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# Comparing binsegRcpp with other implementations of binary segmentation for changepoint detection

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#### Abstract

Binary segmentation is a classic algorithm for detecting changepoints in sequential data. In theory it should be extremely fast for N data and K segments, O(NK) in the worst case, and  $O(N\log K)$  in the best case. In practice existing implementations such as ruptures (Python module) and changepoint (R package) are much slower, and in fact sometimes do not return a correct result. We present the R package binsegRcpp, which provides an efficient C++ implementation of binary segmentation, and always returns correct results. We discuss some advanced C++ coding techniques which were used to avoid repetition, for efficiency, and for readability. We additionally include detailed theoretical and empirical comparisons with other implementations of binary segmentation in R packages fpop, blockcpd and wbs.

Keywords: JSS, style guide, comma-separated, not capitalized, R.

## 1. Introduction: Count data regression in R

The introduction is in principle "as usual". However, it should usually embed both the implemented *methods* and the *software* into the respective relevant literature. For the latter both competing and complementary software should be discussed (within the same software environment and beyond), bringing out relative (dis)advantages. All software mentioned should be properly \cite{}d. (See also Appendix B for more details on BibTeX.)

For writing about software JSS requires authors to use the markup \proglang{} (programming languages and large programmable systems), \pkg{} (software packages), \code{} (functions, commands, arguments, etc.). If there is such markup in (sub)section titles (as above), a plain text version has to be provided in the LATEX command as well. Below we also illustrate how abbrevations should be introduced and citation commands can be employed. See the LATEX code for more details.

TODO (Standard Template Library containers, virtual classes, static variables, function pointers, templates, macros).

TODO fpop::multiBinSeg (Maidstone, Hocking, Rigaill, and Fearnhead 2017).

TODO wbs::sbs (Baranowski and Fryzlewicz 2019).

TODO changepoint::cpt.mean(method="BinSeg") (Killick and Eckley 2014; Killick, Haynes, and Eckley 2022).

TODO ruptures.Binseg (Truong, Oudre, and Vayatis 2020).

#### 2. Models and software

The basic Poisson regression model for count data is a special case of the GLM framework McCullagh and Nelder (1989). It describes the dependence of a count response variable  $y_i$  (i = 1, ..., n) by assuming a Poisson distribution  $y_i \sim \text{Pois}(\mu_i)$ . The dependence of the conditional mean  $\mathsf{E}[y_i \mid x_i] = \mu_i$  on the regressors  $x_i$  is then specified via a log link and a linear predictor

$$\log(\mu_i) = x_i^{\top} \beta, \tag{1}$$

where the regression coefficients  $\beta$  are estimated by maximum likelihood (ML) using the iterative weighted least squares (IWLS) algorithm.

Note that around the {equation} above there should be no spaces (avoided in the LATEX code by % lines) so that "normal" spacing is used and not a new paragraph started.

R provides a very flexible implementation of the general GLM framework in the function glm() (Chambers and Hastie 1992) in the stats package. Its most important arguments are

```
glm(formula, data, subset, na.action, weights, offset,
  family = gaussian, start = NULL, control = glm.control(...),
  model = TRUE, y = TRUE, x = FALSE, ...)
```

where formula plus data is the now standard way of specifying regression relationships in R/S introduced in Chambers and Hastie (1992). The remaining arguments in the first line (subset, na.action, weights, and offset) are also standard for setting up formula-based regression models in R/S. The arguments in the second line control aspects specific to GLMs while the arguments in the last line specify which components are returned in the fitted model object (of class 'glm' which inherits from 'lm'). For further arguments to glm() (including alternative specifications of starting values) see ?glm. For estimating a Poisson model family = poisson has to be specified.

As the synopsis above is a code listing that is not meant to be executed, one can use either the dedicated {Code} environment or a simple {verbatim} environment for this. Again, spaces before and after should be avoided.

