

# (Advanced) deep learning

Convolutional neural networks - 2

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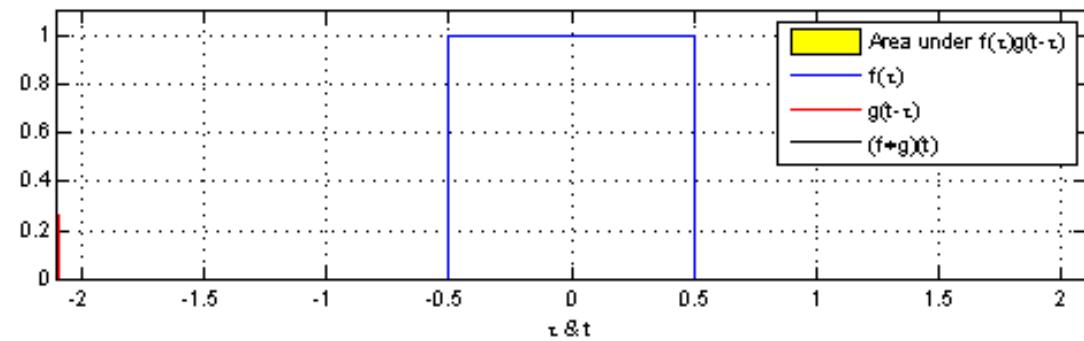
# Convolution 1D

$$f, k: \mathbb{R} \rightarrow \mathbb{R}$$

$$g(x) = (f * k)(x) = \int_{-\infty}^{\infty} f(\alpha) k(x - \alpha) d\alpha$$

$$f, k \in \mathbb{R}^M$$

$$g(i) = (f * k)(i) = \sum_{m=1}^M f(m)k(i - m)$$



By Convolution\_of\_box\_signal\_with\_itself.gif: Brian Ambergderivative work: Tinos (talk) - Convolution\_of\_box\_signal\_with\_itself.gif, CC BY-SA 3.0, <https://commons.wikimedia.org/w/index.php?curid=11003835>

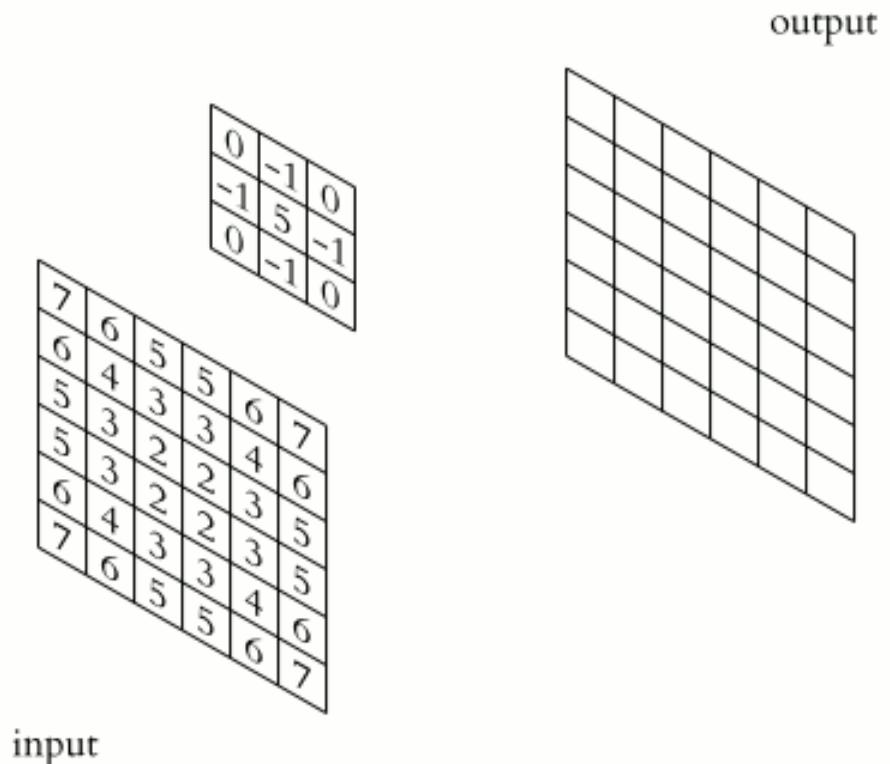
## Convolution 2D

$$f, k: \mathbb{R}^2 \rightarrow \mathbb{R}^2$$

$$(f * k)(x, y) = \iint_{-\infty}^{\infty} f(\alpha, \beta) k(x - \alpha, y - \beta) d\alpha d\beta$$

