



# Scheduling: RR, Priority, MLFQ, and Lottery

CS 571: *Operating Systems* (Spring 2020)  
Lecture 5

Yue Cheng

Some material taken/derived from:

- Wisconsin CS-537 materials created by Remzi Arpacı-Dusseau.

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- CPU scheduling worksheet posted on BB

# **Review: FIFO, SJF**

# Workload Assumptions

1. Each job runs for the same amount of time
2. All jobs arrive at the same time
3. All jobs only use the CPU (no I/O)
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# FIFO

- First-In, First-Out: Run jobs in arrival (time) order

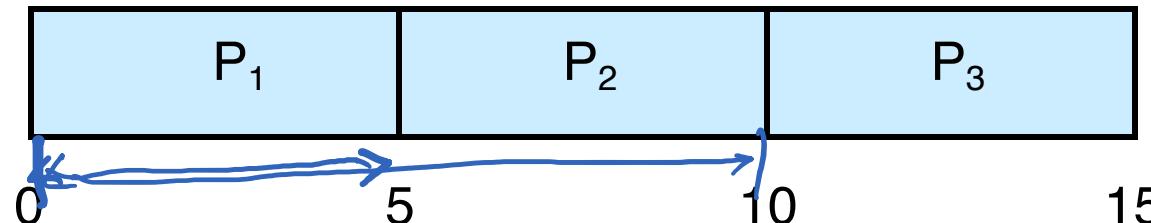
# FIFO

First-In, First-Out: Run jobs in arrival (time) order

*Def:  $\text{waiting\_time} = \underbrace{\text{start\_time}}_{\sim\sim\sim} - \text{arrival\_time}$*

<u>Process</u>	<u>Burst Time</u>
$P_1$	5
$P_2$	5
$P_3$	5

- Suppose that the processes arrive in order:  $P_1, P_2, P_3$   
The Gantt Chart for the schedule:



- Waiting time for  $P_1 = 0$ ;  $P_2 = 5$ ;  $P_3 = 10$        $\frac{15}{3} = 5$
- Average waiting time: 5

# FIFO

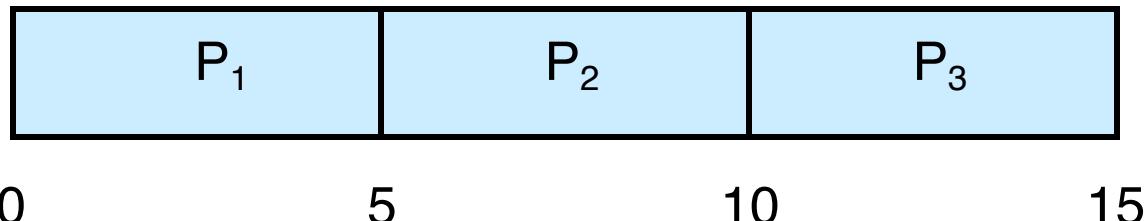
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What is the average turnaround time? (Q2)?

*Def: turnaround\_time = completion\_time – arrival\_time*

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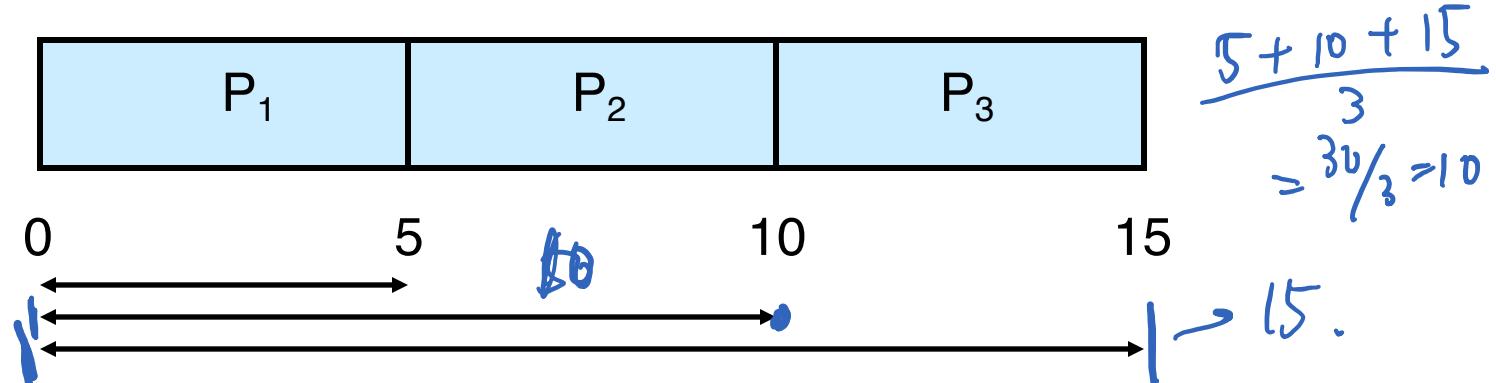
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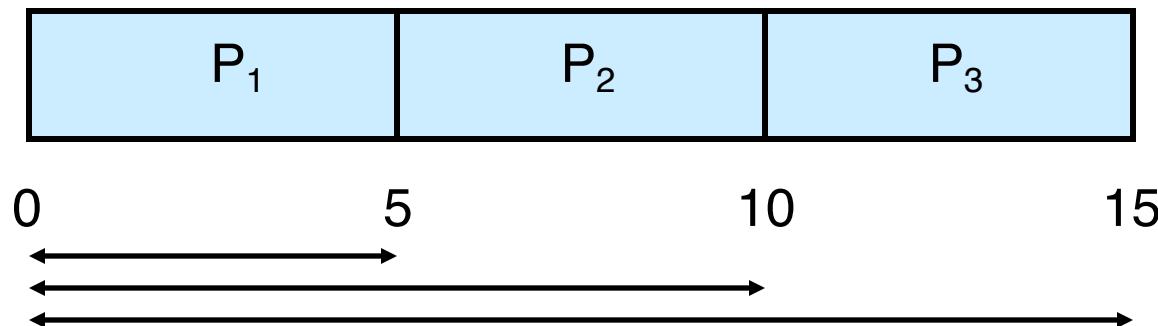
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- Suppose that the processes arrive in order:  $P_1, P_2, P_3$   
The Gantt Chart for the schedule:



Average turnaround time:  $(5+10+15)/3 = 10$

# Workload Assumptions

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# Example: Big First Job

JOB	arrival_time	run_time
P1	~0	80
P2	~0	5
P3	~0	5

What is the average turnaround time? (Q3)



$$\frac{80 + 85 + 90}{3} = \frac{165 + 90}{3} = \frac{255}{3}$$

# Example: Big First Job

JOB	arrival_time	run_time
P1	~0	80
P2	~0	5
P3	~0	5



# Example: Big First Job

JOB	arrival_time	run_time
P1	~0	80
P2	~0	5
P3	~0	5



Average turnaround time:  $(80+85+90) / 3 = 85$

# Convoy Effect



# Better Schedule?



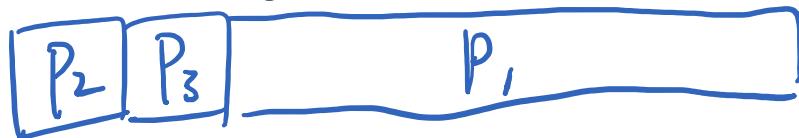
# Passing the Tractor

- New scheduler: SJF (Shortest Job First)
- Policy: When deciding which job to run, choose the one with the smallest run\_time

# Example: SJF

JOB	arrival_time	run_time
P1	~0	80
P2	~0	5
P3	~0	5

What is the average turnaround time with SJF? (Q4)



$$\frac{5 + 10 + 90}{3} = \frac{105}{3}$$

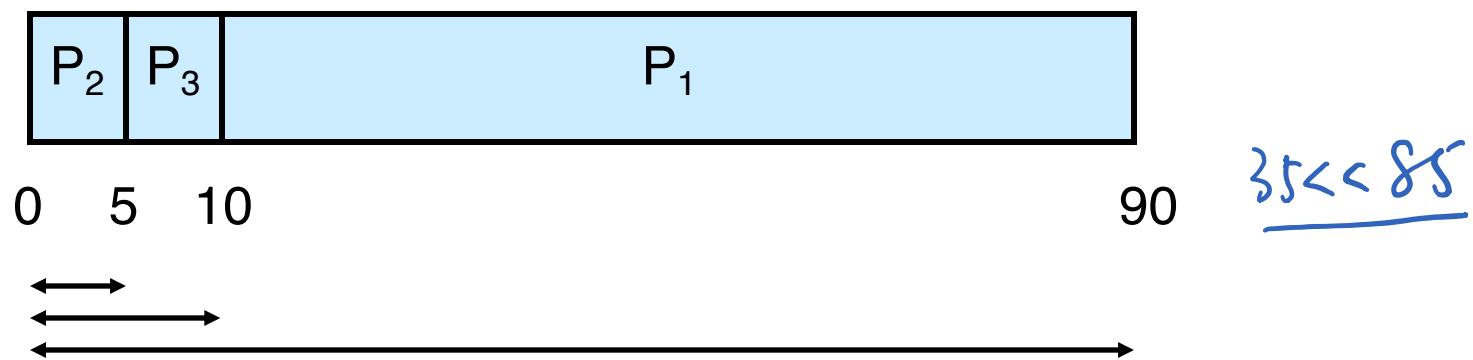
# Example: SJF

JOB	arrival_time	run_time
P1	~0	80
P2	~0	5
P3	~0	5



# Example: SJF

JOB	arrival_time	run_time
P1	~0	80
P2	~0	5
P3	~0	5



Average turnaround time:  $(5+10+90) / 3 = 35$

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# Workload Assumptions

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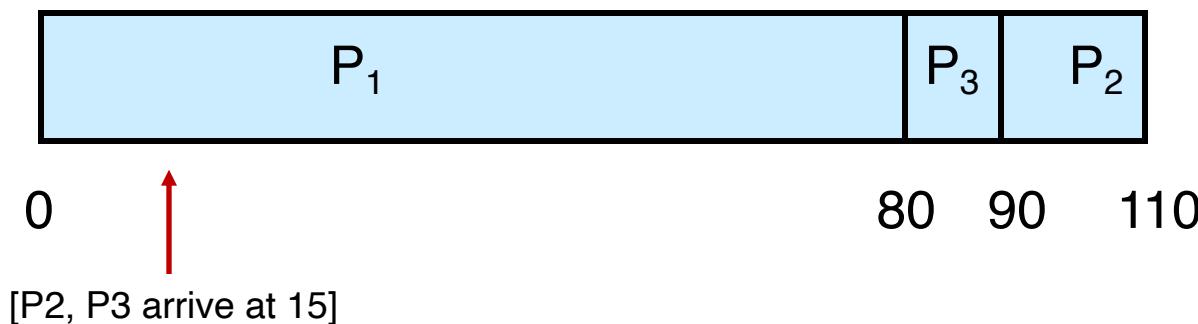
# Shortest Job First (Arrival Time)

JOB	<u>arrival_time</u>	run_time
P1	~0	80
P2	~15	20
P3	~15	10

What is the average turnaround time with SJF? (Q5)

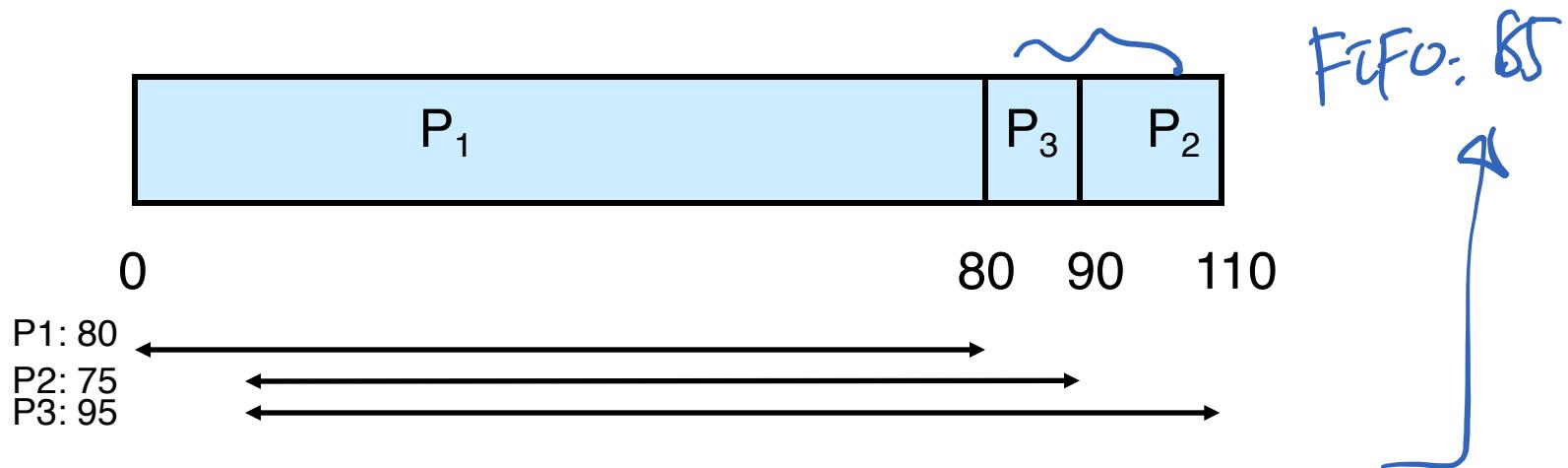
# Shortest Job First (Arrival Time)