Finally, there might be a reference to a {table} such as Table 1. Usually, these are placed at the top of the page ([t!]), centered (\centering), with a caption below the table, column headers and captions in sentence style, and if possible avoiding vertical lines.

package	binsegRcpp	changepoint	wbs	fpop	ruptures
function	binseg	cpt.mean	$\operatorname{sbs}$	multiBinSeg	Binseg
version	2022.3.29	2.2.3	1.4	2019.8.26	1.1.6
weights	yes	no	no	no	no
$\max segs$	yes	yes	no	yes	yes
$\dim$	one	one	one	$\operatorname{multi}$	$\operatorname{multi}$
correct	yes	no	yes	yes	no
losses	C++	$\mathbf{C}$	L2	L2	Python
storage	STL multiset	arrays	recursion	heap	LRU cache
space	O(S)	$O(S^2)$	O(S)	O(S)	O(S)
cumsum	yes	yes	yes	yes	no
best	$O(N \log N)$	$O(N^3)$	$O(N \log N)$	$O(N \log N)$	$> O(N \log N)$
worst	$O(N^2)$	$O(N^3)$	$O(N^2)$	$O(N^2)$	$O(N^2)$
CV	yes	no	no	no	no
params	yes	largest	no	no	no

Table 1: TODO

case/splits:	one		best/equal		worst/unequal	
operation:	insert	argmin	insert	argmin	insert	argmin
list	O(1)	O(n)	$O(S \log S)$	O(S)	O(S)	O(S)
heap/multiset	$O(\log n)$	O(1)	O(S)	$O(S^2)$	O(S)	O(S)
Find new split		$O(N \log S)$ $O(NS)$			$\overline{NS}$	

Table 2: container properties

Loss computation. We run each algorithm on N.data points up to max.segments = max.changes+1. binsegRcpp::binseg result is a list which contains a data table with max.segments rows and column loss that is the square loss. changepoint::cpt.mean result is a list of class cpt.range with method logLik which returns the square loss of one of the models. wbs::sbs result is a list which contains a data frame with N.data-1 rows and CUSUM and min.th columns TODO.fpop::multiBinSeg result is a list with element J.est, which is a vector of max.changes square loss decrease values. ruptures.Binseg.predict result is a vector of segment ends for one model size, which can be passed to sum\_of\_costs method to compute the square loss.

Three packages have implemented the normal change in mean and variance model. binsegRcpp::binseg loss values are the normal negative log likelihood (NLL). The changepoint::logLik function returns two times the NLL. The ruptures.Binseg loss is related via this equation,

$$NLL = (rupturesLoss + N[1 + log(2\pi)])/2$$
 (2)

#### 3. Illustrations

For a simple illustration of basic Poisson and NB count regression the quine data from the MASS package is used. This provides the number of Days that children were absent from school in Australia in a particular year, along with several covariates that can be employed

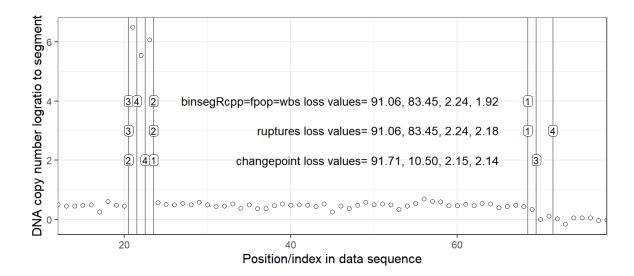


Figure 1: For a real cancer DNA copy number data set with 273 observations, we show the first four changepoints detected by several different implementations of binary segmentation.

as regressors. The data can be loaded by

and a basic frequency distribution of the response variable is displayed in Figure ??.

For code input and output, the style files provide dedicated environments. Either the "agnostic" {CodeInput} and {CodeOutput} can be used or, equivalently, the environments {Sinput} and {Soutput} as produced by Sweave() or knitr when using the render\_sweave() hook. Please make sure that all code is properly spaced, e.g., using y = a + b \* x and not y=a+b\*x. Moreover, code input should use "the usual" command prompt in the respective software system. For R code, the prompt "R> " should be used with "+ " as the continuation prompt. Generally, comments within the code chunks should be avoided – and made in the regular LATEX text instead. Finally, empty lines before and after code input/output should be avoided (see above).