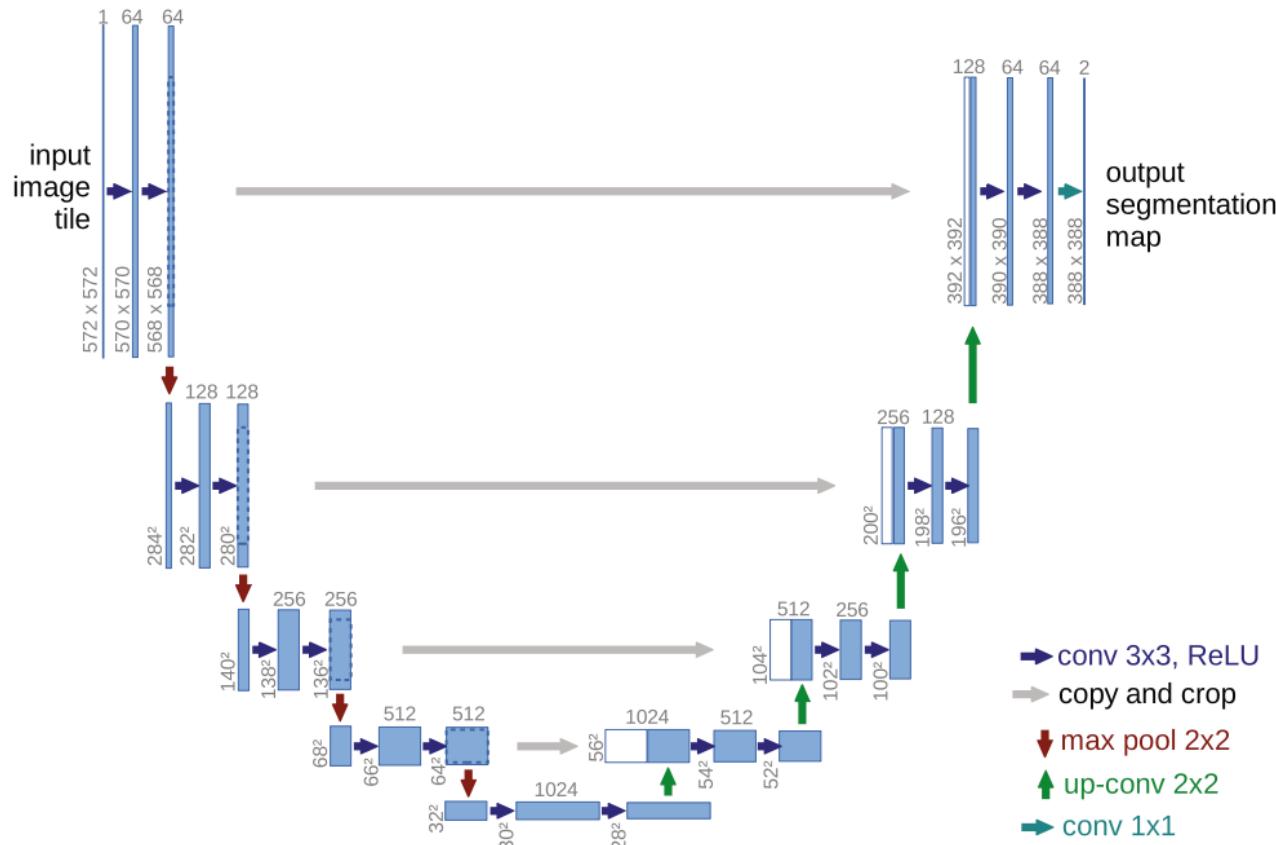
$$f, k \in \mathbb{R}^{M \times N}$$

$$(f * k)(i, j) = \sum_{m=1}^M \sum_{n=1}^N f(m, n) k(i - m, j - n)$$

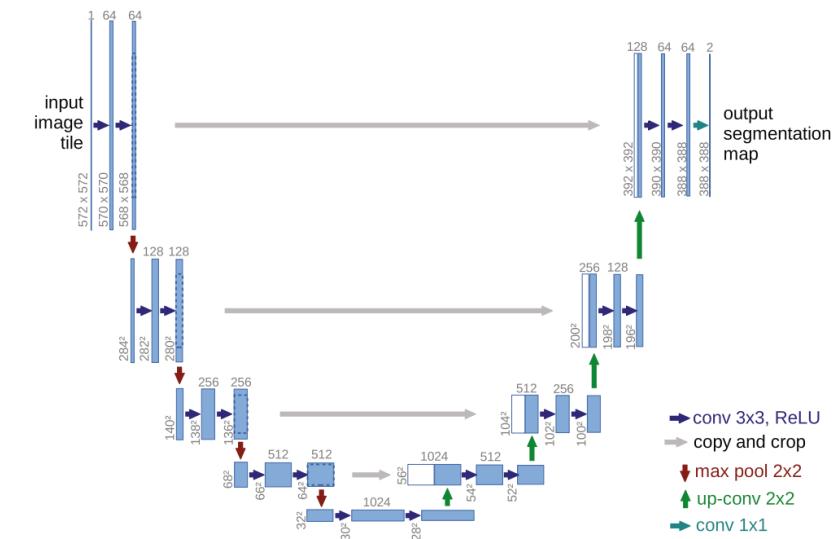
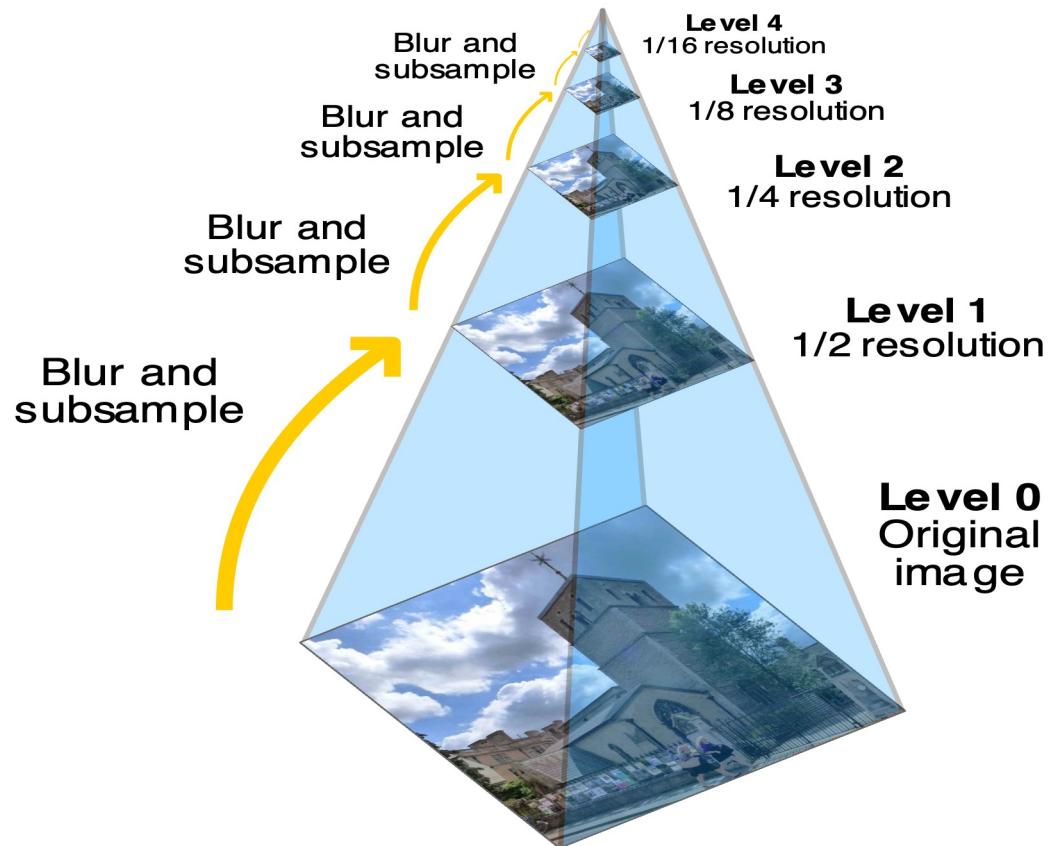