JOB	arrival_time	run_time
P1	~0	80
P2	~15	20
P3	~15	10



# Shortest Job First (Arrival Time)

JOB	arrival_time	run_time
P1	~0	80
P2	~15	20
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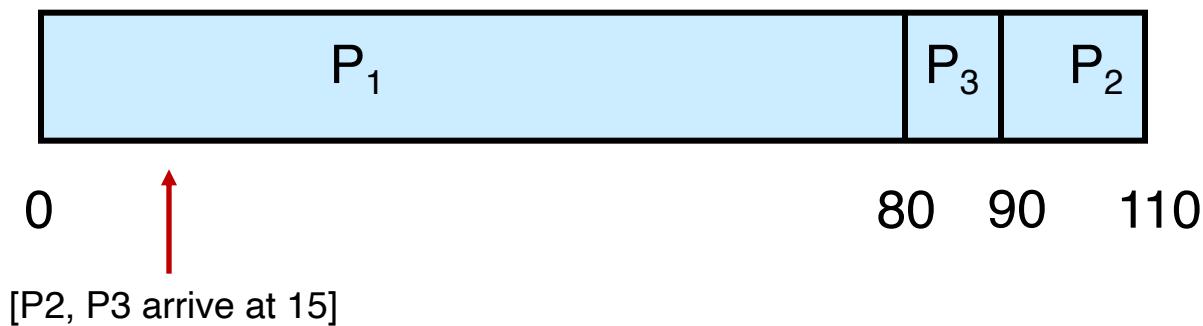
$$\text{Average turnaround time: } (80+75+95) / 3 = \sim 83.3$$

# A Preemptive Scheduler

- Previous schedulers: FIFO and SJF are non-preemptive
- New scheduler: STCF (Shortest Time-to-Completion First)
- Policy: Switch jobs so we always run the one that will complete the quickest

# SJF

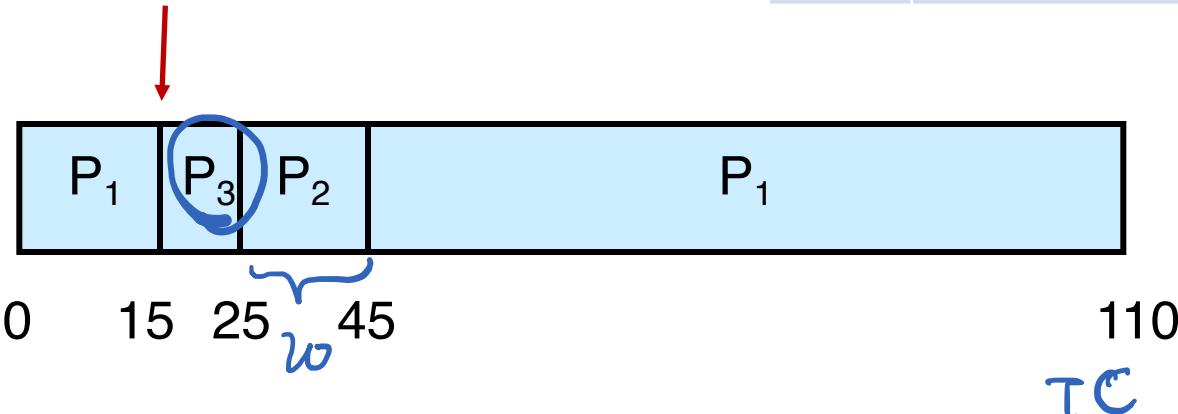
JOB	arrival_time	run_time
P1	~0	80
P2	~15	20
P3	~15	10



# STCF

JOB	arrival_time	run_time
P1	~0	80
P2	~15	20
P3	~15	10

[P2, P3 arrive]



What is the average turnaround time with SRTF? (Q6)

$$P_1 : 110$$

$$P_2 : 45 - 15 = 30$$

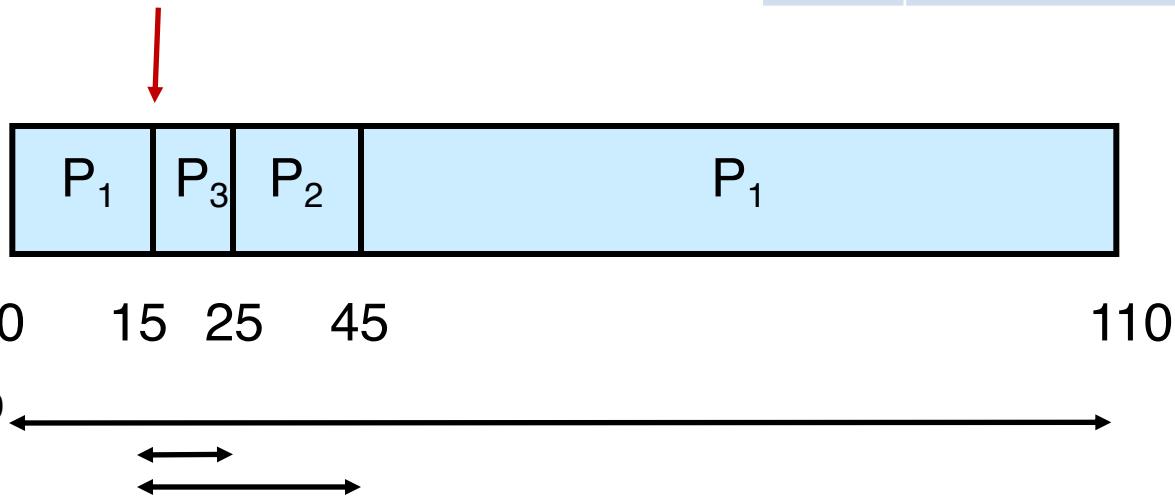
$$P_3 : 25 - 15 = 10$$

TC

**STCF**

JOB	arrival_time	run_time
P1	~0	80
P2	~15	20
P3	~15	10

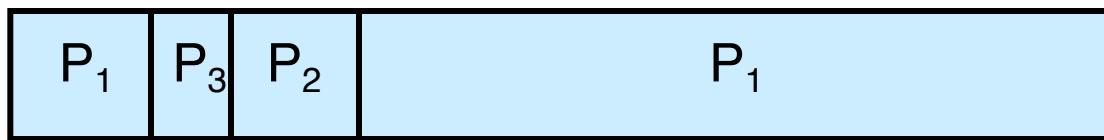
[P2, P3 arrive]



Average turnaround time:  $(110+30+10) / 3 = 50$

# STCF

[P2, P3 arrive]



0      15      25      45                          110

What is the average waiting time with STCF? (Q7)

$$P_1 : 0 + (45 - 15) = 30$$

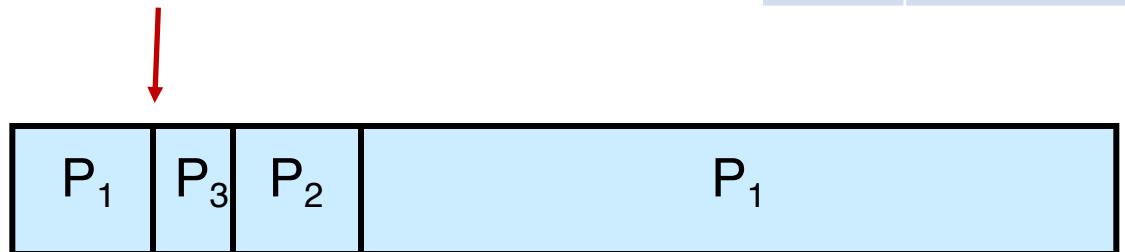
$$P_2 : 25 - 15 = 10$$

$$P_3 : 0$$

**STCF**

JOB	arrival_time	run_time
P1	~0	80
P2	~15	20
P3	~15	10

[P2, P3 arrive]



0 15 25 45 110

P1: 30

P3: 0

P2: 10

Average waiting time:  $(30+10+0) / 3 = \sim 13.3$

# Outline

- Scheduling algorithms
  - First In, First Out (FIFO)
  - Shortest Job First (SJF)
  - Shortest Time-to-Completion First (STCF)
    - Optimality discussion
  - Round Robin (RR)
  - Priority
  - Multi-Level Feedback Queue (MLFQ)
  - Lottery Scheduling

# Optimality of SJF and STCF

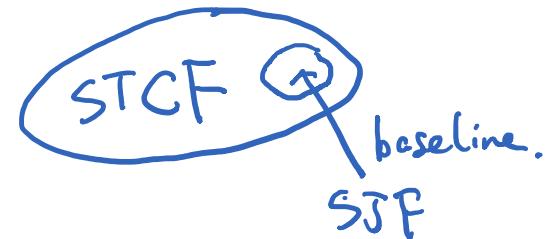
- Non-preemptive SJF is optimal if all the processes are ready simultaneously
  - Gives minimum average waiting time for a given set of processes

# Optimality of SJF and STCF

- Non-preemptive SJF is **optimal** if all the processes are ready simultaneously
  - Gives minimum average waiting time for a given set of processes
- What is the **intuition** behind the **optimality** of STCF?

# Optimality of SJF and STCF

- Non-preemptive SJF is **optimal** if all the processes are ready simultaneously
  - Gives minimum average waiting time for a given set of processes
- What is the **intuition** behind the **optimality** of STCF?
  - A: STCF is optimal, considering a more realistic scenario where all the processes may be arriving at different times



# Optimality of SJF and STCF

- Non-preemptive SJF is optimal if all the processes are ready simultaneously
  - Gives minimum average waiting time for a given set of processes

**Q: What's the problem?**

- We don't exactly know how long a job would run!  
*What is the intuition behind the optimality of SRTF?*
  - A: SRTF is optimal, considering a more realistic scenario where all the processes may be arriving at different times

# Estimating the Length of Next CPU Burst

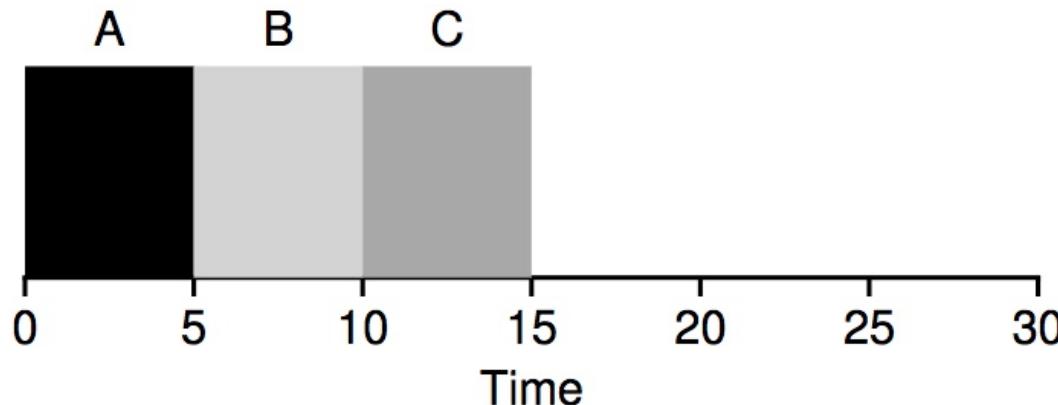
- Idea: Based on the observations in the recent past, we can try to **predict**
- Techniques such as **exponential averaging** are based on combining the observations in the past and our predictions using different **weights**
- Exponential averaging
  - $t_n$ : actual length of the  $n^{th}$  CPU burst
  - $z_{n+1}$ : predicted value for the next CPU burst
  - $$z_{n+1} = k \cdot t_n + (1-k) \cdot z_n$$
  - Commonly,  $k$  is set to  $\frac{1}{2}$

