# **Answers: Introduction to matrices**

Jessica Taberner

#### Summary

Answers to a selection of questions on matrices.

These are the answers to [Questions: Introduction to matrices].

Please attempt the questions before reading these answers!

### Q1

### Q1.1

The matrix A has dimension  $2 \times 3$ 

The matrix B has dimension  $2 \times 2$ 

The matrix C has dimension  $3\times 4$ 

The matrix D has dimension  $3 \times 2$ 

The matrix E has dimension  $3 \times 3$ 

The matrix F has dimension  $3\times 3$ 

The matrix G has dimension  $5\times 1$ 

The matrix H has dimension  $4\times 3$ 

#### Q1.2

a. 
$$a_{11} = 2$$

- b.  $g_{41} = 8$
- c.  $d_{12} = -1$
- d.  $f_{32} = 0$
- $\text{e.} \quad b_{21}=3$
- f.  $a_{12} = -1$
- ${\rm g.} \hspace{0.5cm} c_{23}=1$
- h.  $e_{23} = -4$
- $i. \qquad h_{31} = x$
- j.  $h_{13} = 4$
- k.  $e_{32} = -6$
- I.  $g_{11} = -1$

## Q1.3

$$diag A=(2,4)$$

$$diagC=(0,-\sqrt{2},-7)$$

$$diagE=(1,3,7)$$

$$diagG = (-1)$$

Q2

a. 
$$I+J=\begin{bmatrix}2\\5-\sqrt{5}\\8/3\\\pi-\sqrt{7}\end{bmatrix}$$

b. 
$$L-K=\begin{bmatrix} -1+\sqrt{3} & -2 & -1/2 \\ -10 & 6 & -3 \\ 3 & 6 & 10-\pi \end{bmatrix}$$

c. 
$$N+M=\begin{bmatrix} -\pi+1 & -5/4 & 2 & 6 \\ 5 & 1-\sqrt{5} & x+\sqrt{2} & 1 \end{bmatrix}$$

d. 
$$O-P = \begin{bmatrix} 1-\sqrt{3} & 2 \\ 3-\pi & -1 \\ 1 & -6 \end{bmatrix}$$

e. 
$$3I = \begin{bmatrix} 9 \\ -3\sqrt{5} \\ 6 \\ 3\pi \end{bmatrix}$$

f. 
$$-2J = \begin{bmatrix} 2\\ -10\\ -4/3\\ 2\sqrt{7} \end{bmatrix}$$

g. 
$$xK = \begin{bmatrix} x & -2x & 3x \\ 4x & x & -5x \\ 6x & -7x & \pi x \end{bmatrix}$$

h. 
$$-4L = \begin{bmatrix} \sqrt{3} & -4 & 5/2 \\ 24 & -28 & 32 \\ -36 & 4 & -40 \end{bmatrix}$$

i. 
$$yM = \begin{bmatrix} y & -2y & 3y & 4y \\ 5y & -y & \sqrt{2}y & -6y \end{bmatrix}$$

j. 
$$7N = \begin{bmatrix} -7\pi & 21/4 & -7 & 14 \\ 0 & -7\sqrt{5} & 7x & 49 \end{bmatrix}$$

k. 
$$(1/2)O = \begin{bmatrix} 1/2 & -1 \\ 3/2 & 2 \\ -5/2 & 1/2 \end{bmatrix}$$

I. 
$$-4P = \begin{bmatrix} -4\sqrt{3} & 16 \\ -4\pi & -20 \\ 24 & 28 \end{bmatrix}$$

m. 
$$3I + J = \begin{bmatrix} 8 \\ 5 - 3\sqrt{5} \\ 20/3 \\ 3\pi - \sqrt{7} \end{bmatrix}$$

n. 
$$-2(K+L) = \begin{bmatrix} -2-2\sqrt{3} & 12 & -11 \\ 4 & -16 & 26 \\ -30 & 14=2 & -20-2\pi \end{bmatrix}$$

o. 
$$N-4M=\begin{bmatrix} -4-\pi & 35/4 & -13 & -14 \\ -20 & 4-\sqrt{5} & x-4\sqrt{2} & 31 \end{bmatrix}$$

