Assignment 4: Sobol

Taylor Cook

2025-04-25

Part 1:

Write a paragraph describing how results of the sensitivity analysis reported on in the paper might contribute to understanding (or prediction) within an environmental problem solving or management context.

Exploring snow model parameter sensitivity using Sobol' variance decomposition

The sensitivity analysis results reported in the paper contribute significantly to environmental problem solving and management by identifying which snow model parameters most influence model outputs under both current and projected climate conditions. By using the Sobol' variance decomposition method on two types of snow models (SNOW-17 and VIC), the study reveals which parameters (such as maximum melt factor in SNOW-17 and albedo decay rates in VIC) most affect snow water equivalent (SWE) predictions. In a management and climate change context, knowing which parameters drive the greatest variability allows managers to better account for uncertainty in future snowpack predictions. This could help guide planning for water supplies, reservoir operations, and drought preparedness in snow-dependent regions. Overall, the sensitivity analysis strengthens the ability to predict environmental responses to changing conditions and supports more resilient and adaptive decision-making frameworks.

Part 2

Question 1: Use the Sobel approach to generate parameter values for the 4 parameters

```
#windspeed in Catm function is in m/s
# generate two examples of random number from parameter distributions
# v = mean of 300 cm/s (3 m/s) and a SD of 50 cm/s (0.5 m/s)
# height = 3.5 and 5.5 m
# k_o and k_d = SD of 1% of default values

np <- 1000
k_o <- rnorm(mean = 0.1, sd = 0.1 * 0.01, n = np)
k_d <- rnorm(mean = 0.7, sd = 0.7 * 0.01, n = np)
v <- rnorm(mean = 3, sd = 0.5, n = np)
height <- runif(min = 3.5, max = 5.5, n = np)

X1 <- cbind.data.frame(k_o, k_d, v, height = height)
# repeat sampling
k_o <- rnorm(mean = 0.1, sd = 0.1 * 0.01, n = np)</pre>
```

```
k_d <- rnorm(mean = 0.7, sd = 0.7 * 0.01, n = np)
v <- rnorm(mean = 3, sd = 0.5, n = np)
height <- runif(min = 3.5, max = 5.5, n = np)

X2 <- cbind.data.frame(k_o, k_d, v, height = height)

# Use Sobel to generate parameter values for the 4 parametes
sens_Catm_Sobol <- sobolSalt(model = NULL, X1, X2, nboot = 100)</pre>
```

Question 2: Run the atmospheric conductance model for these parameters

```
# run atmosph conductance model for all parameter sets
parms <- as.data.frame(sens_Catm_Sobol$X)</pre>
colnames(parms) <- colnames(X1)</pre>
res <- pmap_dbl(parms, Catm)</pre>
sens_Catm_Sobol <- sensitivity::tell(sens_Catm_Sobol, res, res.names = "ga")</pre>
# main effect: partitions variance (main effect without co-variance) - sums approximately to one
sens_Catm_Sobol$S
##
         original
                         bias std. error
                                            min. c.i. max. c.i.
## X1 0.010591640 0.003220669 0.03606085 -0.06698960 0.08128997
## X2 0.008419687 0.002978815 0.03658677 -0.07338363 0.07949393
## X3 0.810938977 0.001572555 0.01071977 0.78863910 0.83056994
## X4 0.194454302 0.002541174 0.03230506 0.12713739 0.26306898
# add row names
row.names(sens_Catm_Sobol$S) <- colnames(parms)</pre>
sens_Catm_Sobol$S
##
             original
                             bias std. error min. c.i. max. c.i.
## k_o
         0.010591640 0.003220669 0.03606085 -0.06698960 0.08128997
## k d
          0.008419687 \ 0.002978815 \ 0.03658677 \ -0.07338363 \ 0.07949393
          0.810938977\ 0.001572555\ 0.01071977\ 0.78863910\ 0.83056994
## v
## height 0.194454302 0.002541174 0.03230506 0.12713739 0.26306898
# total effect - accounts for parameter interactions, is the T in the code
row.names(sens_Catm_Sobol$T) <- colnames(parms)</pre>
sens_Catm_Sobol$T
                                      std. error min. c.i.
##
             original
                               bias
## k o
         0.003145451 1.082868e-05 0.0002001431 0.002640237 0.003517924
## k_d
          0.002588719 -2.188234e-06 0.0001844076 0.002078675 0.002929420
          0.823112144 2.427676e-04 0.0350786267 0.757250007 0.891424487
## height 0.172831392 -1.735551e-03 0.0100685302 0.152116100 0.194874735
```