# Response Time

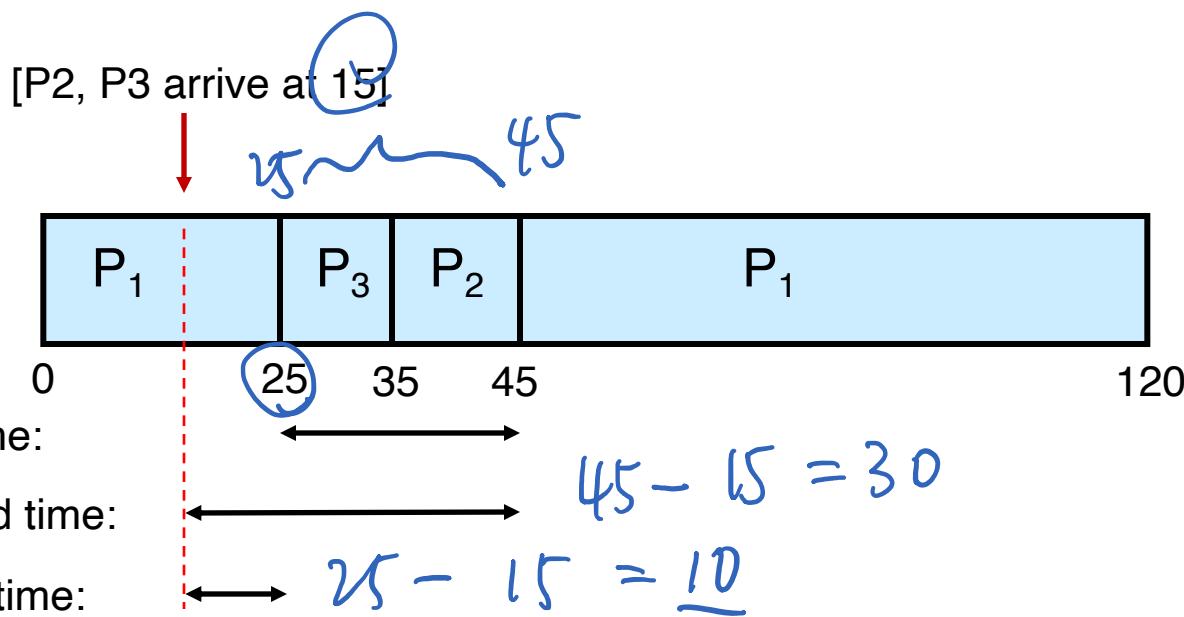
- Response time definition

$$T_{\text{response}} = T_{\text{first\_run}} - T_{\text{arrival}}$$

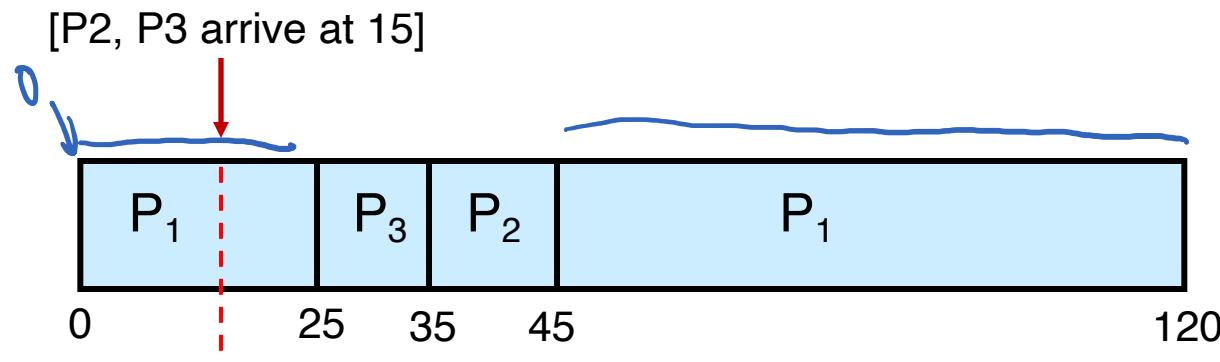
- SJF's average response time (all 3 jobs arrive at same time)
  - $(0 + 5 + 10)/3 = 5$



# Waiting, Turnaround, Response



# Waiting, Turnaround, Response



P1's waiting time:  $0+20=20$

P2's turnaround time:  $45-15=30$

P3's response time:  $25-15=10$

Q: What is P1's response time?

0 .

# Round Robin (RR)

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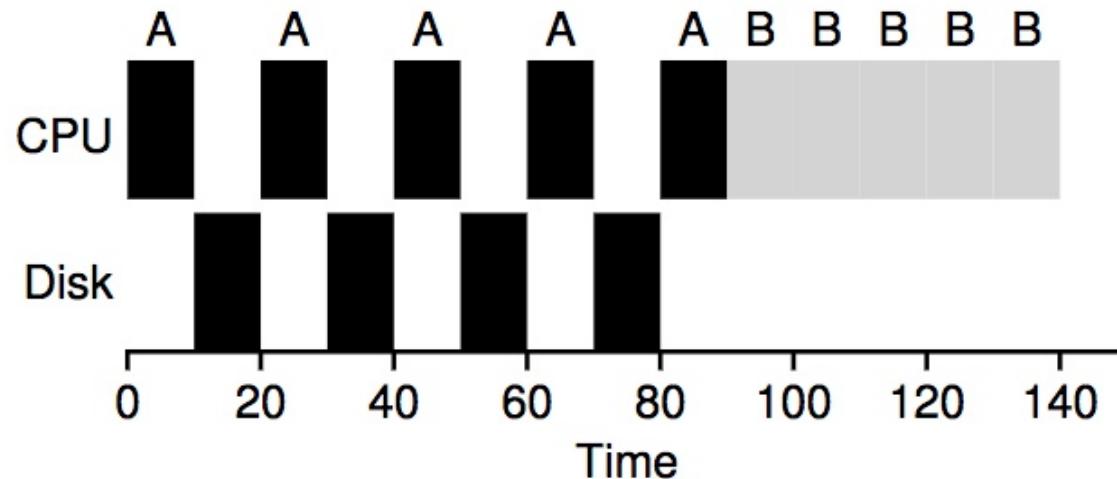
# Extension to Multiple CPU & I/O Bursts

- When the process arrives, it will try to execute its **first** CPU burst
  - It will join the ready queue
  - The priority will be determined according to the underlying scheduling algorithm and considering only that specific (i.e. first) burst
- When it completes its first CPU burst, it will try to perform its **first** I/O operation (burst)
  - It will join the device queue
  - When that device is available, it will use the device for a time period indicated by the length of the first I/O burst.
- Then, it will re-join the ready queue and try to execute its **second** CPU burst
  - Its new priority may now change (as defined by its second CPU burst)!

# Round Robin (RR)

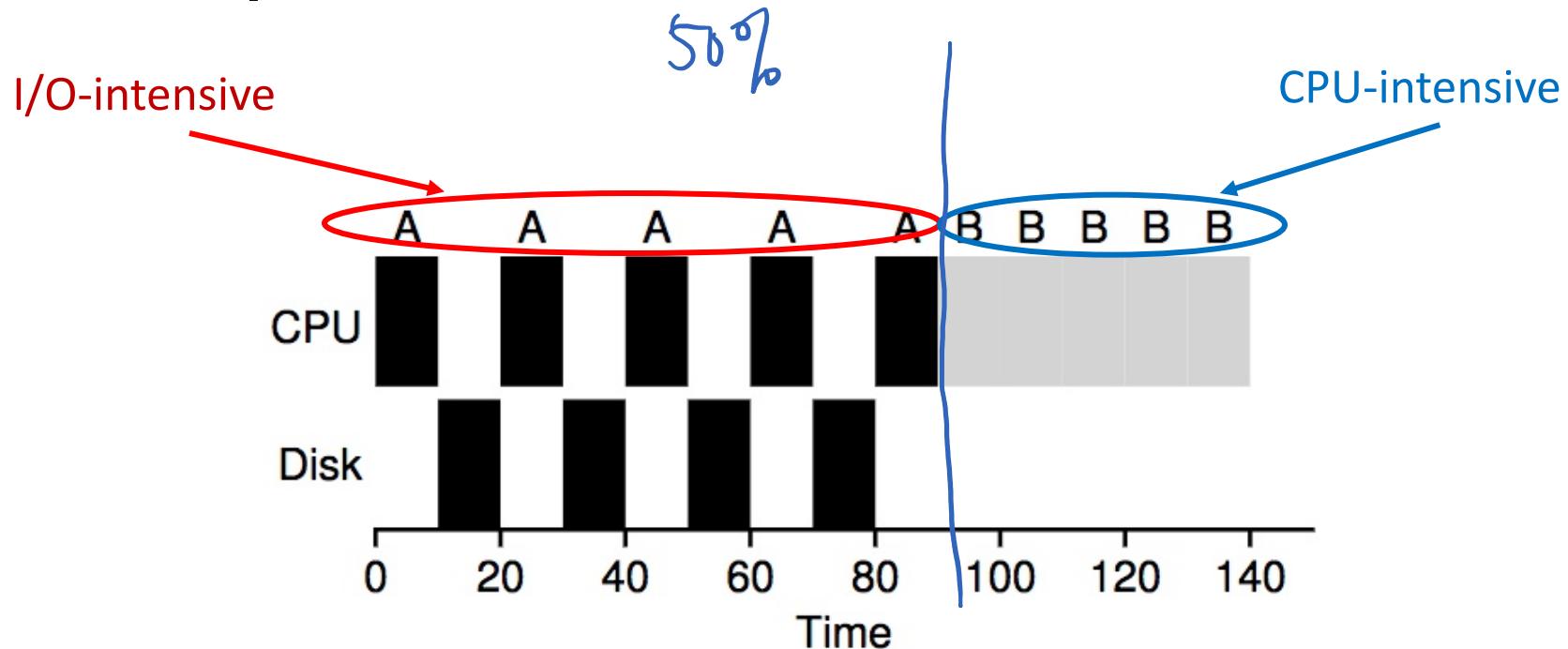
- Each process gets a small unit of CPU time (**time quantum**). After this time has elapsed, the process is preempted and added to the end of the ready queue
- Newly-arriving processes (and processes that complete their I/O bursts) are added to the end of the ready queue
- If there are  $n$  processes in the ready queue and the time quantum is  $q$ , then no process waits more than  $(n-1)q$  time units
- Performance
  - $q$  large  $\Rightarrow$   FIFO
  - $q$  small  $\Rightarrow$  **Processor Sharing** (The system appears to the users as though each of the  $n$  processes has its own processor running at the  $(1/n)^{th}$  of the speed of the real processor)

# Not I/O Aware



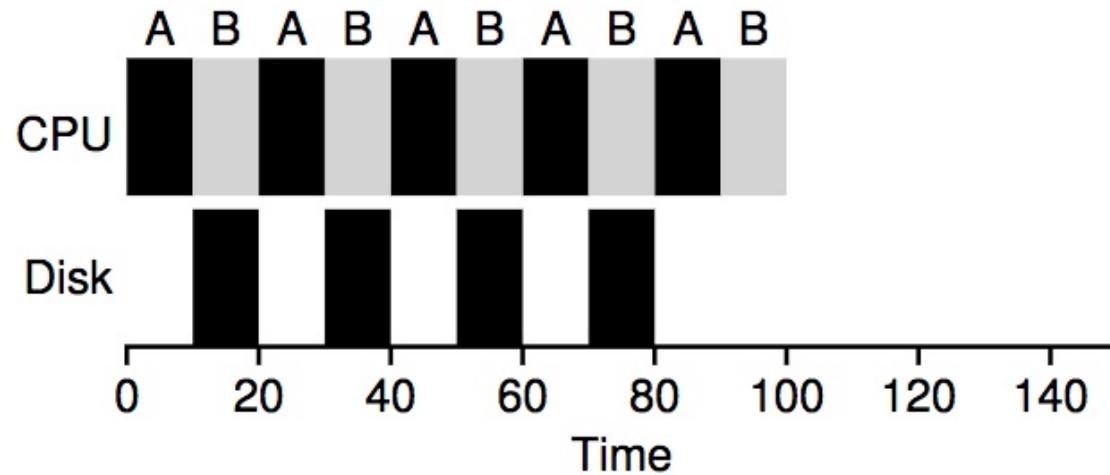
Poor use of resources

# Not I/O Aware



Poor use of resources

# I/O Aware (Overlap)



Overlap allows better use of resources!