As a first model for the quine data, we fit the basic Poisson regression model. (Note that JSS prefers when the second line of code is indented by two spaces.)

To account for potential overdispersion we also consider a negative binomial GLM.

```
R> library("MASS")
R> m_nbin <- glm.nb(Days ~ (Eth + Sex + Age + Lrn)^2, data = quine)</pre>
```

In a comparison with the BIC the latter model is clearly preferred.

```
R> BIC(m_pois, m_nbin)
```

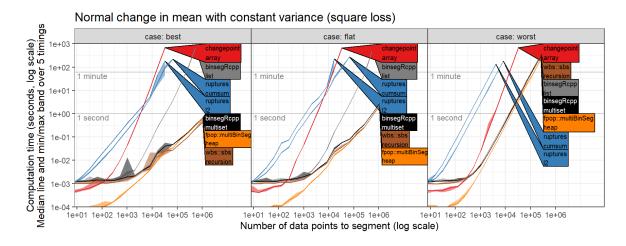


Figure 2: Timings using square loss.

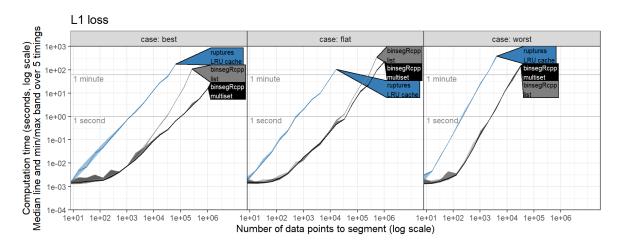


Figure 3: Timings using L1 loss.

```
df BIC
m_pois 18 2046.851
m_nbin 19 1157.235
```

Hence, the full summary of that model is shown below.

```
R> summary(m_nbin)
```

#### Call:

```
glm.nb(formula = Days ~ (Eth + Sex + Age + Lrn)^2, data = quine,
  init.theta = 1.60364105, link = log)
```

#### Deviance Residuals:

```
Min 1Q Median 3Q Max -3.0857 -0.8306 -0.2620 0.4282 2.0898
```

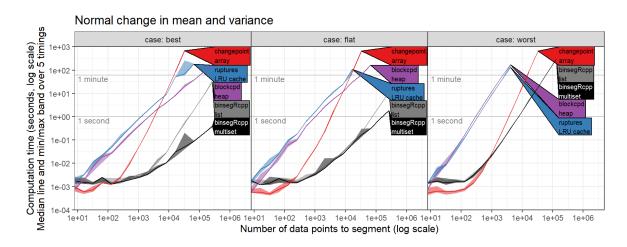


Figure 4: Timings using Gaussian change in mean and variance model.

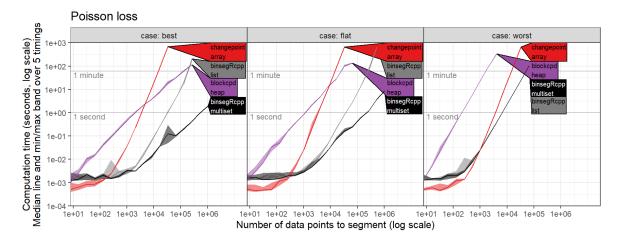


Figure 5: Timings using Poisson loss.

s: (1 not	defined be	cause of	singularities)
${\tt Estimate}$	Std. Error	z value	Pr(> z )
3.00155	0.33709	8.904	< 2e-16 ***
-0.24591	0.39135	-0.628	0.52977
-0.77181	0.38021	-2.030	0.04236 *
-0.02546	0.41615	-0.061	0.95121
-0.54884	0.54393	-1.009	0.31296
-0.25735	0.40558	-0.635	0.52574
0.38919	0.48421	0.804	0.42153
0.36240	0.29430	1.231	0.21818
-0.70000	0.43646	-1.604	0.10876
-1.23283	0.42962	-2.870	0.00411 **
0.04721	0.44883	0.105	0.91622
0.06847	0.34040	0.201	0.84059
	Estimate 3.00155 -0.24591 -0.77181 -0.02546 -0.54884 -0.25735 0.38919 0.36240 -0.70000 -1.23283 0.04721	Estimate Std. Error 3.00155 0.33709 -0.24591 0.39135 -0.77181 0.38021 -0.02546 0.41615 -0.54884 0.54393 -0.25735 0.40558 0.38919 0.48421 0.36240 0.29430 -0.70000 0.43646 -1.23283 0.42962 0.04721 0.44883	-0.24591       0.39135       -0.628         -0.77181       0.38021       -2.030         -0.02546       0.41615       -0.061         -0.54884       0.54393       -1.009         -0.25735       0.40558       -0.635         0.38919       0.48421       0.804         0.36240       0.29430       1.231         -0.70000       0.43646       -1.604         -1.23283       0.42962       -2.870         0.04721       0.44883       0.105

