

# Regression and practical advice

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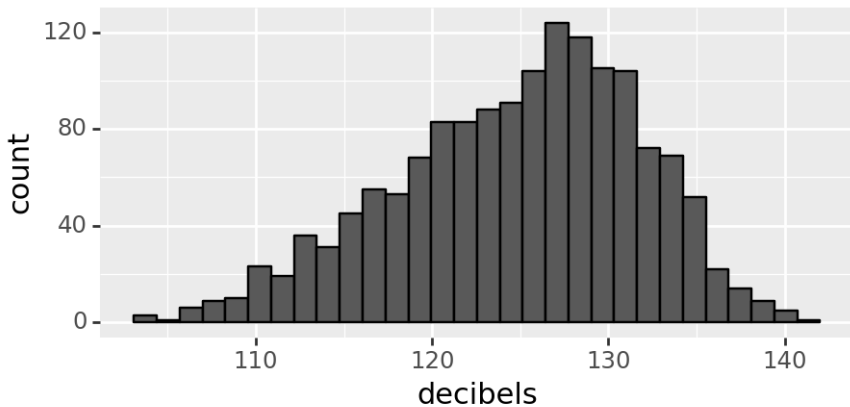
# Supervised machine learning

- ▶ Goal is to learn a function  $f(\mathbf{x}) = y$  where  $\mathbf{x} \in \mathbb{R}^p$  is an input/feature vector and  $y$  is an output/label.
- ▶ This week we will study linear models and neural networks for regression, meaning labels represented by  $y \in \mathbb{R}$  is a real number.
- ▶ air foil self-noise data:  $\mathbf{x}$  = Frequency (Hertz), Angle of attack (degrees), Chord length (meters), Free-stream velocity (meters per second),  $y \in \mathbb{R}$  Scaled sound pressure level, in decibels.
- ▶ forest fires data:  $\mathbf{x}$  = meteorological and other data,  $y \in \mathbb{R}_+$  burned area.
- ▶ some practical advice for getting gradient descent learning to work better (scaling, log transform, feature transform)

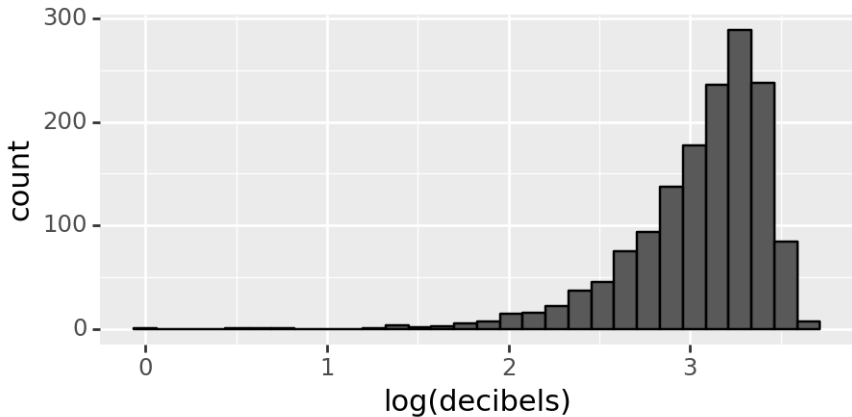
## air foil self-noise

```
##      Hertz  degrees  ...      meters  decibels
## 0         800      0.0  ...    0.002663   126.201
## 1        1000      0.0  ...    0.002663   125.201
## 2        1250      0.0  ...    0.002663   125.951
## 3        1600      0.0  ...    0.002663   127.591
## 4        2000      0.0  ...    0.002663   127.461
## ...      ...      ...  ...      ...      ...
## 1498      2500     15.6  ...    0.052849   110.264
## 1499      3150     15.6  ...    0.052849   109.254
## 1500      4000     15.6  ...    0.052849   106.604
## 1501      5000     15.6  ...    0.052849   106.224
## 1502      6300     15.6  ...    0.052849   104.204
##
## [1503 rows x 6 columns]
```

