Questions: Introduction to integration

Donald Campbell

Summary

A selection of questions for the study guide on introduction to integration.

Before attempting these questions, it is highly recommended that you read Guide: Introduction to integration.

Q1

Using the power rule and laws of indices (as appropriate), find the following indefinite integrals.

1.1.
$$\int x^4 \, \mathrm{d}x$$

1.2.
$$\int 2x \, \mathrm{d}x$$

1.3.
$$\int 7x^5 \, \mathrm{d}x$$

1.4.
$$\int -5 \, \mathrm{d}t$$

1.5.
$$\int \frac{3}{y^3} \, \mathrm{d}y$$

$$1.6. \qquad \int 6x^{-4} \, \mathrm{d}x$$

$$1.7. \qquad \int -\frac{2}{x^5} \, \mathrm{d}x$$

$$1.8. \qquad \int \frac{8}{3x^6} \, \mathrm{d}x$$

$$1.9. \qquad \int -\frac{7}{2z^7} \, \mathrm{d}z$$

1.10.
$$\int x^{1/3} \, \mathrm{d}x$$

1.11.
$$\int 3t^{-2/3} dt$$

1.12.
$$\int \frac{4x^{1/4}}{3} \, \mathrm{d}x$$

1.13.
$$\int \frac{2}{5x^{1/3}} \, \mathrm{d}x$$

1.14.
$$\int \frac{5}{6y^{-4/3}} \, \mathrm{d}y$$

Q2

Find the following integrals.

$$2.1. \qquad \int e^{2x} \, \mathrm{d}x$$

$$2.2. \qquad \int -3e^{-3x} \, \mathrm{d}x$$

$$2.3. \qquad \int 2e^{11x} \, \mathrm{d}x$$

2.4.
$$\int \frac{4}{x} \, \mathrm{d}x$$

$$2.5. \qquad \int -\frac{5}{3x} \, \mathrm{d}x$$

2.6.
$$\int \cos(x) \, \mathrm{d}x$$

2.7.
$$\int \sin(2x) \, \mathrm{d}x$$

2.8.
$$\int \frac{5}{6} \cos(x) \, \mathrm{d}x$$

2.9.
$$\int \cos(3x) \, \mathrm{d}x$$

2.10.
$$\int \sin\left(\frac{x}{3}\right) \, \mathrm{d}x$$

Q3

Evaluate the following definite integrals with respect to $\boldsymbol{x}.$

$$3.1. \qquad \int_1^4 2 \, \mathrm{d}x$$

$$3.2. \qquad \int_{-2}^{2} 3x \, \mathrm{d}x$$

3.3.
$$\int_{2}^{4} 2x^{3} dx$$

3.4.
$$\int_{1}^{27} \frac{4}{\sqrt[3]{x}} \, \mathrm{d}x$$

3.5.
$$\int_0^{\ln(3)} 4e^x \, dx$$

3.6.
$$\int_0^5 e^{-3x} \, \mathrm{d}x$$

3.7.
$$\int_{1}^{2} -4e^{4x} \, \mathrm{d}x$$

$$3.8. \qquad \int_1^2 \frac{2}{x} \, \mathrm{d}x$$

3.9.
$$\int_{1}^{e^3} -\frac{4}{x} \, \mathrm{d}x$$

3.10.
$$\int_{e^3}^{e^9} \frac{9}{5x} \, \mathrm{d}x$$

$$3.11. \qquad \int_0^{\pi/2} \sin(x) \, \mathrm{d}x$$

3.12.
$$\int_0^{\pi} \cos(x) \, \mathrm{d}x$$

$$3.13. \qquad \int_0^{\pi/4} \sin(2x) \, \mathrm{d}x$$

3.14.
$$\int_0^{\pi/6} \cos(2x) \, \mathrm{d}x$$

3.15.
$$\int_{-\pi/4}^{0} \sin(3x) \, \mathrm{d}x$$

After attempting the questions above, please click this link to find the answers.

Version history and licensing

v1.0: initial version created 05/25 by Donald Campbell as part of a University of St Andrews VIP project.

This work is licensed under CC BY-NC-SA 4.0.