By Michael Plotke - Own work, CC BY-SA 3.0,  
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# Unet: Convolutional network – encoding and decoding



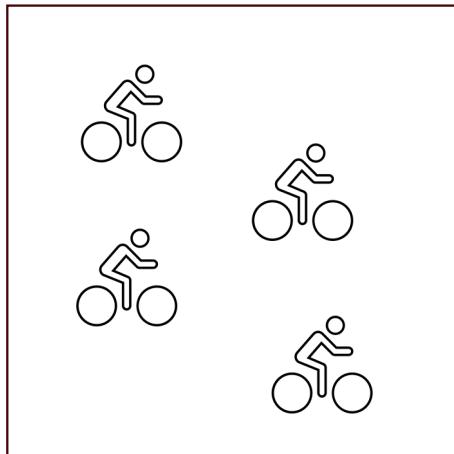
# Image pyramid



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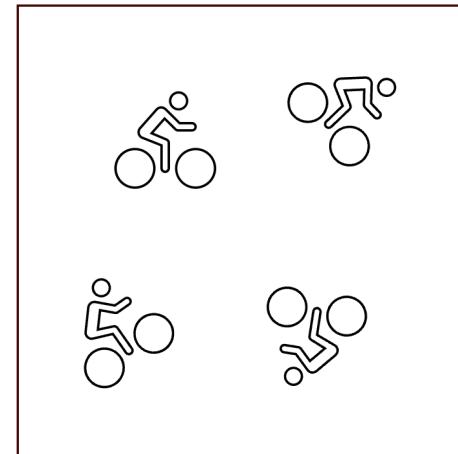
# Invariances