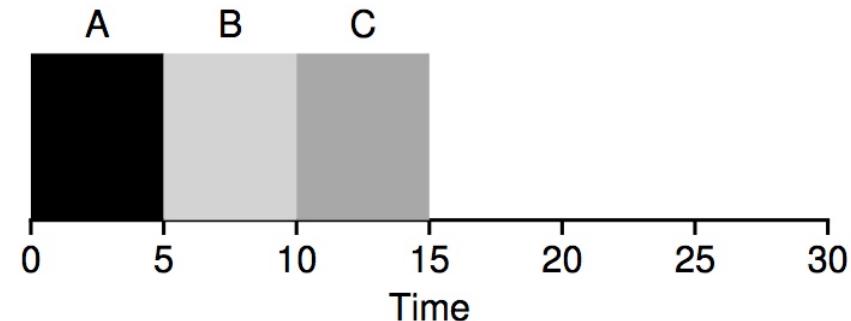
# RR

- SJF's average response time

- $(0 + 5 + 10) / 3 = 5$

*turnaround time*:  $(5 + 10 + 15) / 3$   
 $= 30 / 3 = 10$

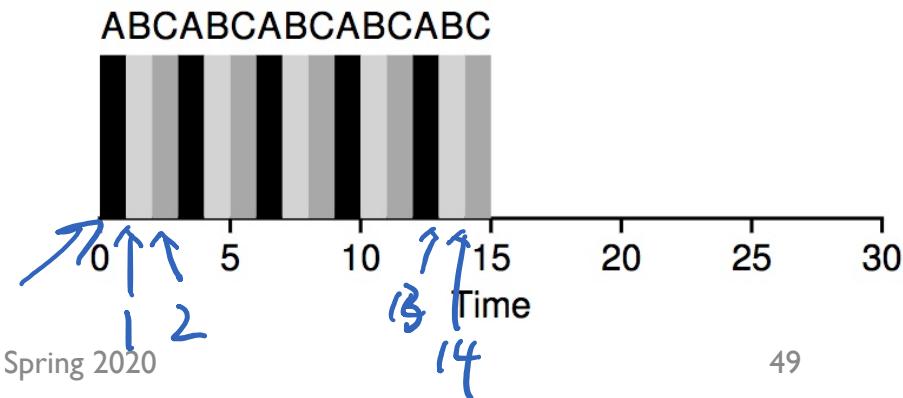
Process	Burst Time
A	5
B	5
C	5



- RR's average response time (time quantum = 1)

- $(0 + 1 + 2) / 3 = 1$

*turnaround time*:  $(13 + 14 + 15) / 3$   
 $= 42 / 3 = 14$

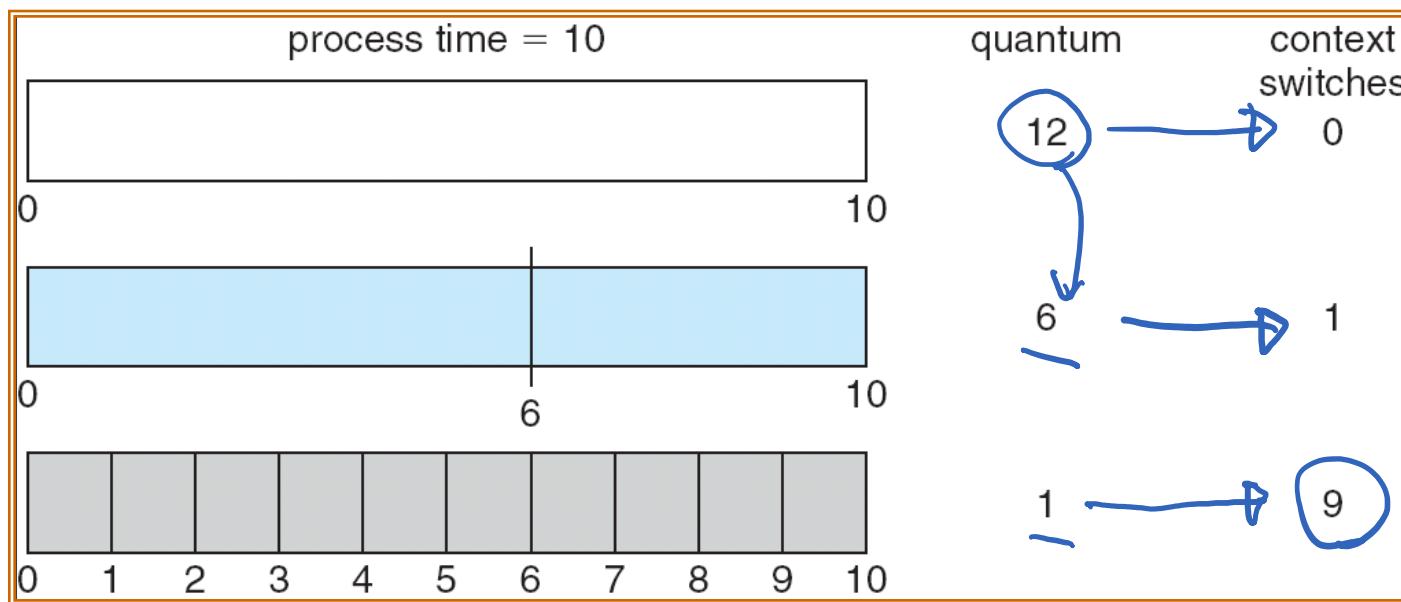


# Tradeoff Consideration

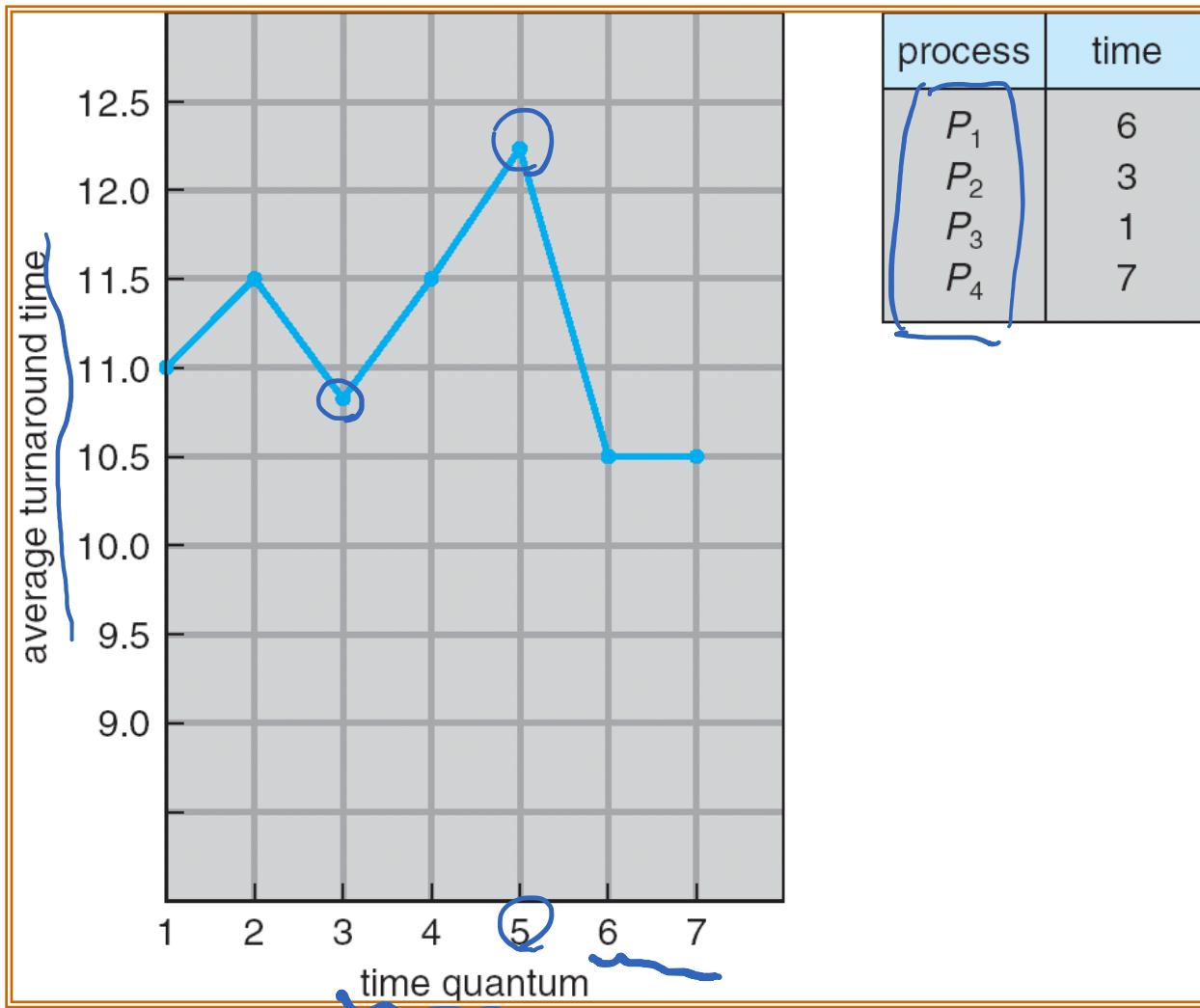
- Typically, RR achieves higher average turnaround time than SJF, but better response time
  - Turnaround time only cares about when processes **finish**
- RR is one of the worst policies
  - -F- turnaround time is the metric

# Choosing a Time Quantum

- The effect of quantum size on context-switching time must be carefully considered
- The time quantum must be large with respect to the context-switch time
- Turnaround time also depends on the size of the time quantum



# Time Quantum vs. Turnaround Time



# Time Quantum vs. Turnaround Time



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# Priority-Based Scheduling

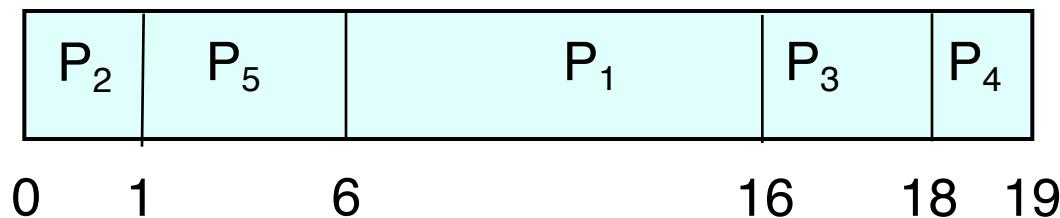
# Priority-Based Scheduling

- A priority number (integer) is associated with each process
- The CPU is allocated to the process with the highest priority
  - (smallest integer ≡ highest priority)
    - Preemptive
    - Non-preemptive

# Example for Priority-Based Scheduling

<u>Process</u>	<u>Burst Time</u>	<u>Priority</u>
$P_1$	10	3
$P_2$	1	1
$P_3$	2	4
$P_4$	1	5
$P_5$	5	2

- Priority scheduling Gantt Chart



- Average waiting time = 8.2

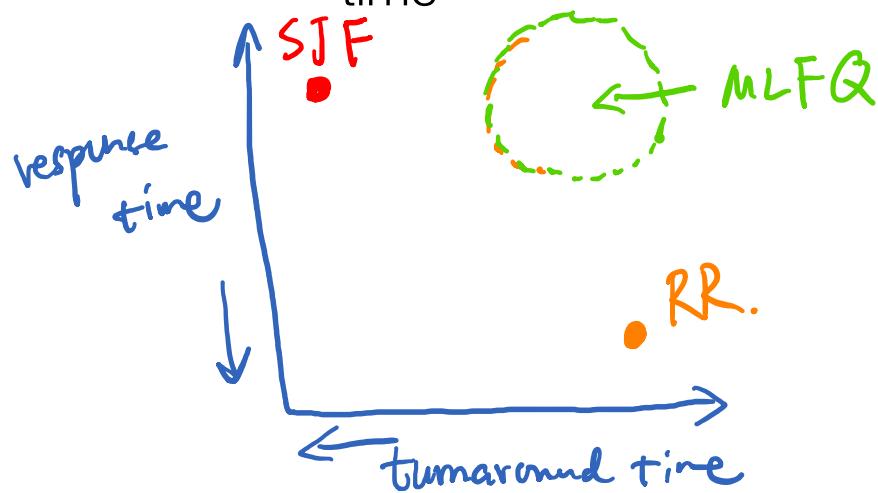
# Priority-Based Scheduling (cont.)