Q3

a. 
$$QR = \begin{bmatrix} 27 + \pi \end{bmatrix}$$

b. 
$$RQ = \begin{vmatrix} -2 & -3 & -1 & -4 \\ 6 & 9 & 3 & 12 \\ 2\pi & 3\pi & \pi & 4\pi \\ 10 & 15 & 5 & 20 \end{vmatrix}$$

c. 
$$ST = \begin{bmatrix} -9 & 30 \\ 13 & 18 \end{bmatrix}$$

d. 
$$TS = \begin{bmatrix} 23 & -34 & 31 \\ 1 & -6 & 33 \\ -24 & 32 & -8 \end{bmatrix}$$

e. 
$$UV = \begin{bmatrix} 6 - \sqrt{2} & 29/2 \\ -12 + 3\sqrt{2} & -59/2 \end{bmatrix}$$

$$\text{f.} \quad VU = \begin{bmatrix} -3/2 - \sqrt{2} & 2 + 2\sqrt{2} \\ 18 & -22 \end{bmatrix}$$

g. 
$$WR = \begin{bmatrix} -3 + 7\pi \\ -45 + 5\pi \\ 44 + 3\sqrt{7} - 8\pi \end{bmatrix}$$

h. 
$$SW = \begin{bmatrix} -1 & 7 + 5\sqrt{7} & -48 & 57 + \pi \\ 11 & -13 - \sqrt{7} & 22 & -33 - 3\pi \end{bmatrix}$$

i. 
$$TU = \begin{bmatrix} -23 & 34 \\ -1 & 6 \\ 24 & -32 \end{bmatrix}$$

j. 
$$TV = \begin{bmatrix} 18 - 5\sqrt{2} & -89/2 \\ 6 + 7\sqrt{2} & 21/2 \\ 24 & 56 \end{bmatrix}$$

k. 
$$TX = \begin{bmatrix} 17\\29\\4 \end{bmatrix}$$

I. 
$$UX = \begin{bmatrix} -3\\10 \end{bmatrix}$$

$$\text{m.} \quad VX = \begin{bmatrix} -1/4 + 4\sqrt{2} \\ 31/2 \end{bmatrix}$$

n. 
$$XQ = \begin{bmatrix} -8 & 12 & 4 & 16 \\ 1 & 3/2 & 1/2 & 2 \end{bmatrix}$$

o. 
$$VV = \begin{bmatrix} 1/2 & -7/2 - \sqrt{2}/2 \\ 21 + 3\sqrt{2} & 95/2 \end{bmatrix}$$

p. 
$$UU = \begin{bmatrix} 7 & -10 \\ -15 & 22 \end{bmatrix}$$

q. 
$$UXQ = \begin{bmatrix} -6 & -9 & -3 & -12 \\ 20 & 30 & 10 & 40 \end{bmatrix}$$

$$\mathbf{r.} \quad U^3 = \begin{bmatrix} -37 & 54 \\ 81 & -118 \end{bmatrix}$$

s. 
$$STU = \begin{bmatrix} 99 & -138 \\ 41 & -46 \end{bmatrix}$$

t. 
$$TXQR = \begin{bmatrix} 459 + 17\pi \\ 783 + 29\pi \\ 108 + 4\pi \end{bmatrix}$$

$$u. \quad 3UX = \begin{bmatrix} -18 \\ 60 \end{bmatrix}$$

v. 
$$(ST)-2U=\begin{bmatrix} -11 & 26\\ 7 & 10 \end{bmatrix}$$

w. 
$$WR + TX = \begin{bmatrix} 14 + 7\pi \\ -16 + 5\pi \\ 18 + 3\sqrt{7} - 8\pi \end{bmatrix}$$

x. 
$$-RQR = \begin{bmatrix} 27 + \pi \\ -81 - 3\pi \\ -27\pi + \pi^2 \\ 135 + 5\pi \end{bmatrix}$$

y. 
$$(V+U)X = \begin{bmatrix} -5 - 3\sqrt{2} \\ 61 \end{bmatrix}$$

z. 
$$4U^2+V^2=\begin{bmatrix} 57/2 & -87/2-\sqrt{2}/2\\ -39+3\sqrt{2} & 271/2 \end{bmatrix}$$

### Version history

 $v1.0\colon$  initial version created 04/25 by Jessica Taberner as part of a University of St Andrews VIP project.

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