# GooseMaterial/Metal/LinearStrain/Elastic

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### **Abstract**

Linear elasticity: a linear relation between the Cauchy stress  $\sigma$  and the linear strain  $\varepsilon$ 

The model is implemented in 3-D, hence it can directly be used for either 3-D or 2-D plane strain problems.

**Keywords:** linear elasticity

## 1 Constitutive model

The stress,  $\sigma$ , is set proportional to the strain,  $\varepsilon$ , through the following linear relation:

$$\sigma = \mathbb{C}_{e} : \varepsilon$$
 (1)

wherein  $\mathbb{C}_{\mathrm{e}}$  is the elastic stiffness, which reads:

$$\mathbb{C}_{e} = K\mathbf{I} \otimes \mathbf{I} + 2G(\mathbb{I}_{s} - \frac{1}{3}\mathbf{I} \otimes \mathbf{I})$$
(2)

$$= K\mathbf{I} \otimes \mathbf{I} + 2G \mathbb{I}_{d} \tag{3}$$

with K and G the bulk and shear modulus respectively. See Appendix A for nomenclature.

### A Nomenclature

· Dyadic tensor product

$$\mathbb{C} = A \otimes B \tag{4}$$

$$C_{ijkl} = A_{ij} B_{kl} \tag{5}$$

• Double tensor contraction

$$C = A : B \tag{6}$$

$$=A_{ij}\,B_{ji}\tag{7}$$

• Deviatoric projection tensor

$$\mathbb{I}_{\mathbf{d}} = \mathbb{I}_{\mathbf{s}} - \frac{1}{3} \mathbf{I} \otimes \mathbf{I} \tag{8}$$