## VE 492 Homework6

Due: 23:59, July.1st

(a) For the following questions, you will be given a set of probability tables and a set of conditional independence assumptions. Given these tables and independence assumptions, write an expression for the requested

## Q1. Probability

probability tables. Keep in mind that your expressions probability tables. If it is not possible, mark "Not possi		
(i) Using probability tables $P(A)$ , $P(A \mid C)$ , $P(B \mid C)$ , tions, write an expression to calculate the table $P(A)$	$\mathbf{P}(\mathbf{C} \mid \mathbf{A}, \mathbf{B})$ and no conditional independence assump-	
$\mathbf{P}(\mathbf{A}, \mathbf{B} \mid \mathbf{C}) =$	O Not possible.	
(ii) Using probability tables P(A), P(A   C), P(B   A), tions, write an expression to calculate the table P(		
P(A)P(B A)P(C A,B)		
$\mathbf{P}(\mathbf{B} \mid \mathbf{A}, \mathbf{C}) = \frac{\sum_{b} \mathbf{P}(\mathbf{A}) \mathbf{P}(\mathbf{B}   \mathbf{A}) \mathbf{P}(\mathbf{C}   \mathbf{A})}{\sum_{b} \mathbf{P}(\mathbf{A}) \mathbf{P}(\mathbf{B}   \mathbf{A}) \mathbf{P}(\mathbf{C}   \mathbf{A})}$	(A, B) (Not possible.	
(iii) Using probability tables $P(A \mid B), P(B), P(B \mid A, C), P(C \mid A)$ and conditional independence assumption $A \perp \!\!\! \perp B$ , write an expression to calculate the table $P(C)$ .		
$\mathbf{P}(\mathbf{C}) = \frac{\sum_{a} \mathbf{P}(\mathbf{A} \mathbf{B})\mathbf{P}(\mathbf{C} \mathbf{A})}{\bigcirc \text{ Not possible.}}$		
$\mathbf{P}(\mathbf{C}) = \frac{\mathbf{Z}_{a}}{a}$	O Not possible.	
(iv) Using probability tables $P(A \mid B, C), P(B), P(B \mid A, C), P(C \mid B, A)$ and conditional independence assumption $A \perp \!\!\!\perp B \mid C$ , write an expression for $P(A, B, C)$ .		
$\mathbf{P}(\mathbf{A}, \mathbf{B}, \mathbf{C}) = $	O Not possible.	
(b) For each of the following equations, select the minima	$l\ set$ of conditional independence assumptions necessary	
for the equation to be true. (i) $P(A, C) = P(A   B) P(C)$		
	$\Box B \perp \!\!\! \perp C$	
$\begin{array}{ c c c c c c }\hline & A \perp \!\!\! \perp B \mid C\\\hline & A \perp \!\!\! \perp C\end{array}$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	
$\Box A \perp \!\!\!\perp C \mid B$		
(ii) $P(A \mid B, C) = \frac{P(A) P(B A) P(C A)}{P(B C) P(C)}$		
$\Box A \perp \!\!\!\perp B$	$\Box B \perp C$	
$\begin{array}{c} \square & A \perp \!\!\! \perp B \mid C \\ \square & A \perp \!\!\! \perp C \end{array}$		
$\Box  A \perp\!\!\!\perp C \mid B$		
(iii) $\mathbf{P}(\mathbf{A},\mathbf{B}) = \sum_{\mathbf{c}} \mathbf{P}(\mathbf{A} \mid \mathbf{B},\mathbf{c}) \; \mathbf{P}(\mathbf{B} \mid \mathbf{c}) \; \mathbf{P}(\mathbf{c})$		
$\begin{array}{c} \square & A \perp \!\!\! \perp B \\ \square & A \perp \!\!\! \perp B \mid C \end{array}$		
$\begin{array}{c} \square & A \perp \!\!\! \perp C \\ \square & A \perp \!\!\! \perp C \mid B \end{array}$	☐ No independence assumptions needed.	
$\mathbf{(iv)}\ \mathbf{P}(\mathbf{A},\mathbf{B}\mid\mathbf{C},\mathbf{D}) = \mathbf{P}(\mathbf{A}\mid\mathbf{C},\mathbf{D})\ \mathbf{P}(\mathbf{B}\mid\mathbf{A},\mathbf{C},\mathbf{D})$		
$\begin{array}{c} \square & A \perp \!\!\! \perp B \\ \square & A \perp \!\!\! \perp B \mid C \end{array}$	$\begin{array}{c c} \square & C \perp \!\!\! \perp D \mid A \\ \square & C \perp \!\!\! \perp D \mid B \end{array}$	
$ \Box A \perp\!\!\!\perp B \mid D  \Box C \perp\!\!\!\perp D $	☐ No independence assumptions needed.	

$\begin{tabular}{ll} (c) & (i) & {\rm Mark \ all \ expressions \ that \ are \ equal \ to} \end{tabular}$	$P(A \mid B)$ , given no independence assumptions.	
$\Box  \sum_{c} P(A \mid B, c)$		
$\square  \sum_{c} P(A, c \mid B)$		
	☐ None of the provided options.	
(ii) Mark all expressions that are equal to $P(A, B, C)$ , given that $A \perp\!\!\!\perp B$ .		
$\square  P(A \mid C) \ P(C \mid B) \ P(B)$	$\square P(A) P(B \mid A) P(C \mid A, B)$	
$\square  P(A) \ P(B) \ P(C \mid A, B)$	$\square  P(A,C) \ P(B \mid A,C)$	
$\square  P(C) \ P(A \mid C) \ P(B \mid C)$	$\square$ None of the provided options.	
$\square  P(A) \ P(C \mid A) \ P(B \mid C)$		
(iii) Mark all expressions that are equal to $P(A, B \mid C)$ , given that $A \perp\!\!\!\perp B \mid C$ .		
$\square  P(A \mid C) \ P(B \mid C)$		
	$\Box  \frac{P(C, A B) \ P(B)}{P(C)}$	
$\square  P(A \mid B) \ P(B \mid C)$	☐ None of the provided options.	