Computer Organization: Data Representation

DS 5110: Big Data Systems (Spring 2023) Lecture 2a

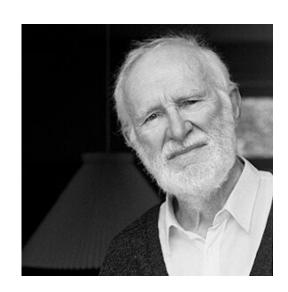
Yue Cheng



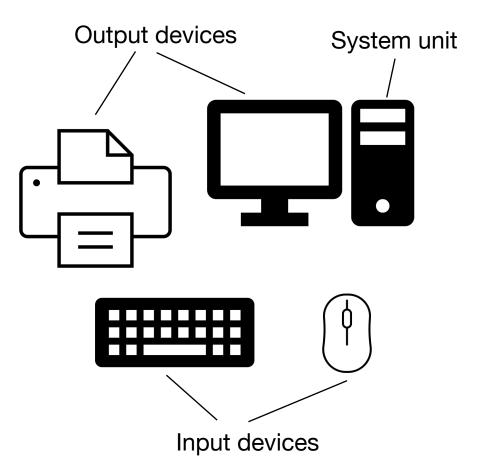
What is a computer?

A programmable electronic device that can store, retrieve, and process digital data

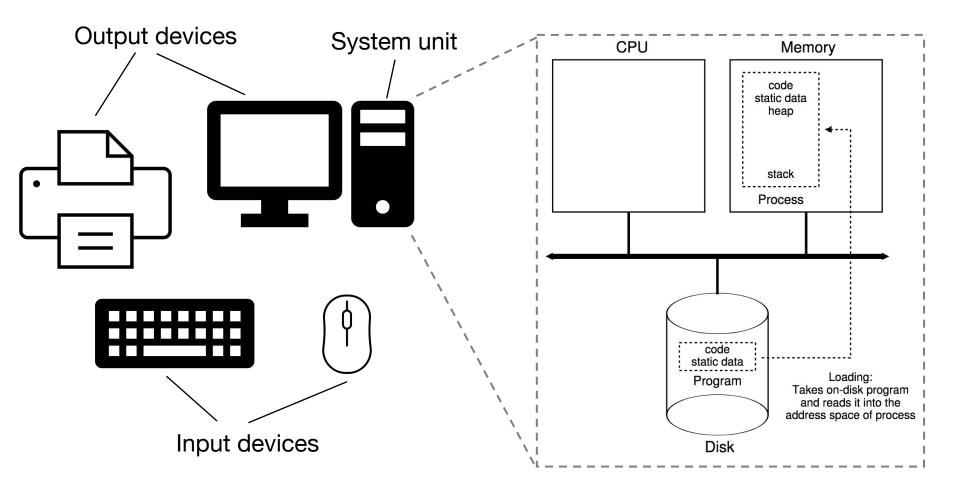
Computer science aka "Datalogy"



What is in a computer?



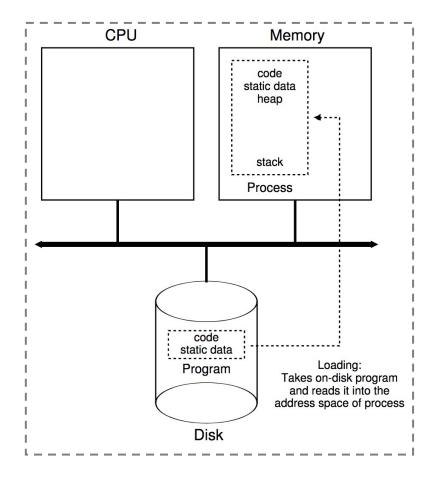
What is in a computer?



