Questions: Rationalizing the denominator

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Summary

A selection of questions for the study guide on rationalizing the denominator.

Before attempting these questions, it is highly recommended that you read Guide: Rationalizing the denominator.

Q1

Rationalize the denominator for each of the following expressions. Provide your answers in their simplest form and with a positive denominator.

- 1.1. $\frac{5}{\sqrt{3}}$
- $1.2. \qquad \frac{7}{2\sqrt{5}}$
- 1.3. $\frac{11}{4\sqrt{7}}$
- 1.4. $\frac{8}{5\sqrt{6}}$
- $1.5. \qquad \frac{3\sqrt{2}}{\sqrt{5}}$
- 1.6. $\frac{9}{\sqrt{10}}$
- 1.7. $\frac{\sqrt{7}}{\sqrt{3}}$
- 1.8. $\frac{\sqrt{2}}{\sqrt{6}}$
- 1.9. $\frac{12}{\sqrt{11}}$
- 1.10. $\frac{\sqrt{8}}{\sqrt{2}}$
- 1.11. $\frac{15}{3\sqrt{7}}$

- $1.12. \qquad \frac{6\sqrt{3}}{\sqrt{10}}$
- $1.13. \qquad \frac{\sqrt{18}}{\sqrt{9}}$
- $1.14. \qquad \frac{2\sqrt{5}}{\sqrt{12}}$
- 1.15. $\frac{4}{\sqrt{2}}$
- 1.16. $\frac{10}{5\sqrt{13}}$

Q2

Rationalize the denominator for each of the following expressions. Provide your answers in their simplest form and with a positive denominator.

- 2.1. $\frac{5}{2+\sqrt{3}}$
- 2.2. $\frac{7}{4-\sqrt{2}}$
- 2.3. $\frac{3}{\sqrt{5}+1}$
- 2.4. $\frac{\sqrt{7}}{\sqrt{3}-1}$
- 2.5. $\frac{2+\sqrt{5}}{1-\sqrt{2}}$
- 2.6. $\frac{3\sqrt{2}+5}{4+\sqrt{6}}$
- 2.7. $\frac{8}{3-\sqrt{7}}$
- 2.8. $\frac{6}{2+\sqrt{5}}$
- $2.9. \qquad \frac{\sqrt{10}}{\sqrt{2}+3}$
- $2.10. \qquad \frac{2\sqrt{3} + 5}{\sqrt{7} 1}$
- $2.11. \quad \frac{\sqrt{6} \sqrt{2}}{2 + \sqrt{5}}$

$$2.12. \qquad \frac{4 + \sqrt{3}}{5 - \sqrt{7}}$$

2.13.
$$\frac{2}{4-\sqrt{11}}$$

2.14.
$$\frac{\sqrt{8} + \sqrt{3}}{\sqrt{7} - 2}$$

Q3

3.1. The denominator of the expression $\frac{\sqrt{11}}{2\sqrt{3}+\sqrt{5}}$ is not of the form $b+c\sqrt{d}$, where b and c are integers and d is an integer that is not a perfect square but you can still rationalize the denominator.

Prove that

$$\frac{\sqrt{11}}{2\sqrt{3}+\sqrt{5}} = \frac{2\sqrt{33}-\sqrt{55}}{7}$$

3.2. Rationalize the denominator of this expression: $\frac{5-\sqrt{2}}{\sqrt{10}-\sqrt{3}}$

Provide your answer in its simplest form and with a positive denominator.

After attempting the questions above, please click this link to find the answers.

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