## Description of R codes for Most Predictable Component of a Linear Stochastic Model

This Github site contains the codes for generating figures in the paper "The Most Predictable Component of a Linear Stochastic Model" by ?. Below is a brief description of each file.

**NDim.master.R** Generates figure 1: APT versus eigenvalue spacing  $\Delta$  of the APT-optimal for dimensions D=2,3,4,5, as well as the associated optimal projection vectors at small  $\Delta$ .

**NDim.timeseries.R** Generates figure 2: time series of eigenmodes and the APT-optimals, as well as the predictability  $P_{\tau}$  and autocorrelation functions.

**NDim. GenPascal. R** Generates figure 3: maximum APT as a function of  $\Delta$  and exponent p.

rank1.ERSST.R Generates figure 4, 5, 6: maximum APT for various stochastic models as a function of EOF truncation D, and the associated  $P_{\tau}$ 's. The three figures are obtained by choosing area.name = NASST, NPSST, PACICIF30S30N. Users should change dir.ersst to the directory containing ERSSTv5 data.

## **Auxiliary Codes**

gev. R function solves generalized eigenvalue problem  $Aq = \lambda Bq$  with real matrices A and B.

**gev.complex.R** function solves generalized eigenvalue problem  $\mathbf{Aq} = \lambda \mathbf{Bq}$  with complex matrices  $\mathbf{A}$  and  $\mathbf{B}$ .

pdf.eps.R function for printing figures in PDF format

lyap. R function for solving the Lyapunov equation

index.climate.v2.R function for identifying a domain in gridded data sets. Points inside the domain are set to TRUE, points outside the domain to FALSE.

plot\_eof.R function for plotting the spatial structure and time series of an EOF.

eof.latlon.R function for computing EOFs given gridded data.

plot\_latlon\_contour function for generating shaded plots with contours

plot\_latlon\_v4 function for generating shaded plots

## References

DelSole, T. and M. K. Tippett, 2023: The most predictable component of a linear stochastic model. *Proceedings of the Royal Society of London. Series A - Mathematical and Physical Sciences*, **submitted**.