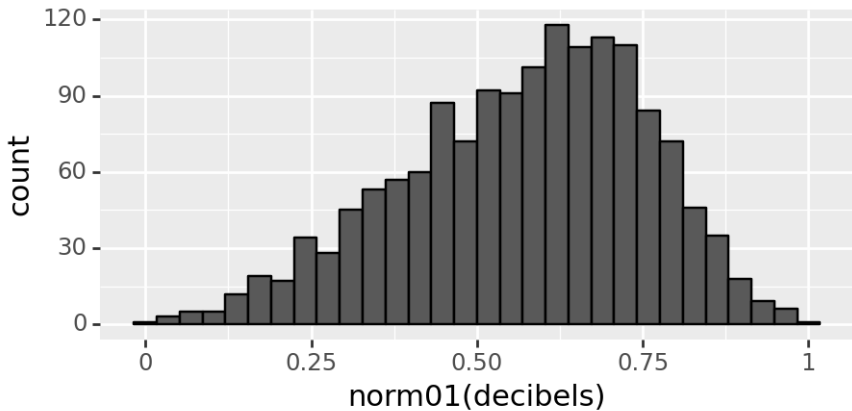
Labels in data=air\_foil



Labels in data=air\_foil

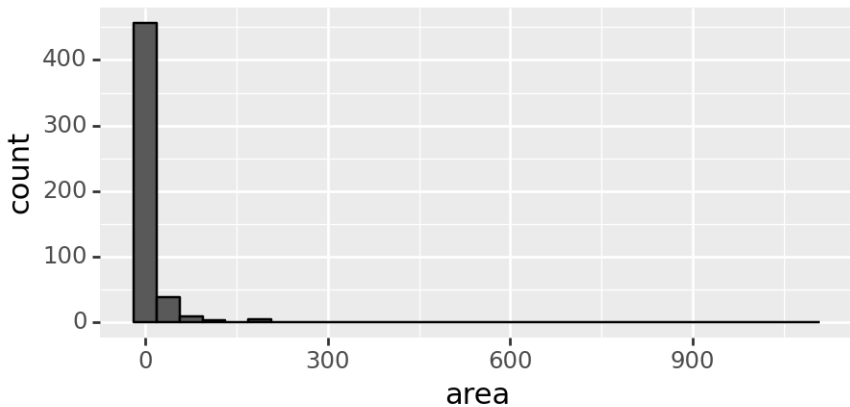


Labels in data=air\_foil



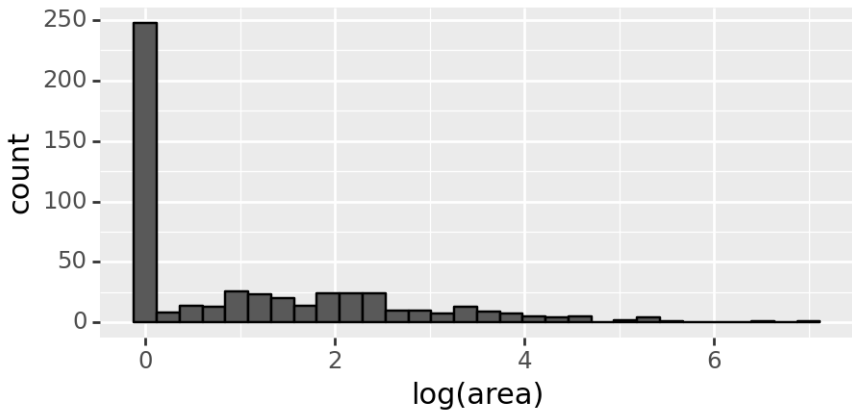
```
##      X  Y month ... wind  rain   area
## 0    7  5  mar ...  6.7   0.0   0.00
## 1    7  4  oct ...  0.9   0.0   0.00
## 2    7  4  oct ...  1.3   0.0   0.00
## 3    8  6  mar ...  4.0   0.2   0.00
## 4    8  6  mar ...  1.8   0.0   0.00
## ..  ..  ..  ...  ...  ...   ...
## 512  4  3  aug ...  2.7   0.0   6.44
## 513  2  4  aug ...  5.8   0.0  54.29
## 514  7  4  aug ...  6.7   0.0  11.16
## 515  1  4  aug ...  4.0   0.0   0.00
## 516  6  3  nov ...  4.5   0.0   0.00
##
## [517 rows x 13 columns]
```