- Priority Assignment
  - Internal factors: timing constraints, memory requirements, the ratio of average I/O burst to average CPU burst ...
  - External factors: Importance of the process, financial considerations, hierarchy among users ...
- Problem: **Indefinite blocking** (or **starvation**) – low priority processes may never execute
- One solution: **Aging**
  - As time progresses increase the priority of the processes that wait in the system for a long time

# **Multi-Level Feedback Queue (MLFQ)**

# Multi-Level Feedback Queue (MLFQ)

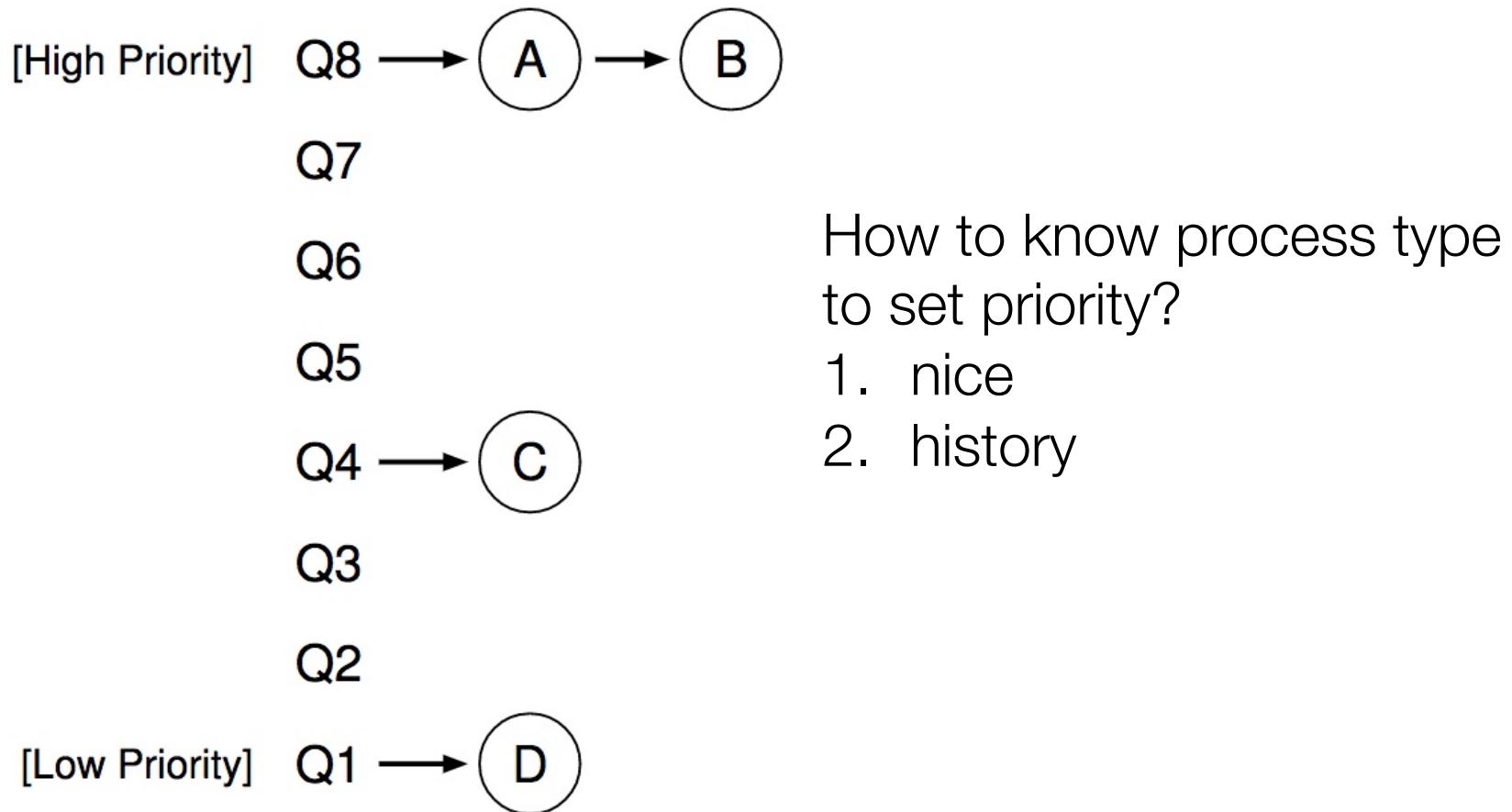
- Goals of MLFQ
  - Optimize turnaround time
    - In reality, SJF does not work since OS does not know how long a process will run
  - Minimize response time
    - Unfortunately, RR is really bad on optimizing turnaround time



# MLFQ: Basics

- MLFQ maintains a number of queues (multi-level queue)
  - Each assigned a different priority level
  - Priority decides which process should run at a given time

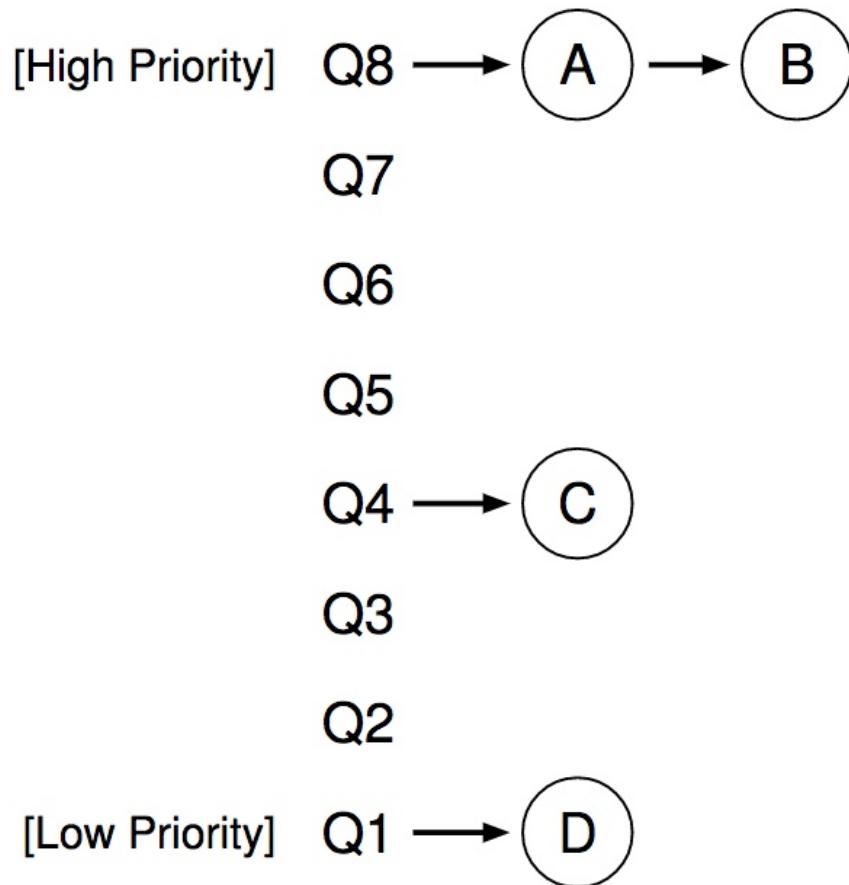
# MLFQ Example



# How to Check Nice Values in Linux?

- % ps ax -o pid,ni,cmd  
*nice value*  
↓

# MLFQ Example



How to know process type to set priority?

1. nice
2. history

In this example, A and B are given high priority to run, while C and D may starve

# MLFQ: Basic Rules

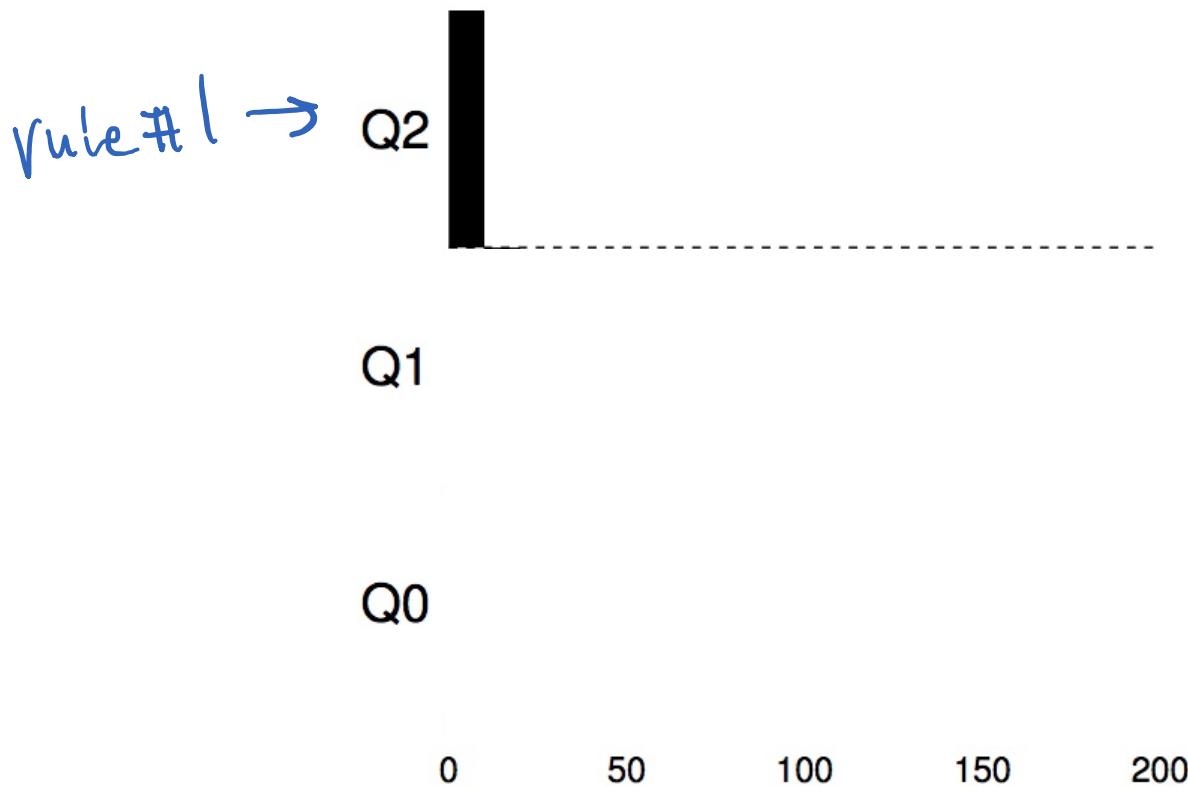
- MLFQ maintains a number of queues (multi-level queue)
  - Each assigned a different priority level
  - Priority decides which process should run at a given time
- **Rule 1:** If  $\text{Priority}(A) > \text{Priority}(B)$ , A runs (B doesn't).
- **Rule 2:** If  $\text{Priority}(A) = \text{Priority}(B)$ , A & B run in RR.  


# Attempt #1: Change Priority

- Workload
  - Interactive processes (many short-run CPU bursts)
  - Long-running processes (CPU-bound)
- Each time quantum = 10ms
- **Rule 3:** When a job enters the system, it is placed at the highest priority (the topmost queue).
- **Rule 4a:** If a job uses up an entire time slice while running, its priority is *reduced* (i.e., it moves down one queue).
- **Rule 4b:** If a job gives up the CPU before the time slice is up, it stays at the *same* priority level.

