**clique**" is used to describe a group (averaging 5 or 6) "persons who interact with each other more regularly and intensely than others in the same setting."

Definition of Clustering Coefficient

clustering(G, nodes=None, weight=None) [source]

Compute the clustering coefficient for nodes.

For unweighted graphs, the clustering of a node u is the fraction of possible triangles through that node that exist,

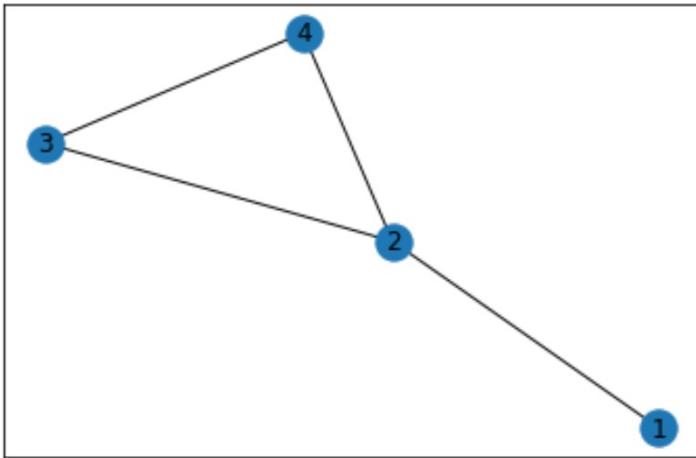
$$c_u = \frac{2T(u)}{\deg(u)(\deg(u) - 1)},$$

where $T(u)$ is the number of triangles through node u and $\deg(u)$ is the degree of u .

Note there are extensions of the definitions for Weighted and Directed Graphs

Next class we study the calculations of Paths and clustering coefficient in ipynb and cover Routing in Networks

Example 1 Average Clustering Coefficient



```
nx.clustering(g)
```

```
{'1': 0, '2': 0.3333333333333333, '3': 1.0, '4': 1.0}
```

```
nx.average_clustering(g)
```

```
0.5833333333333333
```

```
(0+0.333333+1+1)/4
```

```
0.58333325
```

