Answers: Introduction to integration

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Summary

Answers to questions relating to the guide on introduction to integration.

These are the answers to Questions: Introduction to integration.

Please attempt the questions before reading these answers!

Q1

1.1.
$$\int x^4 \, \mathrm{d}x = \frac{1}{5}x^5 + C.$$

1.2.
$$\int 2x \, \mathrm{d}x = x^2 + C.$$

1.3.
$$\int 7x^5 \, \mathrm{d}x = \frac{7}{6}x^6 + C.$$

1.5.
$$\int -5 \, \mathrm{d}t = -5t + C.$$

Q2

2.1.
$$\int \frac{3}{y^3} \, \mathrm{d}y = -\frac{3}{2}y^{-2} + C.$$

2.2.
$$\int 6x^{-4} \, \mathrm{d}x = -2x^{-3} + C.$$

2.3.
$$\int -\frac{2}{x^5} \, \mathrm{d}x = \frac{1}{2}x^{-4} + C.$$

2.4.
$$\int \frac{8}{3x^6} \, \mathrm{d}x = -\frac{8}{15}x^{-5} + C.$$

2.5.
$$\int -\frac{7}{2z^7} \, \mathrm{d}z = \frac{7}{12}z^{-6} + C.$$

Q3

3.1.
$$\int x^{1/3} \, \mathrm{d}x = \frac{3}{4} x^{4/3} + C.$$

3.2.
$$\int 3t^{-2/3} \, \mathrm{d}t = 9t^{1/3} + C.$$

3.3.
$$\int \frac{4x^{1/4}}{3} \, \mathrm{d}x = \frac{16}{15}x^{5/4} + C.$$

3.4.
$$\int \frac{2}{5x^{1/3}} \, \mathrm{d}x = \frac{3}{5}x^{2/3} + C.$$

3.5.
$$\int \frac{5}{6y^{-4/3}} \, \mathrm{d}y = \frac{5}{14} y^{7/3} + C.$$

Q5

5.
$$\int e^{2x} \, \mathrm{d}x = \frac{1}{2}e^{2x} + C$$

6.
$$\int -3e^{-3x} \, \mathrm{d}x = e^{-3x} + C$$

7.
$$\int 2e^{11x} \, \mathrm{d}x = \frac{2}{11}e^{11x} + C$$

$$8. \qquad \int \frac{4}{x} \, \mathrm{d}x = 4 \ln|x| + C$$

9.
$$\int -\frac{5}{3x} \, \mathrm{d}x = -\frac{5}{3} \ln|x| + C$$

5.1.
$$\int \cos(x) \, \mathrm{d}x = \sin(x) + C.$$

5.2.
$$\int \sin(2x) \, \mathrm{d}x = -\frac{1}{2} \cos(2x) + C.$$

5.3.
$$\int \frac{5}{6} \cos(x) \, \mathrm{d}x = \frac{5}{6} \sin(x) + C.$$

5.4.
$$\int \cos(3x) \, dx = \frac{1}{3} \sin(3x) + C.$$

5.5.
$$\int \sin\left(\frac{x}{3}\right) dx = -3\cos\left(\frac{x}{3}\right) + C.$$

Answers

Q1

1.1.
$$\int_{1}^{4} 2 \, \mathrm{d}x = 6$$

1.2.
$$\int_{-2}^{2} 3x \, \mathrm{d}x = 0$$

1.4.
$$\int_{2}^{4} 2x^{3} \, \mathrm{d}x = 120$$

Q2

$$2.1. \quad \int_{1}^{27} \frac{4}{\sqrt[3]{x}} \, \mathrm{d}x = 48$$

Q3

3.
$$\int_0^{\ln(3)} 4e^x \, \mathrm{d}x = 8$$

4.
$$\int_0^5 e^{-3x} \, \mathrm{d}x = \frac{1}{3} \left(1 - e^{-15} \right)$$

5.
$$\int_{1}^{2} -4e^{4x} \, \mathrm{d}x = e^{4}(1 - e^{4})$$

6.
$$\int_{1}^{2} \frac{2}{x} \, \mathrm{d}x = 2 \ln(2)$$

7.
$$\int_{1}^{e^3} -\frac{4}{x} \, \mathrm{d}x = -12$$

8.
$$\int_{e^3}^{e^9} \frac{9}{5x} \, \mathrm{d}x = \frac{54}{5}$$

3.1.
$$\int_0^{\pi/2} \sin(x) \, \mathrm{d}x = 1$$

$$3.2. \quad \int_0^\pi \cos(x) \, \mathrm{d}x = 0$$

3.6.
$$\int_0^{\pi/4} \sin(2x) \, \mathrm{d}x = \frac{1}{2}$$

Q4

4.1.
$$\int_0^{\pi/6} \cos(2x) \, \mathrm{d}x = \frac{\sqrt{3}}{4}$$

4.2.
$$\int_{-\pi/4}^{0} \sin(3x) \, \mathrm{d}x = -\frac{1}{3} - \frac{1}{3\sqrt{2}}$$

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