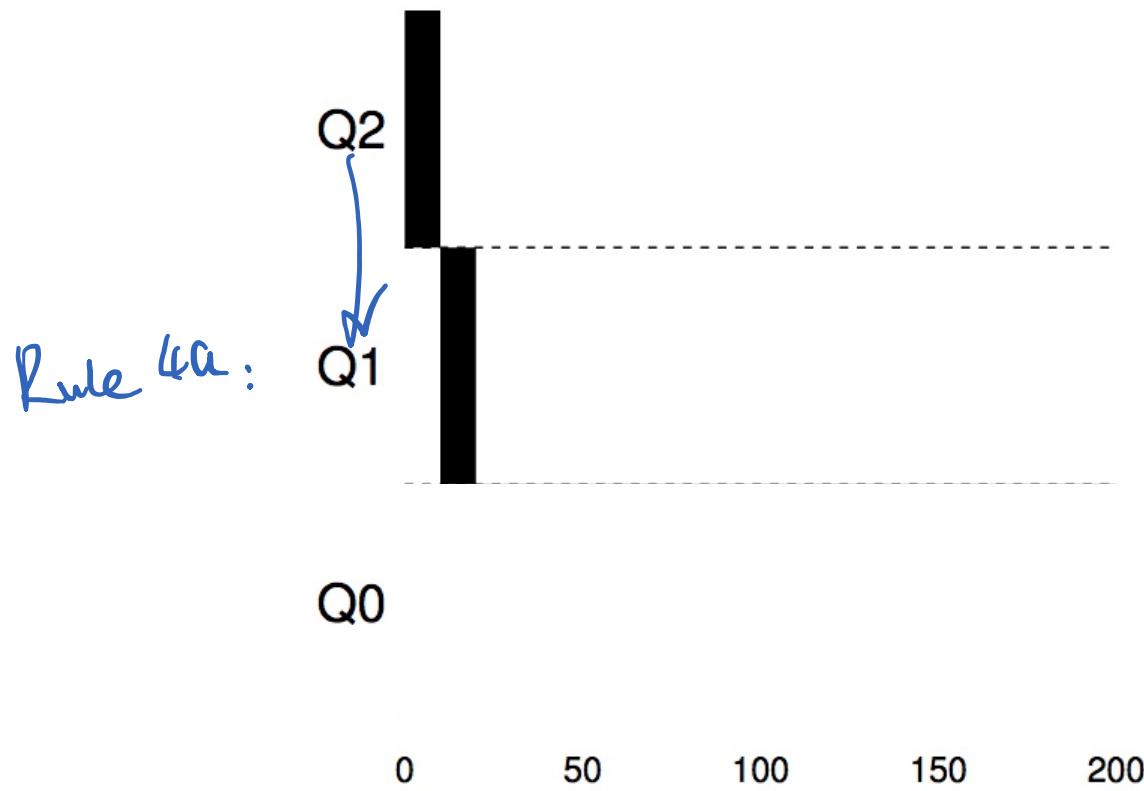
# Example 1: One Single Long-Running Process

- A process enters at highest priority (time quantum = 10ms)



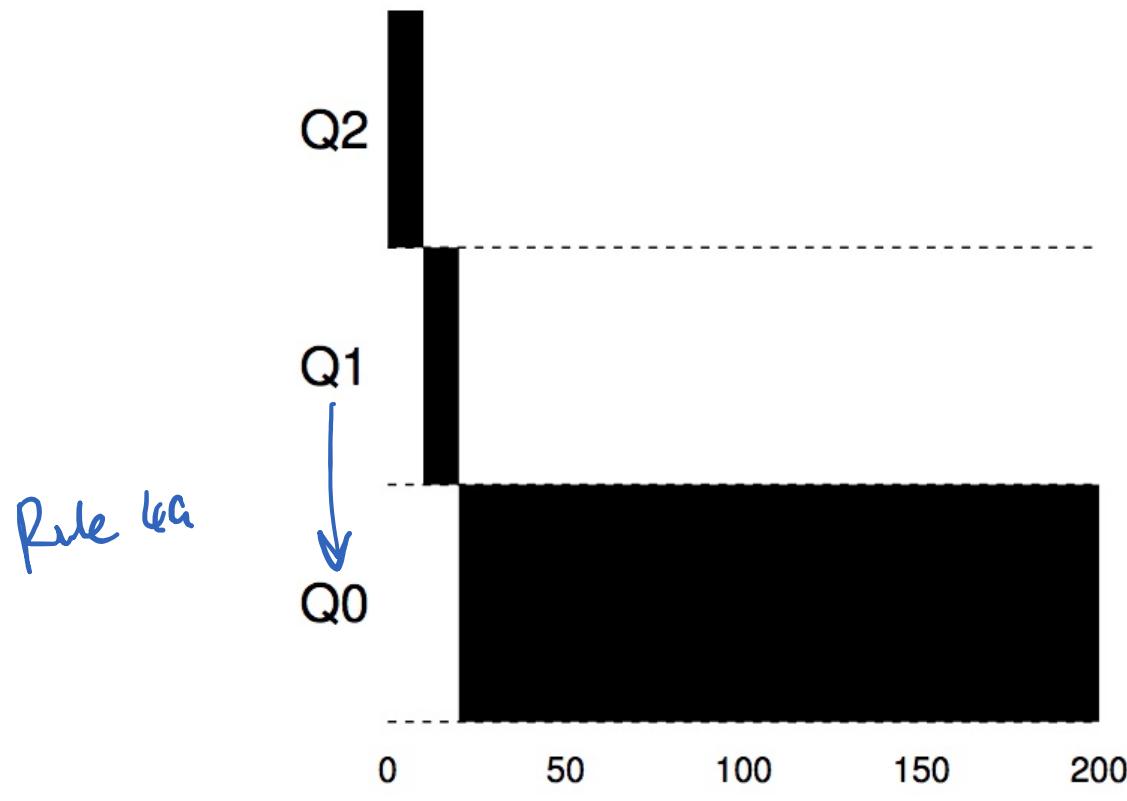
# Example 1: One Single Long-Running Process

- A process enters at highest priority (time quantum = 10ms)



# Example 1: One Single Long-Running Process

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# Example 2: Along Came a Short-Running Process

- Process A: long-running process (start at 0)

Q2

Q1

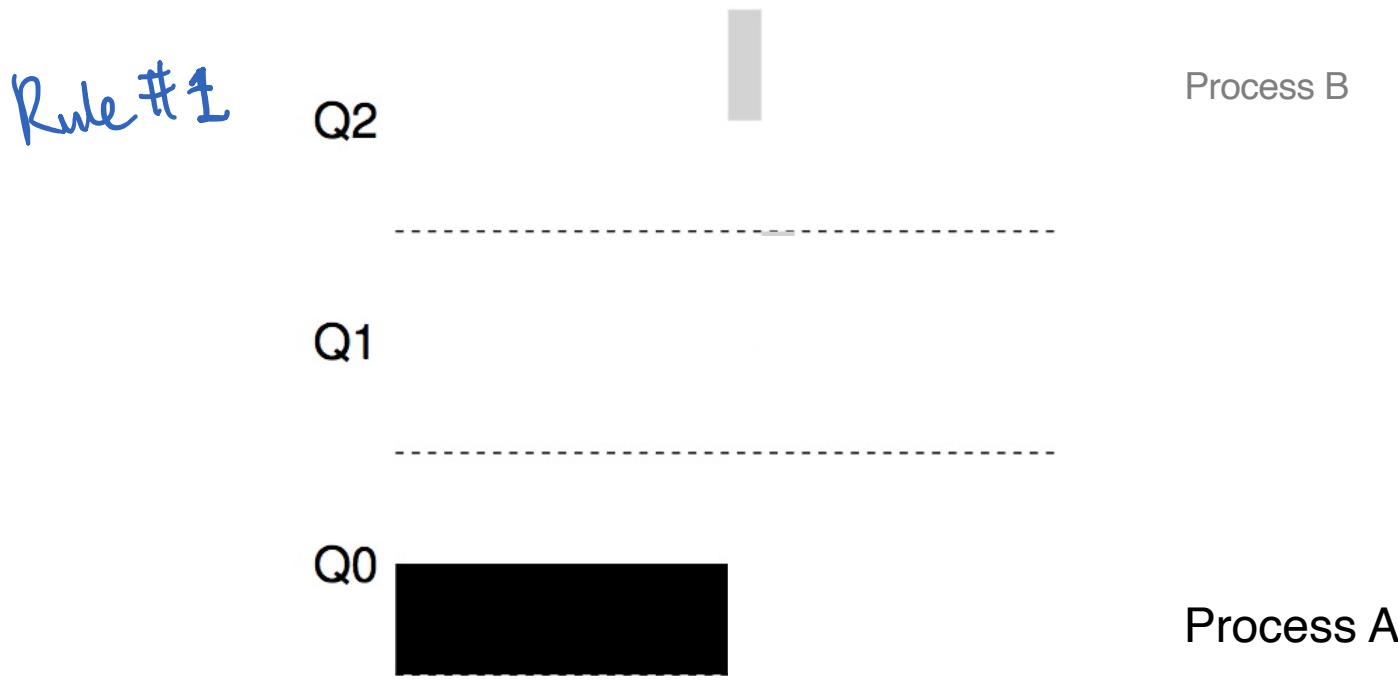
Q0



Process A

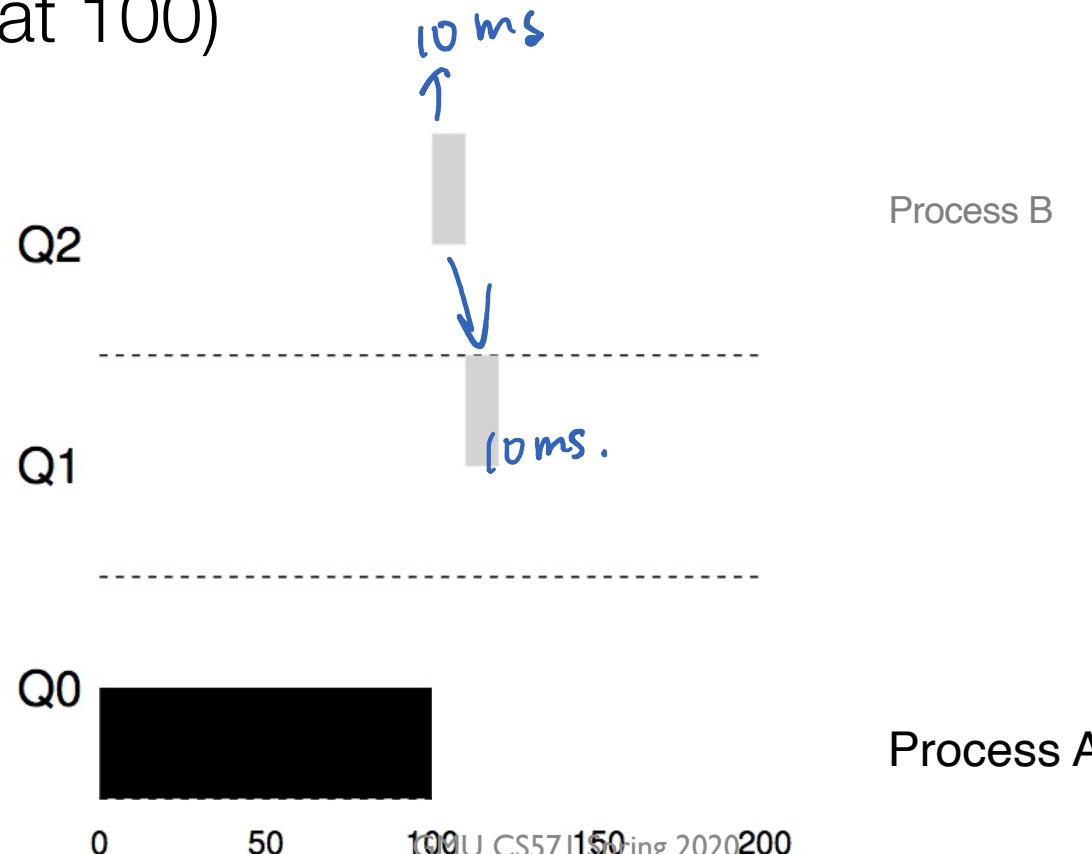
# Example 2: Along Came a Short-Running Process

- Process A: long-running process (start at 0)
- Process B: short-running interactive process (start at 100)



# Example 2: Along Came a Short-Running Process

- Process A: long-running process (start at 0)
- Process B: short-running interactive process (start at 100)