Translation



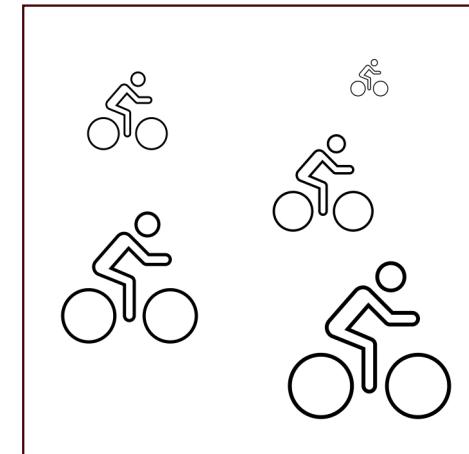
Convolution/Attention

Translation + Rotation



Augmentation/Geometric Deep Learning

Translation + Scaling



Augmentation/UNet

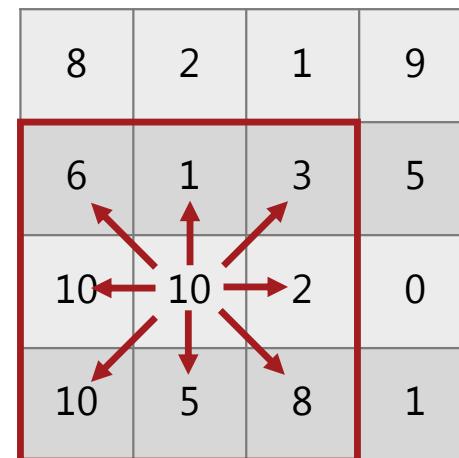
## Max Pooling

$$f(i, j) = \max_{i=[0, M-1], j=[0, N-1]} f(i + m, j + n)$$

8	2	1	9
6	1	3	5
10	10	2	0
10	5	8	1