Key parts of computer hardware

CPU

 Hardware to execute instructions to manipulate data as specified by a program



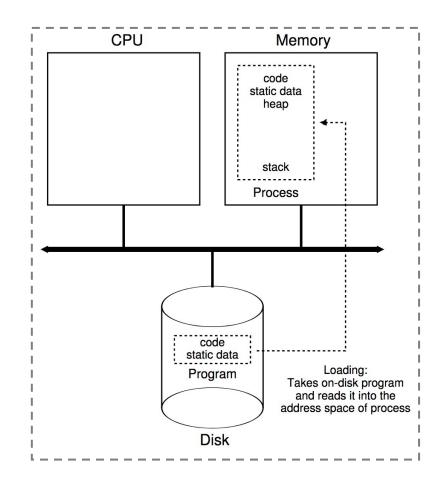
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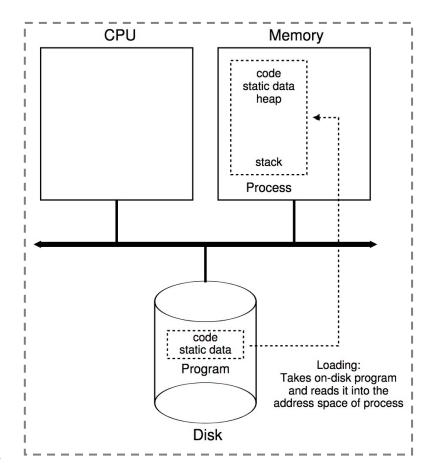
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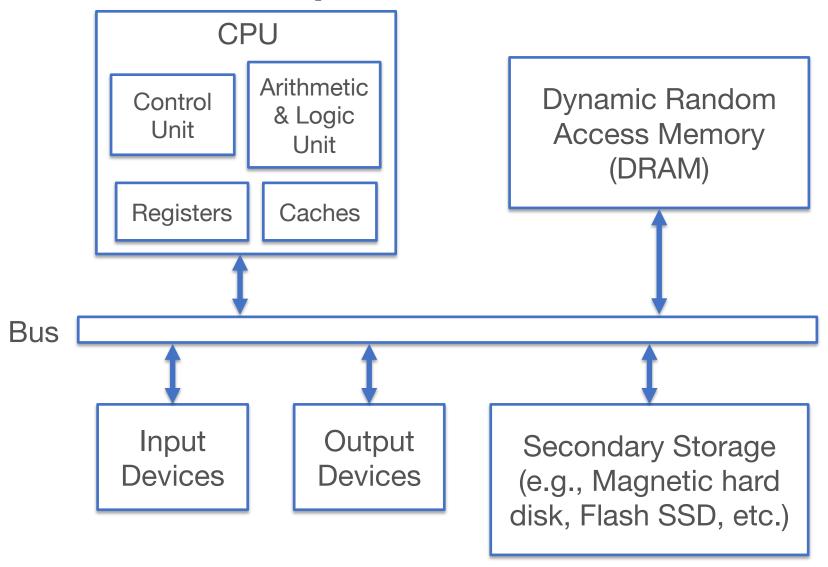
 Hardware to store data and programs that allow fast storage/retrieval (byte addressable)

Disk (second storage)

 Persistent, slower storage with higher capacity (block addressable)



How different parts interact



Instruction

- A command understood by hardware
- Finite vocabulary for a CPU: Instruction Set Architecture (ISA)
- Bridge between hardware and software

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Data

 Digital representation of information that is stored, processed, displayed, retrieved, or sent by a program

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Firmware

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Application software programs

- A (user-space) program or a collection of (user-space) programs to perform a certain task for human use
- Examples: Office, Chrome, Zoom

What is data?

Digital representation of data

- **Bits:** All digital data are sequences of 0s and 1s (binary)
 - Amenable to high-low/on-off electromagnetism

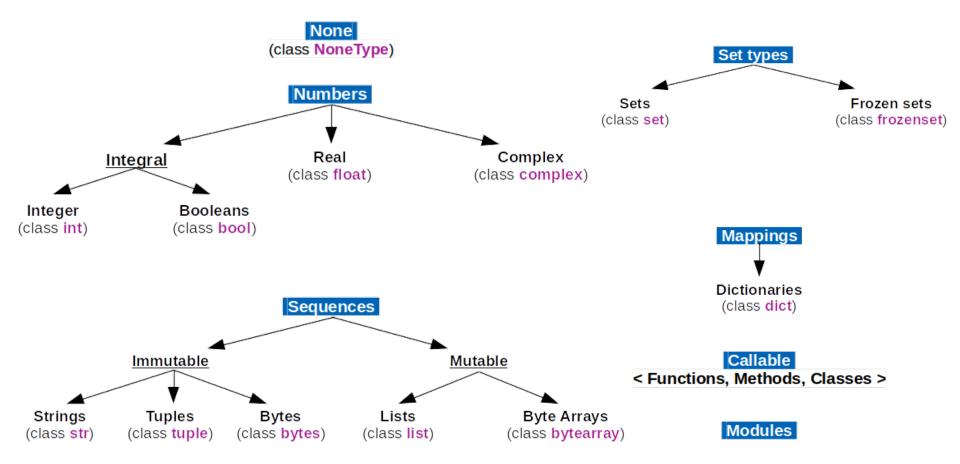
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 - Example data types: Boolean, byte, integer, floating point number (float), character, string
- Data structures: A second layer of abstraction to organize multiple instances of same or varied data types as a more complex object with specific properties
 - Examples: Array, dictionary (hash table), tree, graph