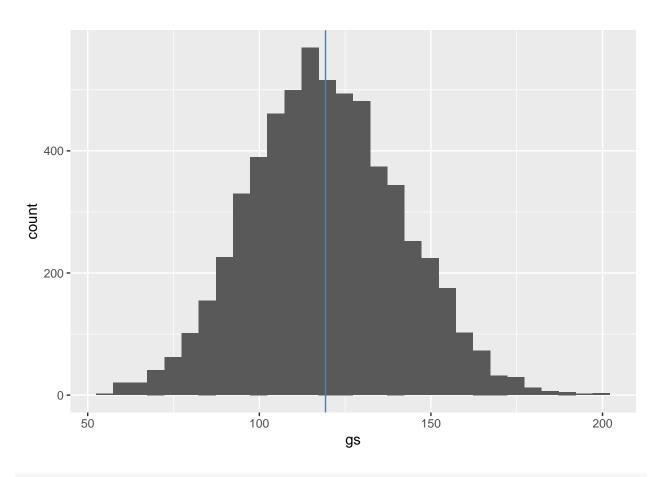
```
print(sens_Catm_Sobol)
##
## Call:
## sobolSalt(model = NULL, X1 = X1, X2 = X2, nboot = 100)
##
## Model runs: 6000
##
## Model variance: 474.9105
##
## First order indices:
            original
                            bias std. error
                                             min. c.i. max. c.i.
## k_o 0.010591640 0.003220669 0.03606085 -0.06698960 0.08128997
         0.008419687 0.002978815 0.03658677 -0.07338363 0.07949393
## k_d
         0.810938977 0.001572555 0.01071977 0.78863910 0.83056994
## height 0.194454302 0.002541174 0.03230506 0.12713739 0.26306898
## Total indices:
##
            original
                              bias
                                     std. error
                                                  min. c.i.
                                                              max. c.i.
## k_o 0.003145451 1.082868e-05 0.0002001431 0.002640237 0.003517924
         0.002588719 -2.188234e-06 0.0001844076 0.002078675 0.002929420
## k_d
         0.823112144 2.427676e-04 0.0350786267 0.757250007 0.891424487
## v
## height 0.172831392 -1.735551e-03 0.0100685302 0.152116100 0.194874735
```