$$T(1) = 0$$

$$2*0/(1)(0) = 0$$

$$T(2)=1$$

$$2*1/(3)(2)=0.333$$

$$T(3)=1$$

$$2*1/(2)(1)=1$$

$$T(4)=1$$

$$2*1/(2)(1)=1$$

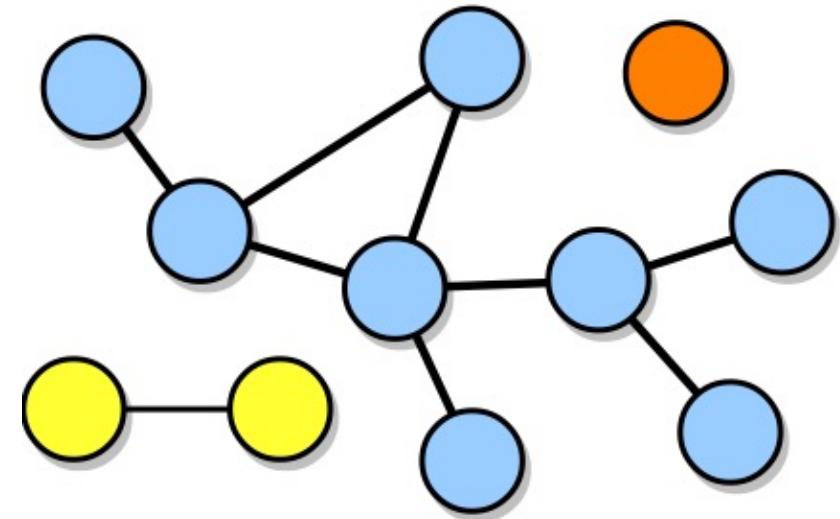
$$\frac{2T(u)}{\deg(u)(\deg(u) - 1)}$$

$$\langle C \rangle = 0.5833$$

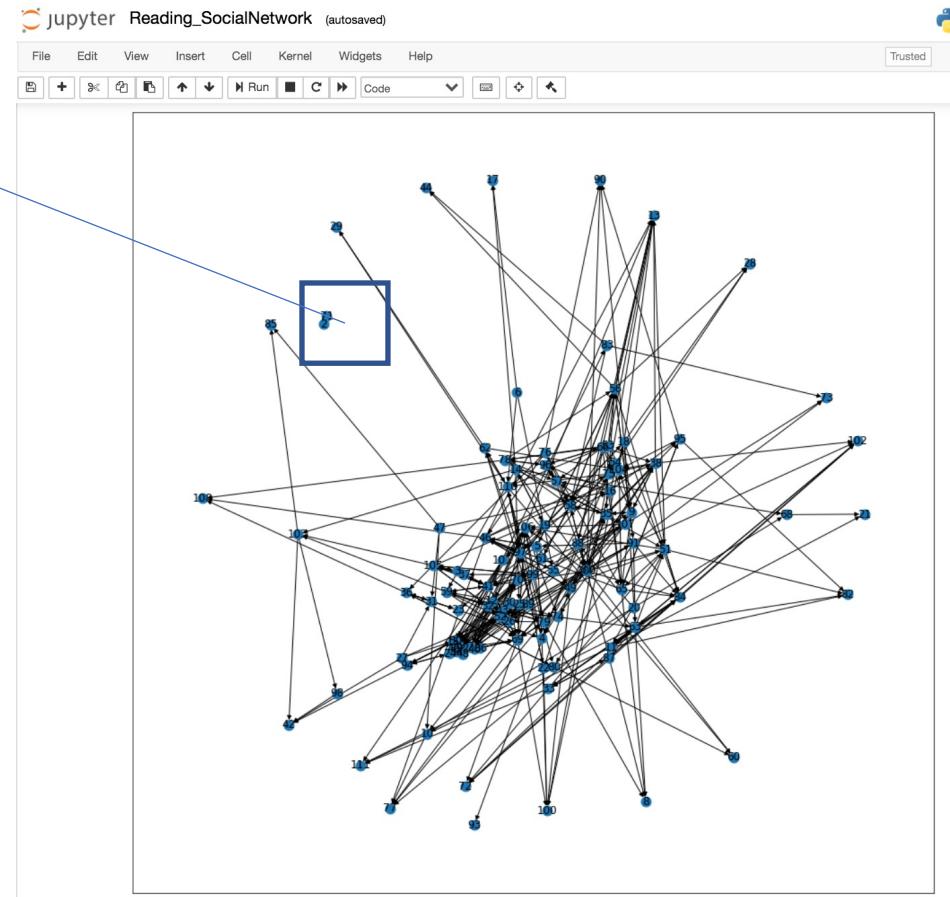
See: Example_ShortestPath_and_CC.ipynb

Connectedness and components

- A network is **connected** if there is a path between any two nodes
- If a network is not connected, it is **disconnected** and has multiple connected components
- A **connected component** is a connected subnetwork
 - The largest one is called **giant component**; it often includes a substantial portion of the network
 - A singleton is the smallest-possible connected component



Disconnected
Component
Of size 2



See: [Reading_SocialNetwork.ipynb](#)

Extract Largest Component

```
In [111]: 1 Gcc = sorted(nx.weakly_connected_components(g), key=len, reverse=True) # identify largest connected component of
```

```
In [112]: 1 len(Gcc) ## Note we have 2 components
```

```
Out[112]: 2
```

```
In [114]: 1 Gcc[1]
```

```
Out[114]: {2, 71}
```

```
In [115]: 1 Gcc[0]
```

```
Out[115]: {3,  
4,  
5,  
6,  
7,  
8,  
9,  
10,  
11,  
12,  
13,  
14,  
15,  
16,  
17,  
18,  
19,  
20,  
21,  
22}
```

```
In [116]: 1 G = g.subgraph(Gcc[0])
```

See: [Reading_SocialNetwork.ipynb](#)

Note you need to use `nx.connected_components(g)` if the graph is undirected

Important, this step creates a Graph G with all the nodes in the largest Connected Component of the dataset

Class Summary

- Definitions of Degree, Clustering Coefficient, shortest path, shortest path length, and average shortest path length
- We need to extract the largest connected component if the network is disconnected
- Three python notebook scripts: MyFirstNetwork_ExerciseSoln.ipynb, Example_ShortestPath_and_CC.ipynb and Reading_SocialNetwork.ipynb

For Lecture 3

- Do the Assignment 1_part 1, and bring questions to lecture
- Watch the Six Degree documentary:
<https://www.youtube.com/watch?v=2rzxAyY7D7k> and participate here:
<https://docs.google.com/presentation/d/1gZnjE7jvMaQ39Bos6jB0iT5nz-fYeBujsAi3EI3Z6Vo/edit?usp=sharing> (Class participation 10%)
- Read the article **Collective dynamics of ‘small-world’ networks uploaded in the folder Lecture 3**, we'll go through the Participation slides of the Documentary

Office Hours

- Marta: Tuesdays 4:00-5:30 PM @ Room 406c and @ Zoom
Thursdays 9:00-11:00 by appointment via email (20 min)
<https://berkeley.zoom.us/j/4124372482>
- Giuseppe: Wednesdays 11:10-1pm, @Davis 305A or
link: <https://berkeley.zoom.us/my/perona>
- Martin: Thursdays 1-3pm, @Davis 305A or
<https://berkeley.zoom.us/j/7628895377>
- Register to the piazza site:
<https://piazza.com/berkeley/spring2023/ce88cp88>

Network Elements

- 1) Go to the data repository provided by the NetSci book by Barabasi, here:
<http://networksciencebook.com/translations/en/resources/data.html>
and select 1 dataset to create their graphs based on their lists of edges and nodes.
Describe what the nodes and the links represent (0.5 pt)
Should it be read as directed or undirected graph? (0.5 pt)

- 2) Plot the histogram of degrees of the network (0.5 pt)

- 3) What is the average clustering coefficient in the network? (0.5 pt)

- 4) What is the average shortest path in the network? (1pt)