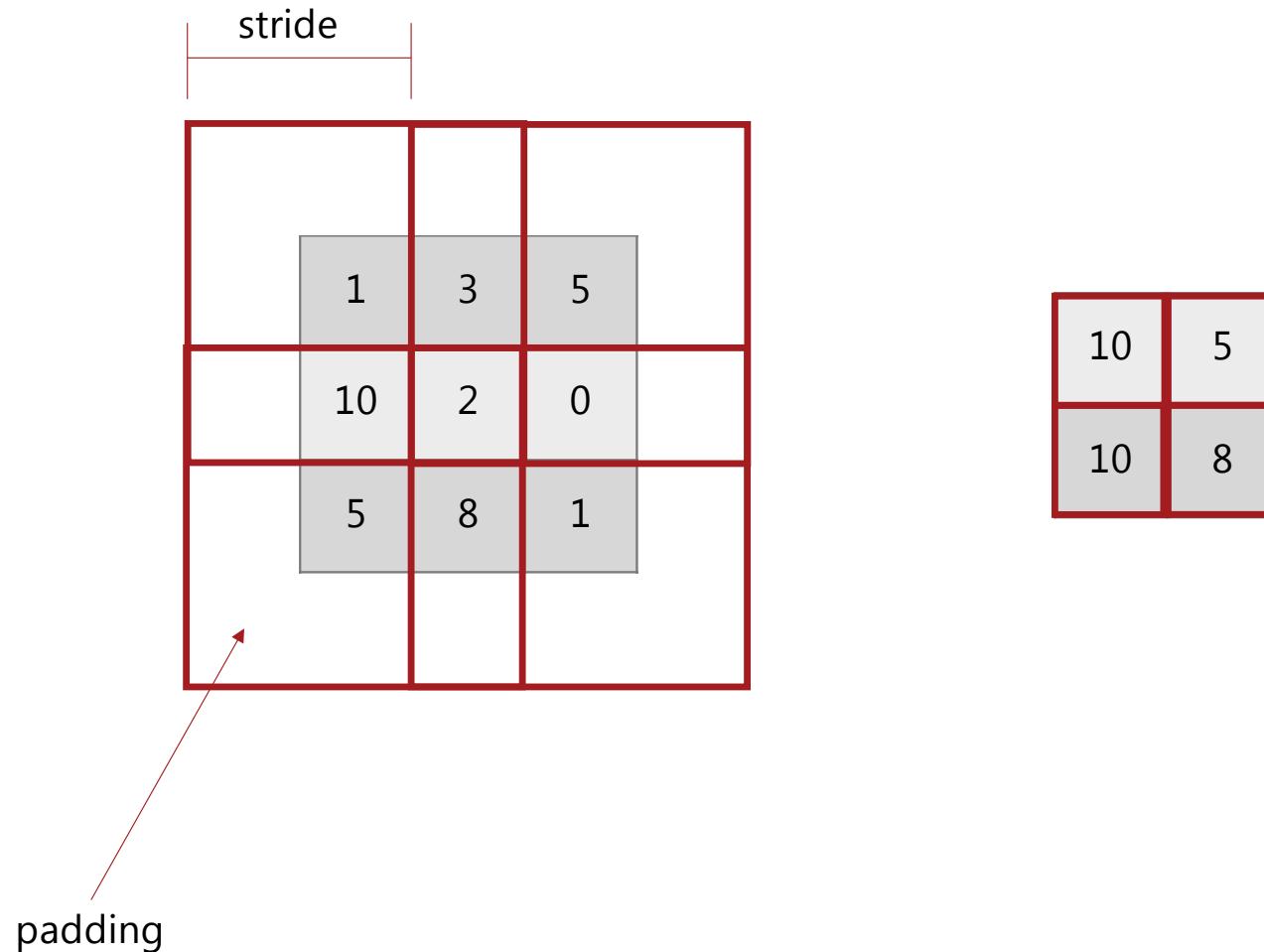
8	3	9
10	10	5
10	10	8



8	2	1	9
6	1	3	5
10	10	2	0
10	5	8	1

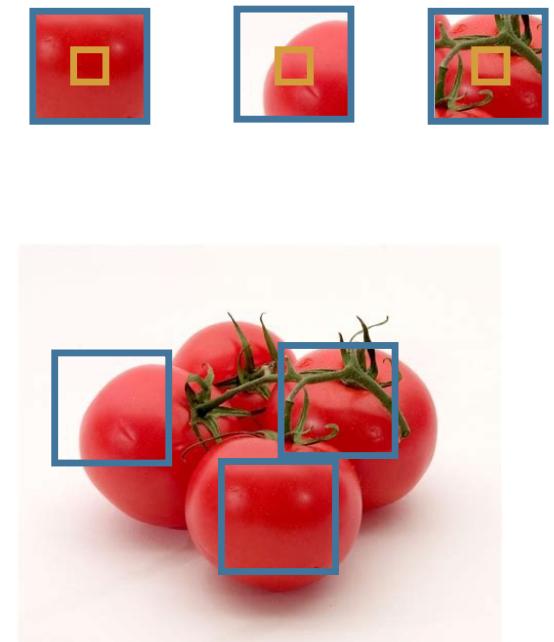
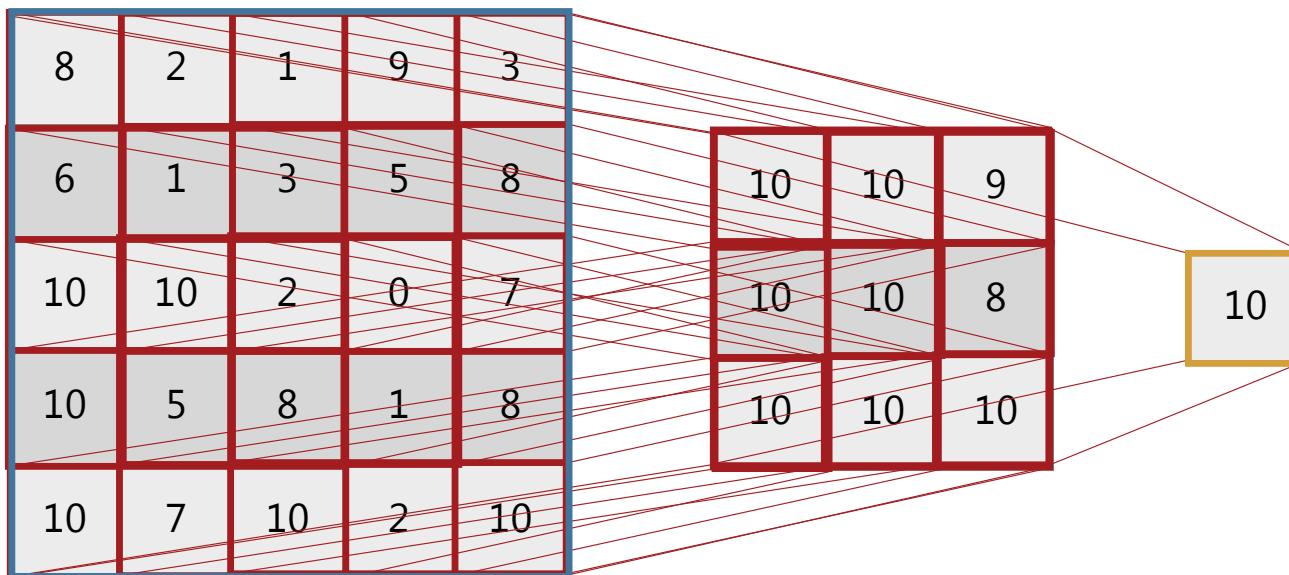
8	3	9

# Padding & Stride



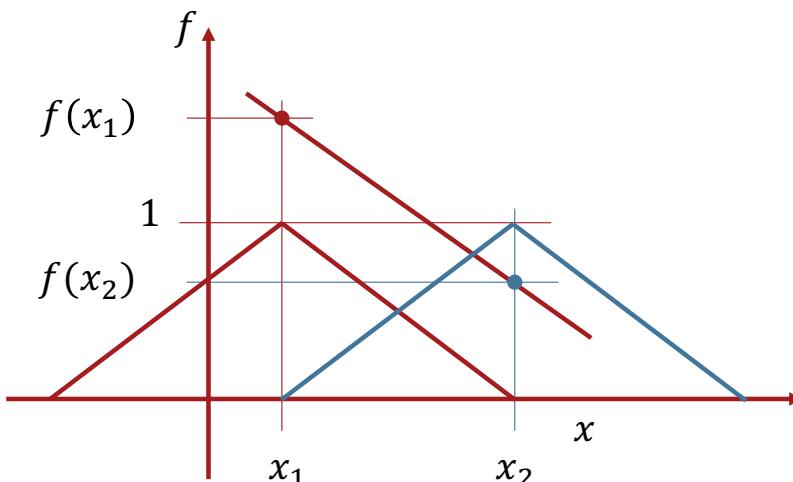
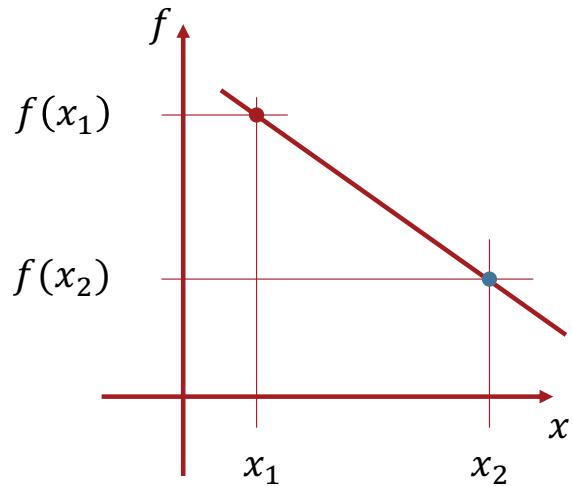
# Receptive field

3x3 max pooling:



<https://www.feedipedia.org/node/7791>

# Upsampling / upconvolution



10	7.5	5
10	8.25	6.5
10	9	8

$$x \in [x_1, x_2]$$

$$f(x) = \frac{x_2 - x}{x_2 - x_1} f(x_1) + \frac{x - x_1}{x_2 - x_1} f(x_2)$$

$$f(x) = a_1(x)f(x_1) + a_2(x)f(x_2)$$

Interpolation:  $a_1(x) + a_2(x) = 1$

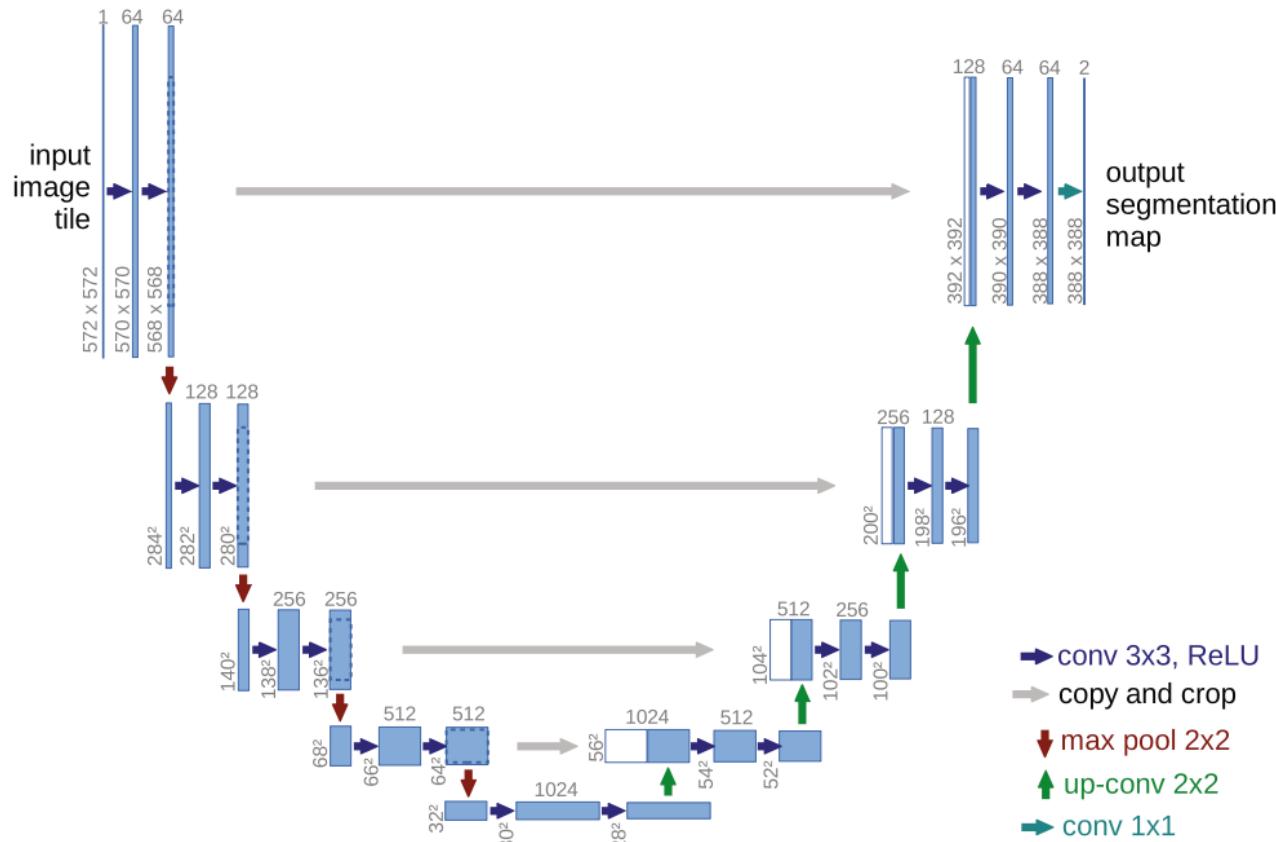
$$\begin{aligned}\tilde{f}(x) &= (f * k)(x) \\ k(x) &= [a_2, a_1](x)\end{aligned}$$

$$x \in [x_1, x_2], y \in [y_1, y_2]$$

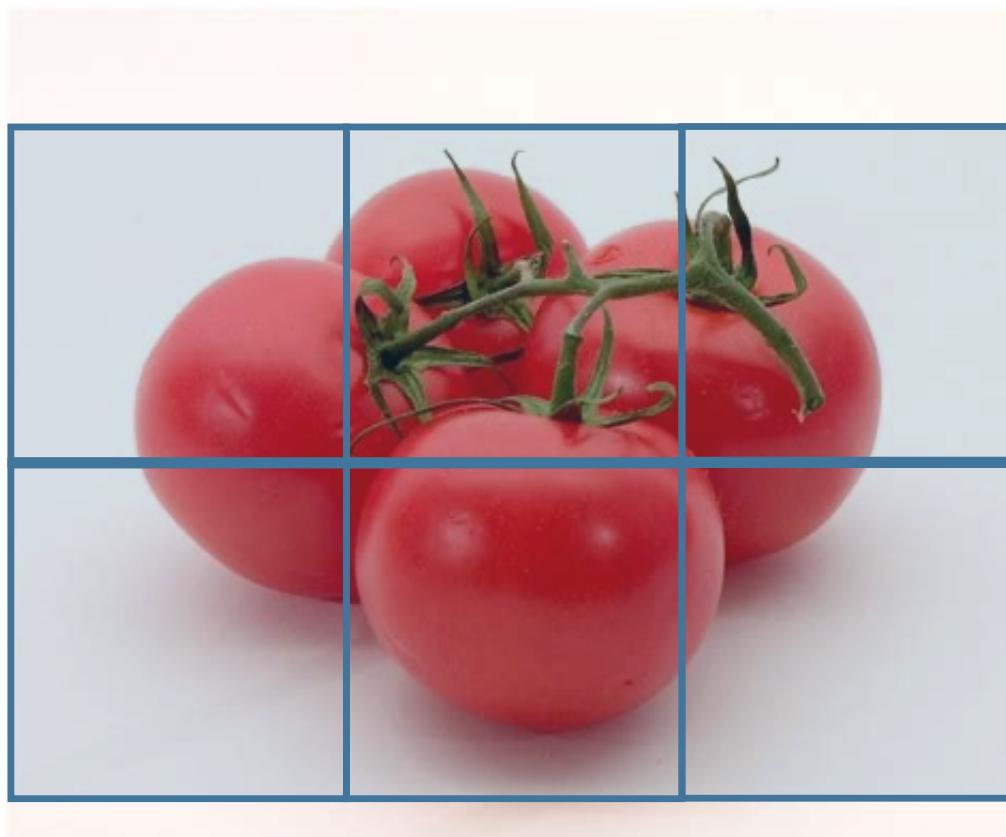
$$f(x, y) = \frac{y_2 - y}{y_2 - y_1} f(x, y_1) + \frac{y_1 - y}{y_2 - y_1} f(x, y_2)$$