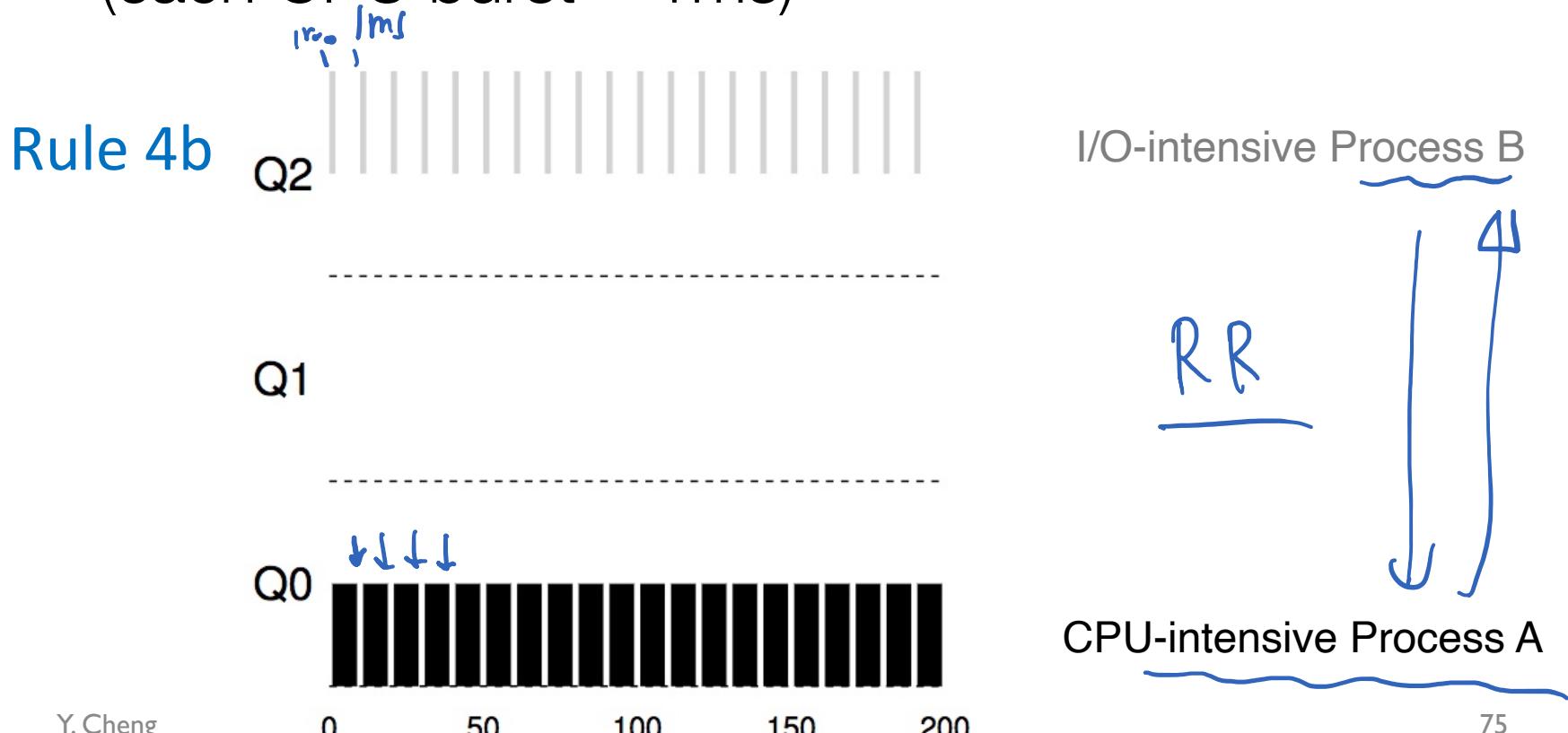
# Example 2: Along Came a Short-Running Process

- Process A: long-running process (start at 0)
- Process B: short-running interactive process (start at 100)



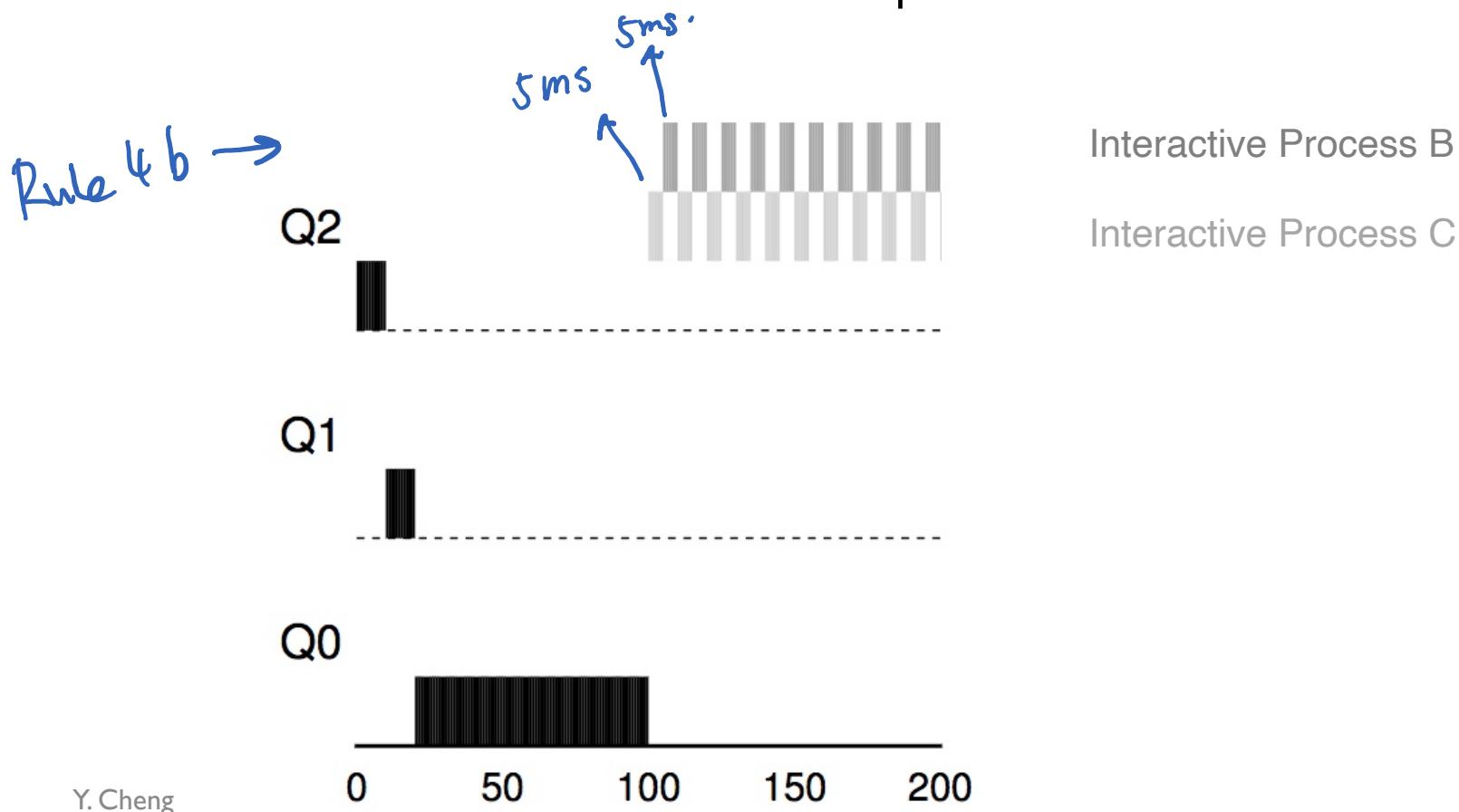
# Example 3: What about I/O?

- Process A: long-running process
- Process B: I/O-intensive interactive process  
(each CPU burst = 1ms)



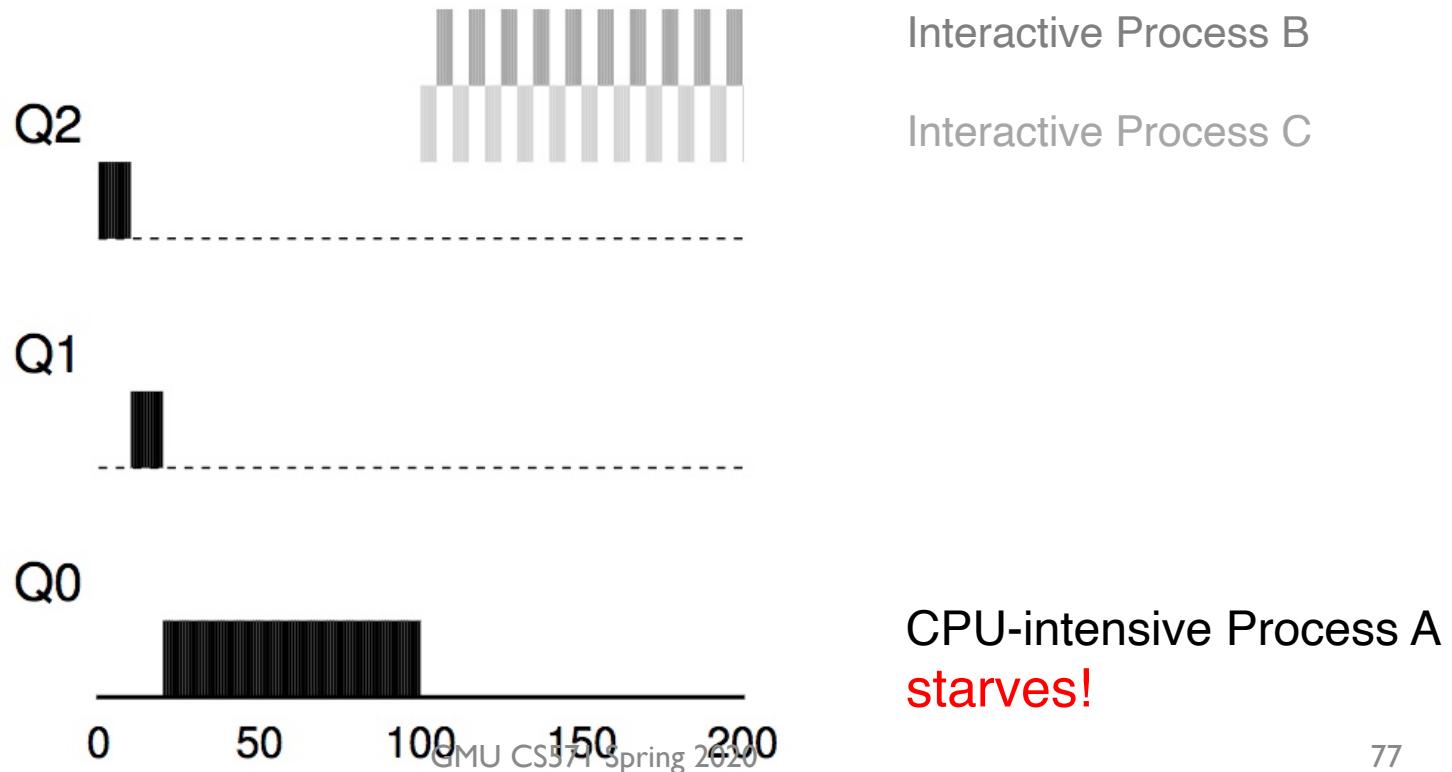
# Example 4: What's the Problem?

- Process A: long-running process
- Process B + C: Interactive process



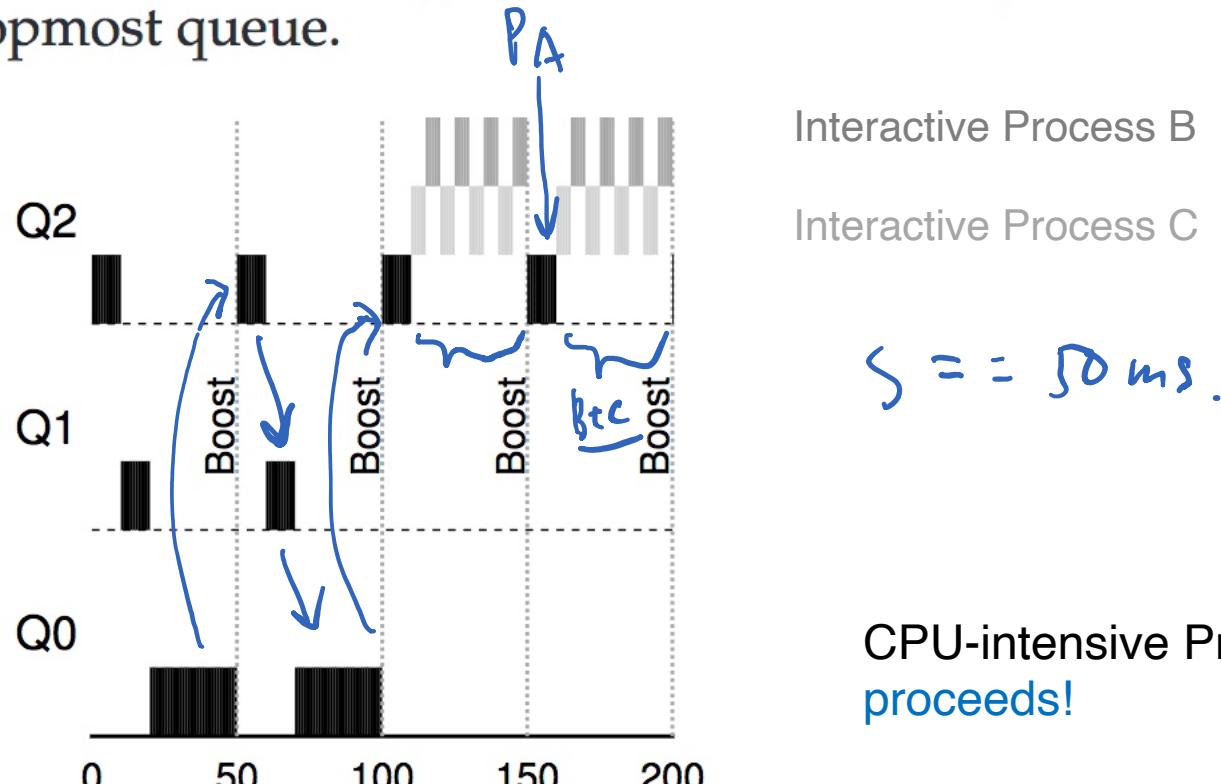
# Example 4: What's the Problem?