- 5) What is the largest clustering coefficient in the network? (1pt)

- 6) List the nodes with the largest clustering coefficient (2 pts)

- 7) What is the value of the longest shortest path in the network? (2 pts)

- 8) Write the nodes in longest shortest paths of the network? (2 pts)

Properties Learned
Today

In `ReadingSocialNetwork.ipynb` we analyze the Results of a School Survey

In `ReadingSocialNetwork.ipynb` we analyze the Results of a School Survey

SchoolEdges.csv

Source	Target	Type	Id	Label	Weight
2	71	Directed	2126	1.0	
3	37	Directed	2127	1.0	
3	41	Directed	2128	1.0	
3	105	Directed	2129	1.0	
4	35	Directed	2130	2.0	
4	62	Directed	2131	1.0	
4	100	Directed	2132	4.0	
4	110	Directed	2133	2.0	
5	4	Directed	2134	5.0	
5	23	Directed	2135	5.0	
5	46	Directed	2136	5.0	
5	49	Directed	2137	5.0	
5	56	Directed	2138	3.0	
6	17	Directed	2139	2.0	
6	55	Directed	2140	2.0	
6	110	Directed	2141	3.0	
7	24	Directed	2142	2.0	
7	34	Directed	2143	1.0	
7	39	Directed	2144	2.0	
7	40	Directed	2145	2.0	
7	45	Directed	2146	2.0	
7	48	Directed	2147	1.0	
7	69	Directed	2148	1.0	
7	92	Directed	2149	1.0	
9	35	Directed	2150	3.0	
9	38	Directed	2151	3.0	
9	65	Directed	2152	2.0	

Reading_SocialNetwork.ipynb

Define Graph and Read the Edges

```
In [2]: 1 g = nx.DiGraph()

In [3]: 1 fl=pd.read_csv('SchoolEdges.csv',delimiter=' ')
2 fl.columns = list(map(str.lower, fl.columns)) #change to lower case

In [4]: 1 fl.columns

Out[4]: Index(['source', 'target', 'type', 'id', 'label', 'weight'], dtype='object')

In [5]: 1 fl
```

```
Out[5]:
   source target      type    id  label  weight
0       2     71  Directed  2126    NaN    1.0
1       3     37  Directed  2127    NaN    1.0
2       3     41  Directed  2128    NaN    1.0
3       3    105  Directed  2129    NaN    1.0
4       4     35  Directed  2130    NaN    2.0
...
450    110     29  Directed  2579    NaN    5.0
451    110     60  Directed  2580    NaN    3.0
452    110     62  Directed  2581    NaN    5.0
453    110     80  Directed  2582    NaN    3.0
454    110     97  Directed  2583    NaN    6.0
```

455 rows × 6 columns

```
In [6]: 1 for L in fl.index.values:
2     g.add_edge(fl['source'][L],fl['target'][L],weight=fl['weight'][L])
```

```
In [7]: 1 g.in_degree()

Out[7]: InDegreeView({2: 1, 71: 1, 3: 3, 37: 4, 41: 7, 105: 4, 4: 4, 35: 5, 62: 2, 100: 6, 110: 6, 5: 3, 23: 3, 46: 5, 49: 5, 56: 5, 6: 0, 17: 2, 55: 2, 7: 17, 24: 12, 34: 8, 39: 9, 40: 18, 45: 14, 48: 11, 69: 12, 92: 12, 9: 6, 38: 6, 65: 6, 104: 7, 10: 3, 77: 5, 11: 2, 21: 2, 63: 5, 82: 4, 84: 10, 87: 3, 102: 6, 111: 4, 12: 1, 19: 2, 50: 6, 70: 2, 14: 1, 25: 1, 59: 4, 68: 2, 81: 2, 103: 3, 107: 2, 15: 7, 16: 2, 57: 5, 95: 3, 96: 4, 18: 2, 8: 4, 13: 10, 28: 3, 90: 4, 97: 7, 101: 1, 20: 0, 88: 2, 22: 1, 36: 4, 94: 4, 26: 11, 43: 3, 27: 0, 31: 3, 42: 4, 52: 7, 30: 0, 32: 7, 74: 4, 79: 4, 106: 9, 33: 2, 51: 6, 72: 5, 58: 9, 109: 4, 80: 3, 108: 3, 75: 6, 99: 2, 47: 0, 85: 2, 91: 3, 53: 1, 54: 1, 44: 2, 61: 1, 29: 2, 66: 1, 78: 2, 76: 0, 60: 3, 83: 1, 73: 3, 86: 0, 93: 1, 89: 0, 98: 1})
```

Lab (Group Exercise)

1- Calculate the Clustering Coefficient of each node and of the School friendship network

2- Calculate the Clustering Coefficient of of the School friendship network

3-Calculate the average shortest path of the School friendship network

Use Example_ShortestPath_and_CC.ipynb and Reading_SocialNetwork.ipynb

Add your name and lastname and answer here:

https://docs.google.com/presentation/d/10VYRXs5Xg44CfxBK3x42Lsf-vpBfQteu4S50nm33FaE/edit#slide=id.g1fdb202be52_0_0