$$\tilde{f}(x, y) = (f * k)(x, y)$$

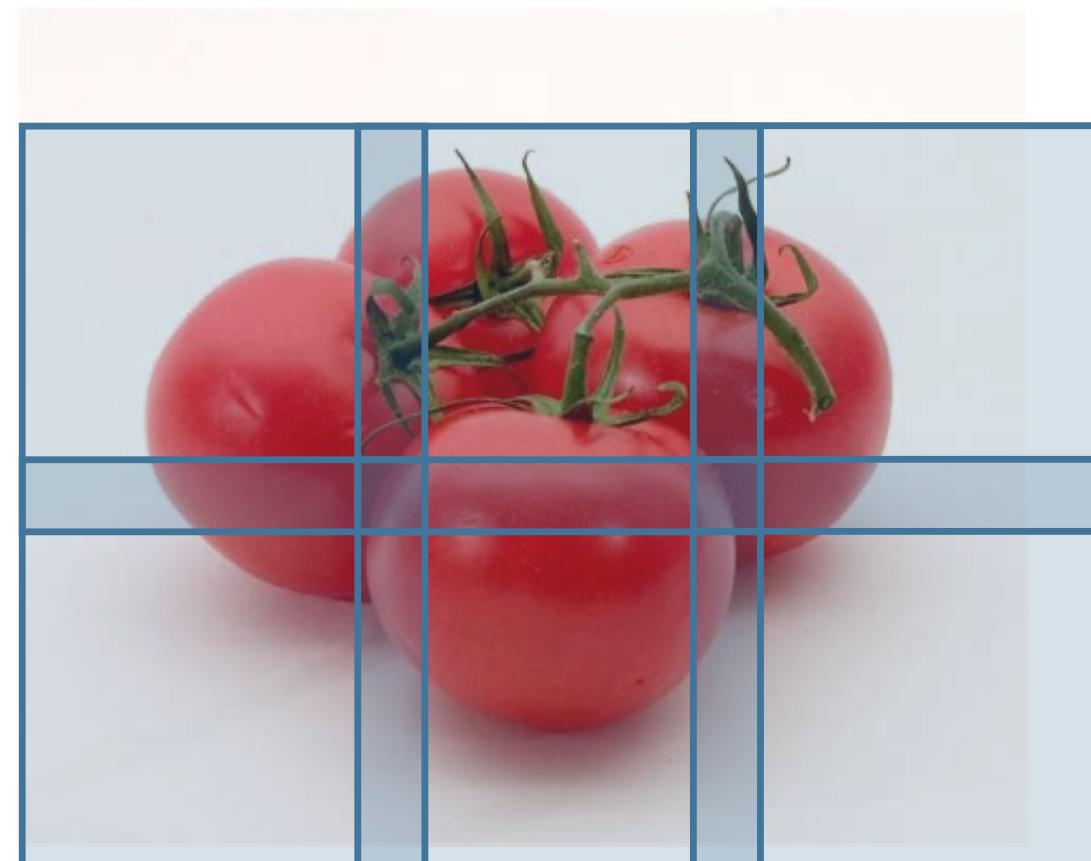
# Unet: Convolutional network – encoding and decoding