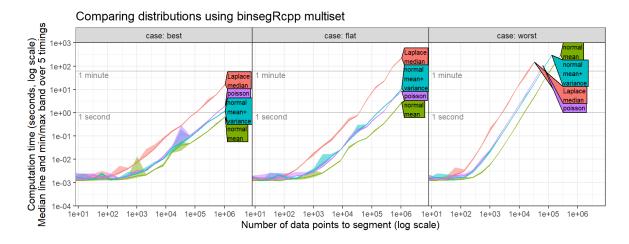


Figure 6: Timings using binsegRcpp multiset with several different loss functions.

```
SexM:AgeF1
             0.02257
                        0.47360
                                          0.96198
                                   0.048
SexM:AgeF2
             1.55330
                        0.51325
                                   3.026
                                          0.00247 **
SexM:AgeF3
             1.25227
                        0.45539
                                   2.750
                                          0.00596 **
SexM:LrnSL
             0.07187
                        0.40805
                                   0.176
                                          0.86019
AgeF1:LrnSL -0.43101
                        0.47948
                                  -0.899
                                          0.36870
AgeF2:LrnSL
                        0.48567
                                          0.28363
             0.52074
                                   1.072
AgeF3:LrnSL
                  NA
                              NA
                                      NA
                                               NΑ
```

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for Negative Binomial (1.6036) family taken to be 1)

Null deviance: 235.23 on 145 degrees of freedom Residual deviance: 167.53 on 128 degrees of freedom

AIC: 1100.5

Number of Fisher Scoring iterations: 1

Theta: 1.604 Std. Err.: 0.214

2 x log-likelihood: -1062.546

#### 4. Summary and discussion

As usual ...

#### Computational details

If necessary or useful, information about certain computational details such as version numbers, operating systems, or compilers could be included in an unnumbered section. Also, auxiliary packages (say, for visualizations, maps, tables, ...) that are not cited in the main text can be credited here.

The results in this paper were obtained using R 4.2.1 with the MASS 7.3.57 package. R itself and all packages used are available from the Comprehensive R Archive Network (CRAN) at https://CRAN.R-project.org/.

#### Acknowledgments

All acknowledgments (note the AE spelling) should be collected in this unnumbered section before the references. It may contain the usual information about funding and feedback from colleagues/reviewers/etc. Furthermore, information such as relative contributions of the authors may be added here (if any).

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#### A. More technical details

Appendices can be included after the bibliography (with a page break). Each section within the appendix should have a proper section title (rather than just Appendix).

For more technical style details, please check out JSS's style FAQ at https://www.jstatsoft.org/pages/view/style#frequently-asked-questions which includes the following topics:

- Title vs. sentence case.
- Graphics formatting.
- Naming conventions.
- Turning JSS manuscripts into R package vignettes.
- Trouble shooting.
- Many other potentially helpful details...

## B. Using BibTeX

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Cleaning up BibTeX files is a somewhat tedious task – especially when acquiring the entries automatically from mixed online sources. However, it is important that informations are complete and presented in a consistent style to avoid confusions. JSS requires the following format.

- JSS-specific markup (\proglang, \pkg, \code) should be used in the references.
- Titles should be in title case.
- Journal titles should not be abbreviated and in title case.
- DOIs should be included where available.
- Software should be properly cited as well. For R packages citation("pkgname") typically provides a good starting point.

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