- Process A: long-running process
- Process B + C: Interactive process



# Attempt #2: Priority Boost

- Simple idea: Periodically boost the priority of all processes
- Rule 5: After some time period  $S$ , move all the jobs in the system to the topmost queue.



# Tuning MLFQ

- MLFQ scheduler is defined by many parameters:
  - Number of queues
  - Time quantum of each queue
  - How often should priority be boosted?
  - A lot more...
- The scheduler can be configured to match the requirements of a specific system
  - Challenging and requires experience

# Lottery Scheduling

# Lottery Scheduling

- Goal: Proportional share
  - One of the fair-share schedulers
- Approach
  - Gives processes lottery tickets
  - Whoever wins runs
  - Higher priority → more tickets

# Lottery Code

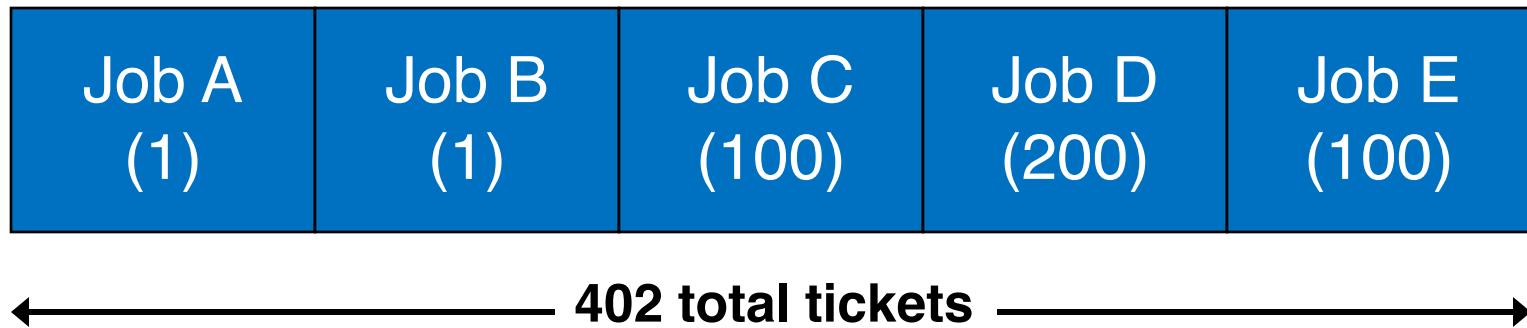
```
1 // counter: used to track if we've found the winner yet
2 int counter = 0;
3
4 // winner: use some call to a random number generator to
5 //         get a value, between 0 and the total # of tickets
6 int winner = getrandom(0, totaltickets);
7
8 // current: use this to walk through the list of jobs
9 node_t *current = head;
10
11 // loop until the sum of ticket values is > the winner
12 while (current) {
13     counter = counter + current->tickets;
14     if (counter > winner)
15         break; // found the winner
16     current = current->next;
17 }
18 // 'current' is the winner: schedule it...
```

# Lottery Scheduling Example



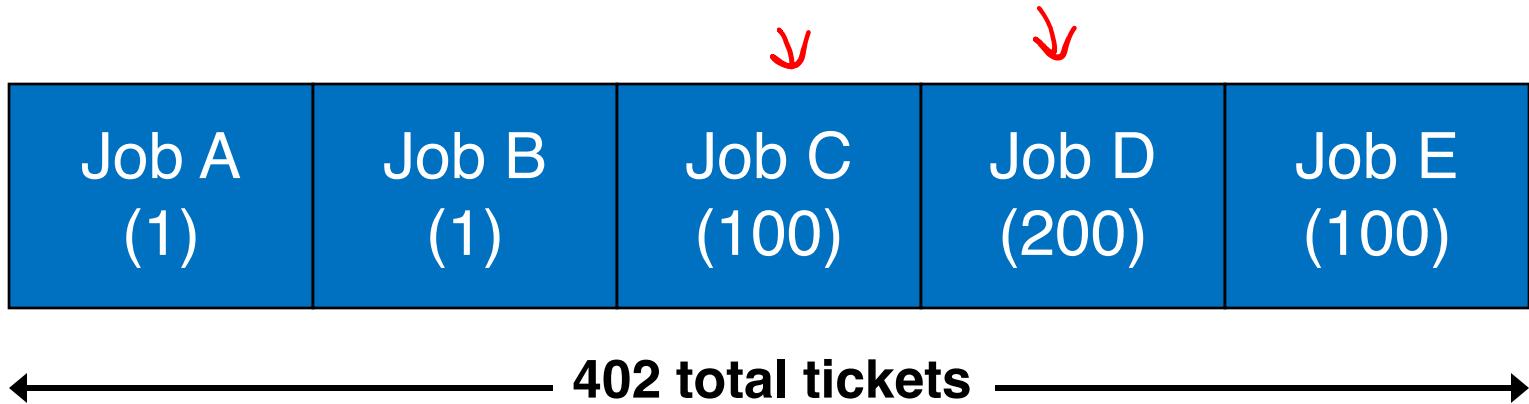
# Lottery Scheduling Example

`winner = random(402)`



# Lottery Scheduling Example

winner = 102



# Lottery Scheduling Example

winner = 102

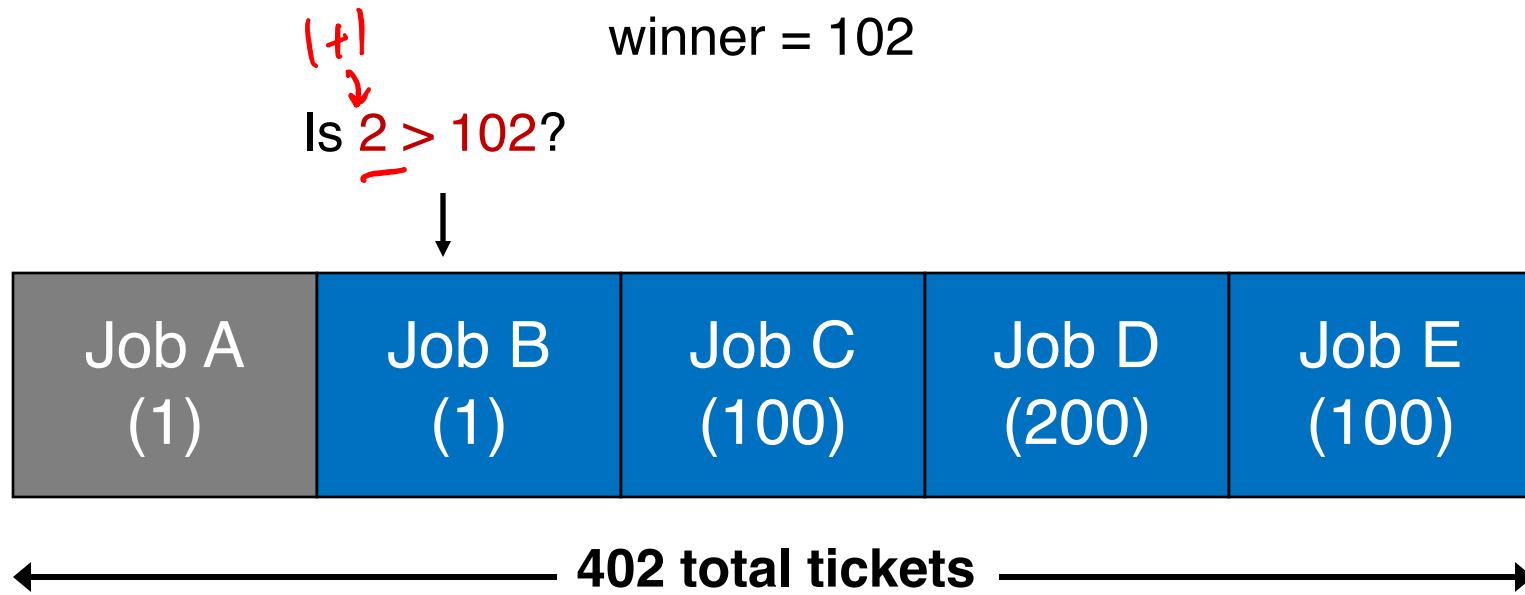
Is 1 > 102?



Job A (1)	Job B (1)	Job C (100)	Job D (200)	Job E (100)
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← 402 total tickets →

# Lottery Scheduling Example



# Lottery Scheduling Example

winner = 102

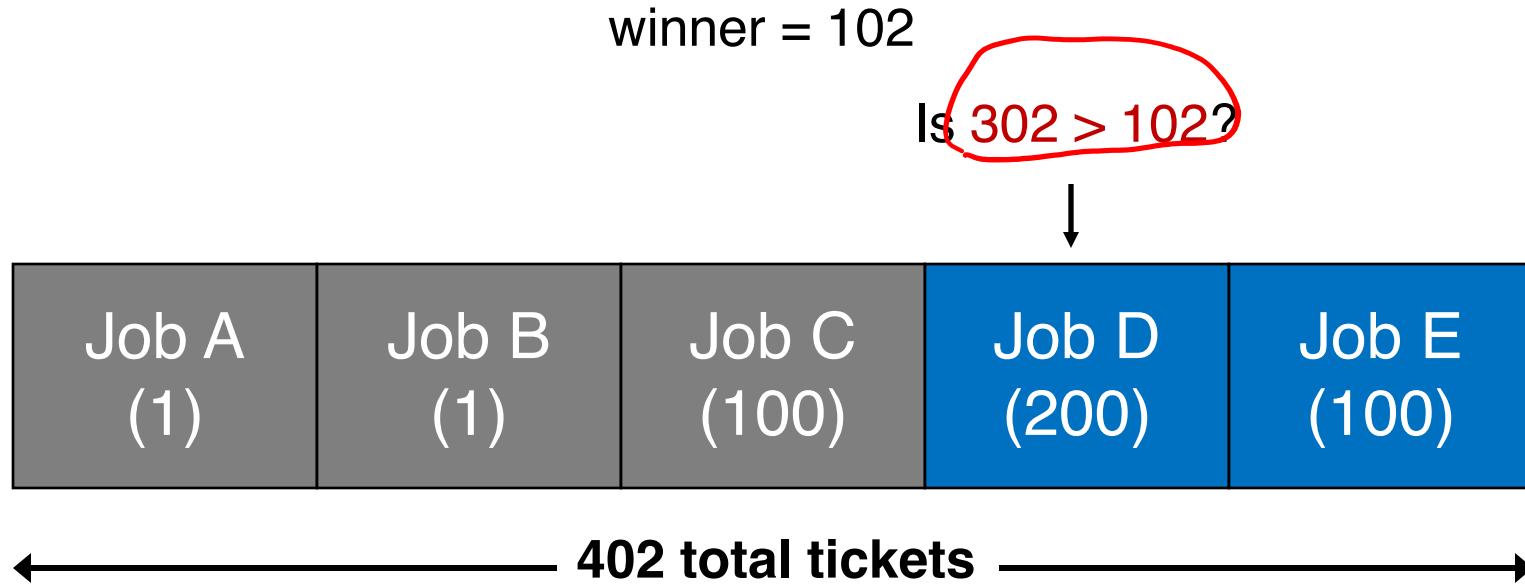
Is **102 > 102?**



Job A (1)	Job B (1)	Job C (100)	Job D (200)	Job E (100)
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← **402 total tickets** →

# Lottery Scheduling Example



# Lottery Scheduling Example

winner = 102

**302 > 102**



←———— **402 total tickets** —————→

**OS picks Job D to run!**