

Factsheet: Trigonometric identities (degrees)

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Summary

A list of trigonometric identities with angles measured in degrees.

The main study guide for this factsheet is [Guide: Trigonometric identities \(degrees\)](#). If you would like to know more about these, please read the guide.

This factsheet measures angles in degrees. For the associated factsheet measuring angles in radians, please go to [Factsheet: Trigonometric identities \(radians\)](#).

Trigonometric identities

Periodicity and parity

For all angles θ and for all whole numbers $k \in \mathbb{Z}$:

$$\cos(-\theta) = \cos(\theta)$$

$$\sin(-\theta) = -\sin(\theta)$$

$$\tan(-\theta) = -\tan(\theta)$$

$$\cos(\theta + 360k) = \cos(\theta)$$

$$\sin(\theta + 360k) = \sin(\theta)$$

$$\tan(\theta + 180k) = \tan(\theta)$$

Pythagorean formulas

For all angles θ

$$\cos^2(\theta) + \sin^2(\theta) = 1$$

$$1 + \tan^2(\theta) = \sec^2(\theta)$$

$$\cot^2(\theta) + 1 = \csc^2(\theta)$$

Sum and difference formulas

For all angles α, β :

$$\cos(\alpha + \beta) = \cos(\alpha) \cos(\beta) - \sin(\alpha) \sin(\beta)$$

$$\cos(\alpha - \beta) = \cos(\alpha) \cos(\beta) + \sin(\alpha) \sin(\beta)$$

$$\sin(\alpha + \beta) = \sin(\alpha) \cos(\beta) + \cos(\alpha) \sin(\beta)$$

$$\sin(\alpha - \beta) = \sin(\alpha) \cos(\beta) - \cos(\alpha) \sin(\beta)$$

$$\tan(\alpha + \beta) = \frac{\tan(\alpha) + \tan(\beta)}{1 - \tan(\alpha) \tan(\beta)}$$

$$\tan(\alpha - \beta) = \frac{\tan(\alpha) - \tan(\beta)}{1 + \tan(\alpha) \tan(\beta)}$$

Double angle formulas

For all angles θ :

$$\cos(2\theta) = \cos^2(\theta) - \sin^2(\theta)$$

$$\sin(2\theta) = 2 \sin(\theta) \cos(\theta)$$

$$\tan(2\theta) = \frac{2 \tan(\theta)}{1 - \tan^2(\theta)}$$

Shift formulas

For all angles θ :

$$\cos(\theta + 90) = -\sin(\theta)$$

$$\cos(\theta - 90) = \sin(\theta)$$

$$\sin(\theta + 90) = \cos(\theta)$$

$$\sin(\theta - 90) = -\cos(\theta)$$

$$\cos(\theta \pm 180) = -\cos(\theta)$$

$$\sin(\theta \pm 180) = -\sin(\theta)$$

$$\sin(180 - \theta) = \sin(\theta)$$

$$\cos(180 - \theta) = -\cos(\theta)$$

Sine and cosine rules

For a triangle with corners A, B, C , angles α, β, γ respectively at those corners, and sides a, b, c opposite their respective corners, the **sine rule** is

$$\frac{\sin(\alpha)}{a} = \frac{\sin(\beta)}{b} = \frac{\sin(\gamma)}{c}$$

and the **cosine rule** is

$$a^2 = b^2 + c^2 - 2bc \cos(\alpha).$$

Common values of trigonometric functions

Angle θ	0	30	45	60	90	120	135	150	180
$\sin(\theta)$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0
$\cos(\theta)$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{3}}{2}$	-1
$\tan(\theta)$	0	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	un-def.	$-\sqrt{3}$	-1	$-\frac{1}{\sqrt{3}}$	0

Version history

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