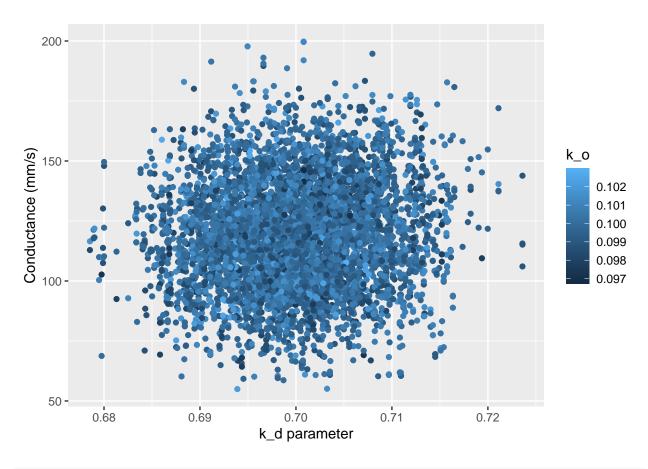
Question 3: Plot conductance estimates in a way that accounts for parameter uncertainty

```
# graph two most sensitive parameters
sens_params <- cbind.data.frame(parms, gs = sens_Catm_Sobol$y)

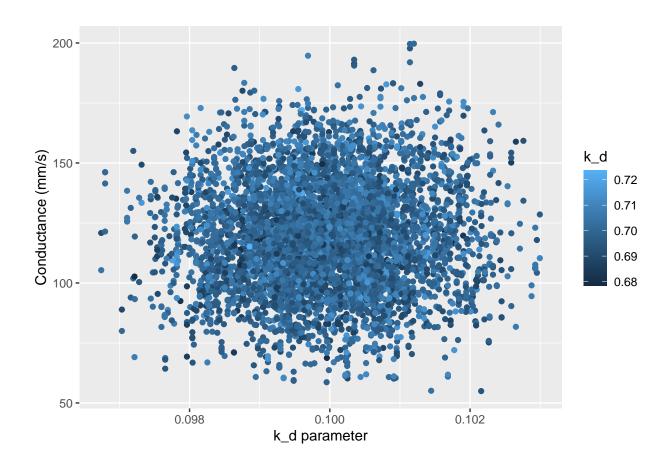
# look at overall gs sensitivity to uncertainty
ggplot(sens_params, aes(x = gs)) +
   geom_histogram() +
   geom_vline(xintercept = mean(sens_params$gs), col = "steelblue")</pre>
```

'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.





```
# use second most sensitive parameter (using most important as color)
ggplot(sens_params, aes(k_o, gs, col = k_d)) +
  geom_point() +
  labs(y = "Conductance (mm/s)", x = "k_d parameter")
```



Question 4: Plot conductance estimates against windspeed use the parameter that is 2nd in terms of total effect on response

```
#2nd paramater of total effect
T_vals <- sens_Catm_Sobol$T$original</pre>
names(T_vals) <- rownames(sens_Catm_Sobol$T)</pre>
# Sort descending
sorted_T <- sort(T_vals, decreasing = TRUE)</pre>
# View ranking
sorted_T
##
                      height
                                      k_o
                                                   k_d
## 0.823112144 0.172831392 0.003145451 0.002588719
#2nd paramet of main effect
S_vals <- sens_Catm_Sobol$S$original</pre>
names(S_vals) <- rownames(sens_Catm_Sobol$S)</pre>
# Sort descending
sorted_S <- sort(S_vals, decreasing = TRUE)</pre>
```

```
# View ranking
sorted_S
##
                      height
## 0.810938977 0.194454302 0.010591640 0.008419687
ggplot(sens_params, aes(v, gs, col = height)) +
  geom_point() +
  labs(y = "Conductance (mm/s)", x = "Windspeed")
   200 -
Conductance (mm/s)
                                                                                        height
                                                                                             5.0
                                                                                             4.5
                                                                                             4.0
     50 -
```