Data types in Python 3



Data types

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Integer:

- Examples: count of something # friends
- Typically 4B but many variants (short, unsigned, etc.)
 - Java int: -2^{31} to $(2^{31}-1)$
 - Cunsigned int: 0 to $(2^{32}-1)$
 - Python3 int: effectively no max limit

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- For k unique items, invert the exponent: log₂(k)
- #bits should be integer, so we do [log₂(k)]
- $[\log_2(97)]$: $97 \rightarrow 128 = 2^7$, so, 7 bits

Q: How to convert a decimal to a binary?

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```
Decimal
810
2610
16310
```

```
7 6 5 4 3 2 1 0 Position/Exponent of 2 128 64 32 16 8 4 2 1 Power of 2
```

Hexadecimal examples

- Hexadecimal representation is a common standin for binary representation; more succinct and readable
 - Base 16 instead of base 2 cuts display length by 4x
 - Digits are 0, 1, ..., 9, A (10₁₀), B, ..., F (15₁₀)
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16 10	1 00002	

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Hexadecimal examples

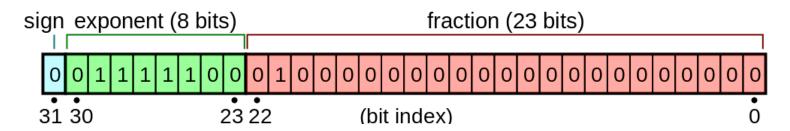
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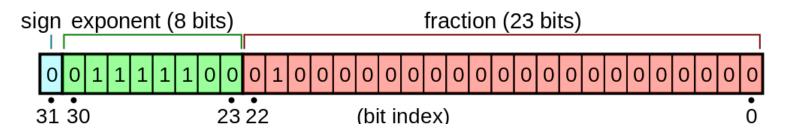
- Float
 - Examples: salary, model weights
 - IEEE-754 single-precision format is 4B long; double-precision format is 8B long
 - Java and C float is single; Python float is double

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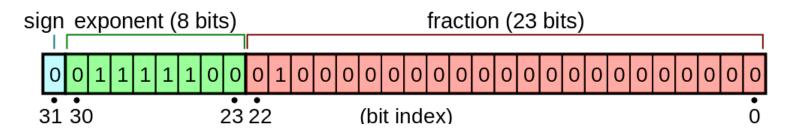


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$$(-1)^{sign} \times 2^{exponent-127} \times (1 + \sum_{i=1}^{23} b_{23-i} 2^{-i})$$
$$(-1)^0 \times 2^{124-127} \times (1 + 1 \cdot 2^{-2}) = (1/8) \times (1 + (1/4)) = 0.15625$$

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- In binary32, special encodings recognized:
 - Exponent 0xFF and fraction 0 is +/- "infinity"
 - Exponent 0xFF and fraction <> 0 is "NaN"
 - Max is 2^{127} x (2- 2^{-23}), i.e., ~3.4 x 10^{38}

More on float standards

- Double-precision (float64, 8B) and half-precision (float16, 2B)
 - Different #bits for exponent, fraction
- float16 is now common for deep learning parameters

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 - Examples: 'D' is 68, 'd' is 100, '!' is 33, '?' is 63
 - Unicode UTF-8 subsumes ASCII
 - 4B for ~1.1 million "code points" including many other language scripts, math symbols, emojis, etc.
 - 😊 🍁 : https://unicode.org/emoji/charts/full-emoji-list.html

Data structures

- Data structures: A second layer of abstraction to organize multiple instances of same or varied data types as a more complex object with specific properties
 - ML feature vectors: array of floats
 - Neural network weights: set of multi-dimensional arrays (matrices or tensors) of floats
 - Trees: binary trees, N-ary trees
 - Graphs: sets of vertices (integers) and sets of edges (pair of integers) that connect vertices
 - And a lot more...