Questions: Solving exponential equations

Zoë Gemmell, Isabella Lewis, Akshat Srivastava

Summary

A selection of questions for the study guide on solving equations involving indices.

Before attempting these questions, it is highly recommended that you read Guide: Solving exponential equations.

Solve each of the exponential equations below for the variable in the equation. If an equation has more than one variable, solve for the variable stated.

1.
$$\sqrt[4]{m-4} = 5$$

2.
$$x^4 = 2^8$$

3.
$$11^x = 121^{(x-1)}$$

4.
$$y^{0.5} = 23$$

$$5. \quad 8^{2-x} = 2^{4+3x}$$

6.
$$2^{3x} = 10$$

7.
$$5^{3-a} = 625$$

8.
$$16^{2x} = 4^{x-1}$$

9.
$$7^{2-x} = 4^{2x+3}$$

10.
$$16 = 8^{3-7x}$$

11.
$$e^{3-8p} - 9 = 0$$

12.
$$e^{4-3q} + 8 = 12$$

13.
$$\sqrt[3]{2^{4l}-4}=5$$

$$14. \qquad \sqrt[3]{e^{2h} - 13} = 81^{\frac{1}{4}}$$

15.
$$\frac{5xa^{-7}b^9}{9a^2b^{-10}} = \frac{25b^{19}}{3a^9}, \text{ solve for } x.$$

16.
$$4^x \cdot 2^x = 64$$

17.
$$\frac{5^{x+1} \cdot 6^{x+1}}{3^{x+1}} = 100$$

18.
$$\frac{\left[\left(\frac{1}{2}\right)^x \cdot \left(\frac{-1}{4}\right)^x\right]}{\left(\frac{2}{3}\right)^x} = -\frac{27}{4096}$$

19.
$$3^{b+1} = 7^b$$

$$20. \quad 5^{x+1} + 5^x = 12$$

21.
$$2^{3z-1} = 10^z$$

22.
$$2^{2v} - 2^{v+3} - 2^4 = 0$$

After attempting the questions above, please click this link to find the answers.

Version history and licensing

v1.0: initial version created 08/23 by Zoë Gemmell, Isabella Lewis, Akshat Srivastava as part of a University of St Andrews STEP project.

■ v1.1: edited 05/24 by tdhc.

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