Question 5: Estimate the Sobel Indices for your output

Windspeed

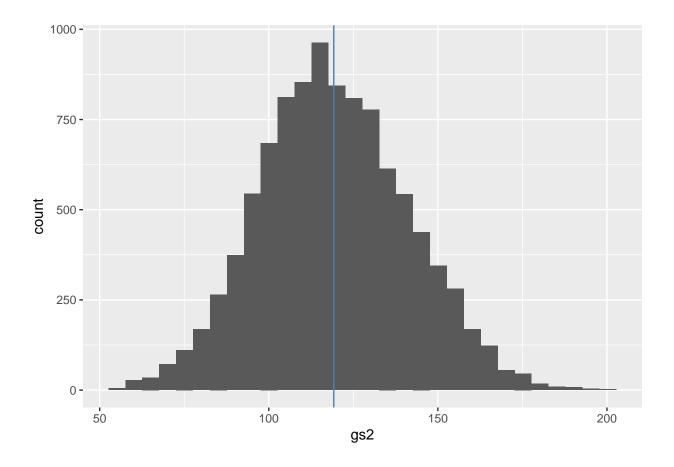
```
sens_Catm_Sobol2 <- sobolSalt(model = NULL, X1, X2, nboot = 100, scheme = "B")

parms2 <- as.data.frame(sens_Catm_Sobol2$X)
colnames(parms2) <- colnames(X1)
res <- pmap_dbl(parms2, Catm)

sens_Catm_Sobol2 <- sensitivity::tell(sens_Catm_Sobol2, res, res.names = "ga")</pre>
```

```
# main effect
row.names(sens_Catm_Sobol2$S) <- colnames(parms2)</pre>
sens Catm Sobol2$S
##
            original
                             bias std. error
                                                min. c.i. max. c.i.
## k o
         0.010951860 0.0055117772 0.034692669 -0.06975497 0.07657343
         ## k_d
         0.816271064 \ -0.0002180543 \ 0.008077769 \ \ 0.80052574 \ 0.83382680
## v
## height 0.182558328 0.0048101181 0.032432116 0.12217729 0.24609598
# total effect
row.names(sens_Catm_Sobol2$T) <- colnames(parms2)</pre>
sens_Catm_Sobol2$T
##
            original
                             bias
                                    std. error min. c.i.
         0.003140867 -2.494872e-06 0.0001865630 0.002751235 0.003465927
## k_o
         0.002664338 -9.522304e-06 0.0001506058 0.002322482 0.002918742
## k_d
## v
         0.811652506 -5.461729e-03 0.0317950962 0.752923989 0.873181280
## height 0.178573218 -2.681534e-05 0.0077691174 0.161538090 0.194765787
# parameters are in order,
sens_Catm_Sobol2$S2
                            bias std. error min. c.i. max. c.i.
##
           original
## X1X2 -0.006563884 -0.005080330 0.03480351 -0.07003237 0.07152647
## X1X3 -0.007350767 -0.005363915 0.03461603 -0.07251555 0.07305801
## X1X4 -0.007532728 -0.005224275 0.03483620 -0.07111795 0.07044697
## X2X3 -0.006953073 -0.005335519 0.03460861 -0.07151287 0.07136158
## X2X4 -0.005414604 -0.005012020 0.03457741 -0.06834785 0.07158364
## X3X4 -0.004465052 -0.004574903 0.03284812 -0.06883808 0.06143503
#If you cross 0 (negative number) in the Confidence interval, it means it is not significant
#Plot the sobol indices
sens params2 <- cbind.data.frame(parms2, gs2 = sens Catm Sobol2$y)
ggplot(sens_params2, aes(x = gs2)) +
 geom_histogram() +
 geom_vline(xintercept = mean(sens_params2$gs2), col = "steelblue")
```

'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



Question 5: Comment on what this tells you about how atmospheric conductance and its sensitivity to variation in compared to the setting that we examined in class where wind speed was lower and less variable and vegetation was taller.

The sensitivity analysis analysis reveals that wind speed (v) is the dominant driver of variation in atmospheric conductance under this scenario. The total effect Sobol index for v is approximately 0.85, indicating that most of the variance in conductance is directly attributable to changes in wind speed alone. Vegetation height (height) also contributes meaningfully, though to a much lesser extent (\sim 18%). In contrast, the conductance parameters k_o and k_d have negligible total effects, suggesting they do not significantly influence conductance in this scenario, either independently or through interactions.

This contrasts with the setting we examined in class, where wind speed was lower and less variable, and vegetation was taller. In that context, k_0 and k_1 were more influential, likely because the system was less driven by wind and more sensitive to plant-level physiological parameters. The shift in sensitivity observed here underscores how increased wind variability amplifies the importance of v in driving conductance, while the role of vegetation structure and internal resistances (k_0 , k_1) becomes relatively less important.