## Patch processing

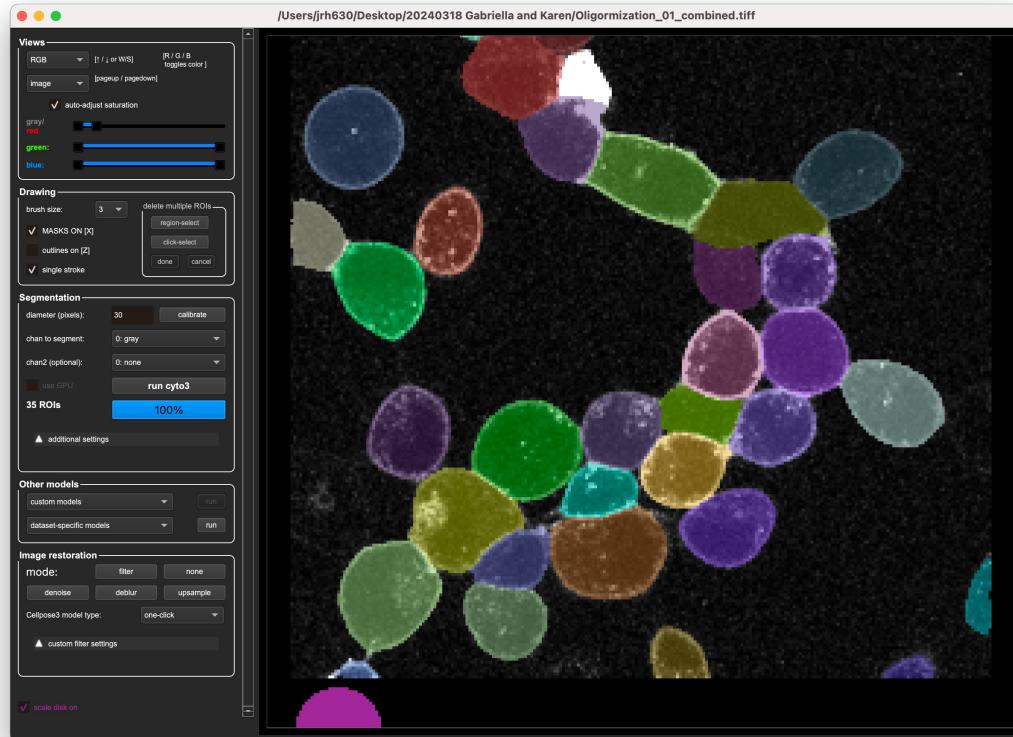


<https://www.feedipedia.org/node/7791>



# You never have enough training data

Image augmentation:



Color



Background



Translation



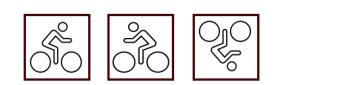
Rotation



Scaling



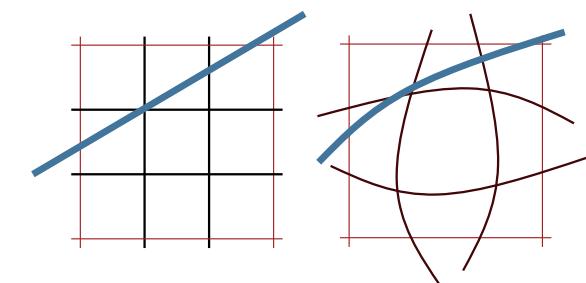
Flipping



Skewing



Non-linear deformations



## Convergence issues: Normalization?

Ideas:

1. Normalize input – both at training and prediction!

$$x \rightarrow \frac{x - \mu}{\sigma} \in [0,1]$$

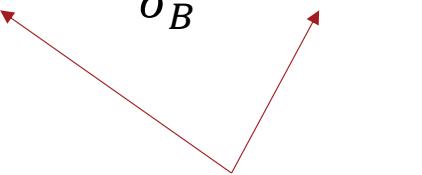
2. Classification with one-hot encoding

$$y \in \{0,1\}^N$$

3. Normalize inner layers – both training and prediction:

$$x \rightarrow \alpha \odot \frac{x - \mu_B}{\sigma_B} + \beta$$

Trainable parameters



# Corrective segmentation: Root painter

[https://github.com/Abe404/root painter](https://github.com/Abe404/root_painter)



# New Phytologist

Methods |  Open Access |  

## RootPAINTER: deep learning segmentation of biological images with corrective annotation

Abraham George Smith , Eusun Han, Jens Petersen, Niels Alvin Faircloth Olsen, Christian Giese, Miriam Athmann, Dorte Bodin Dresbøll, Kristian Thorup-Kristensen

First published: 18 July 2022 | <https://doi.org/10.1111/nph.18387> | Citations: 15

 SECTIONS



PDF



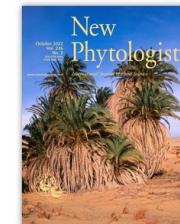
TOOLS



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### Summary

- Convolutional neural networks (CNNs) are a powerful tool for plant image analysis, but challenges remain in making them more accessible to researchers without a



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Pages 774-791



Figures



References



Related



Information

### Recommended

[Deep RNA sequencing improved the structural annotation of the \*Tuber melanosporum\* transcriptome](#)

E. Tisserant, C. Da Silva, A. Kohler, E. Morin, P. Wincker, F. Martin

[New Phytologist](#)

[Automated and accurate segmentation of leaf venation networks via deep](#)

# Where to be inspired: <https://paperswithcode.com/>

The screenshot shows the PapersWithCode website interface. The top navigation bar includes a search bar, a magnifying glass icon, and links for 'Browse State-of-the-Art', 'Datasets', 'Methods', and 'More'. Below the navigation, a large section for 'Semantic Segmentation' is displayed, showing 5207 papers with code, 125 benchmarks, and 311 datasets. A sub-section for 'Image Classification' shows 3788 papers with code, 142 benchmarks, and 238 datasets. A sub-section for 'Object Detection' shows 3714 papers with code, 91 benchmarks, and 262 datasets. The 'Content' sidebar on the right lists categories: Introduction, Benchmarks, Datasets, Subtasks, Libraries, Papers (with 'Most implemented', 'Social', 'Latest', and 'to code' sub-options), and a large image of a semantic segmentation result.

**Semantic Segmentation**  
5207 papers with code • 125 benchmarks • 311 datasets

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3714 papers with code • 91 benchmarks • 262 datasets

**Content**

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- Benchmarks
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