Labels in data=forest\_fires

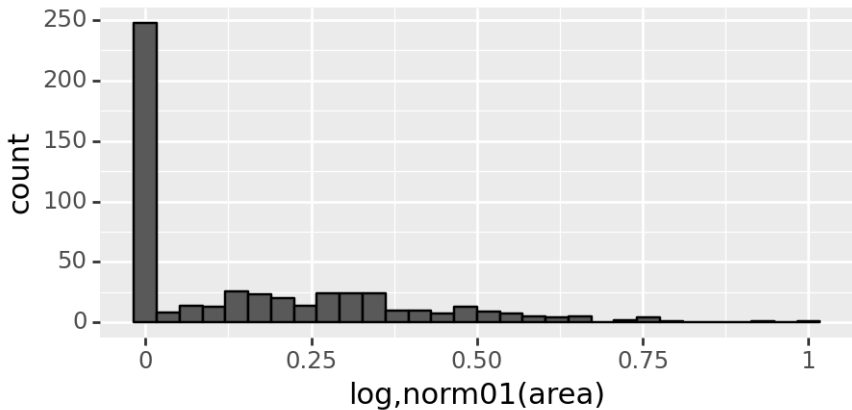




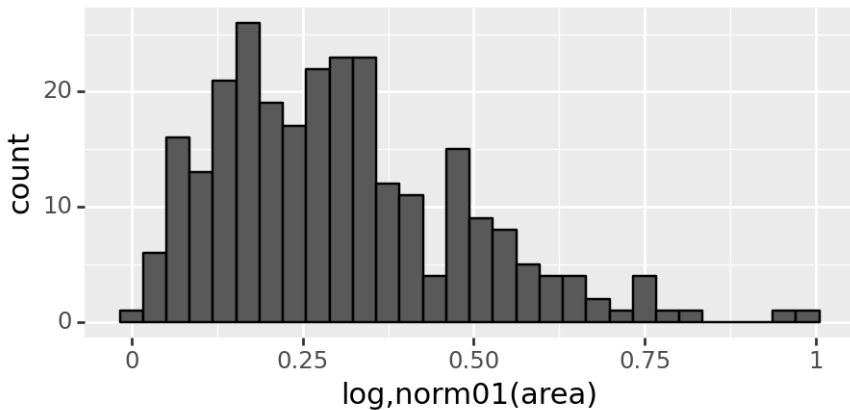
Labels in data=forest\_fires



Labels in data=forest\_fires



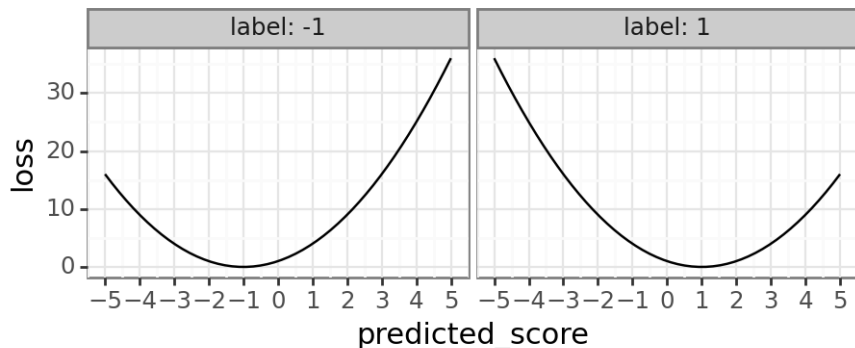
Labels in data=forest\_fires, zeros excluded



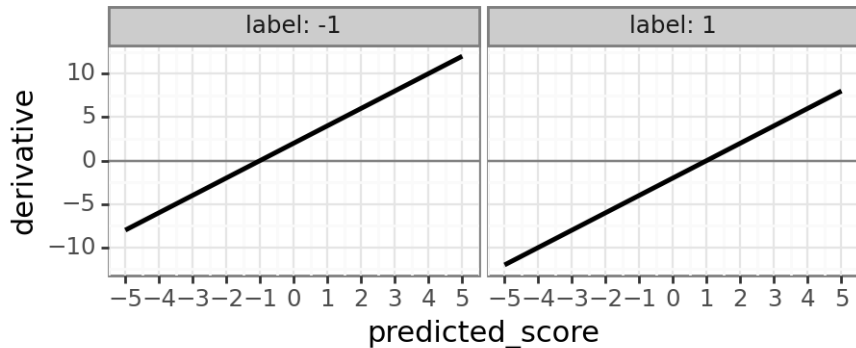
TODO angle to sin/cos

## How are the neural network weights learned?

- ▶ Typically we use some version of gradient descent.
- ▶ This algorithm requires definition of a differentiable loss function to minimize on the train set.
- ▶ For regression problems ( $y \in \mathbb{R}$ ) we use the square loss,  $\ell[f(\mathbf{x}), y] = [f(\mathbf{x}) - y]^2$ .



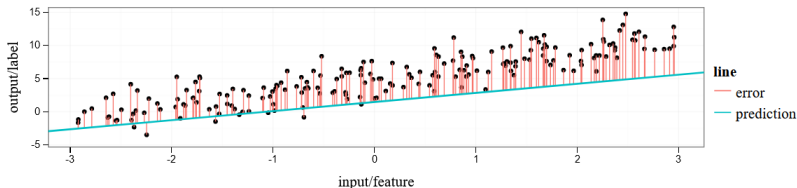
## Visualization of square loss gradient/derivative



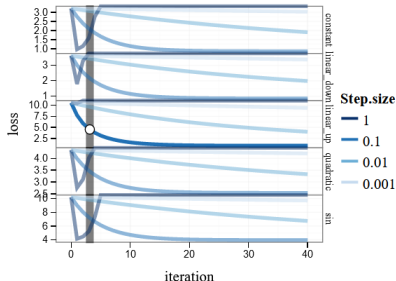
# Interactive visualization of gradient descent for regression

<http://ml.nau.edu/viz/2022-02-02-gradient-descent-regression/>

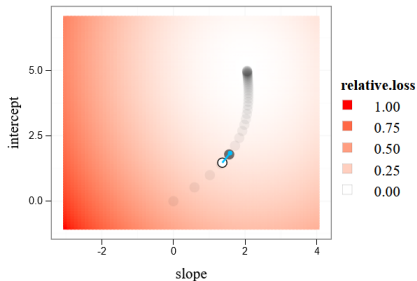
Data and regression model



Loss, select iteration/data/step size



Optimization variables, select iteration



## Possible exam questions

► TODO