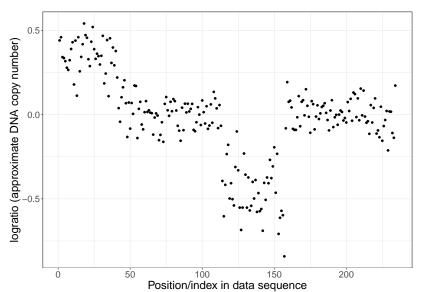
Segmentation model selection and evaluation

Toby Dylan Hocking

Background: detecting abrupt changes is important

Example from cancer diagnosis: breakpoints are associated with aggressive disease in neuroblastoma.



Motivation for segmentation model selection and evaluation

- ▶ In each of the segmentation models we have studied, there is a choice of model size (segments/changepoints or hidden states).
- ► Too large model sizes result in false positives (changepoints predicted by algorithm but they are not significant/real).
- ➤ Too small model sizes result in false negatives (no changepoint predicted where there should be).
- Want to maximize true positive rate (number of correctly predicted changepoints) and true negative rate (number of correct predicted regions without changepoints).

Model selection via Classic Information Criteria

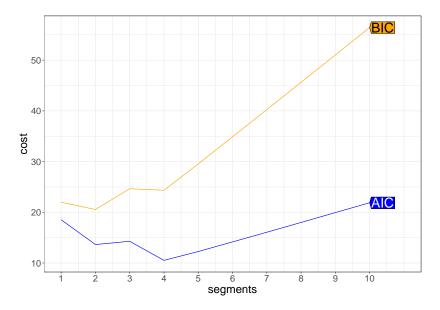
For every model size $k \in \{1, ..., K\}$ let L_k be the loss.

Information criteria choose the model which minimizes the penalized cost, for some non-negative penalty $\lambda \geq 0$,

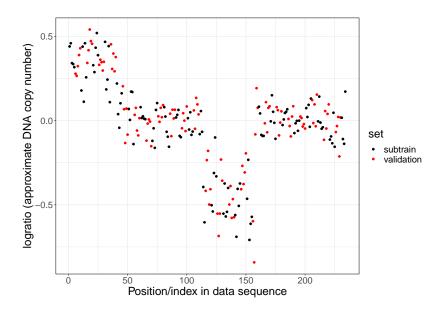
$$C_k = \min_{k \in \{1, \dots, K\}} L_k + \lambda k$$

- ▶ BIC=Bayesian Information Criterion, sometimes referred to as SIC=Schwarz who was the author. $\lambda = \log n$ where n is the number of data points.
- ▶ AIC=Akaike Information Criterion: $\lambda = 2$.
- Data viz: http://bl.ocks.org/tdhock/raw/43ac9c6be9188dcb02a7/

Model selection criteria plot for binary segmentation



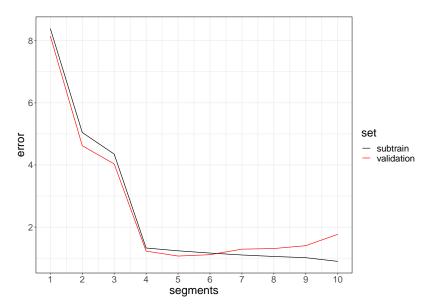
Cross-validation for model selection



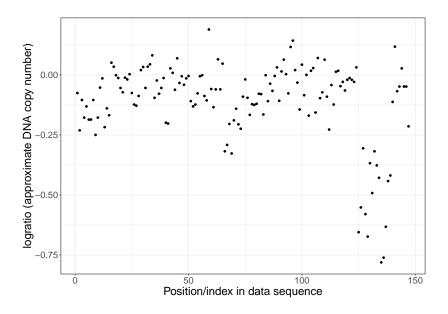
Idea for cross-validation

- Divide full data sequence into subtrain and validation sets.
- Use subtrain data as input to learning algorithm.
- Use validation data to choose best model size (min error or negative log likelihood).
- As model size increases, subtrain error should always decrease, whereas validation error should be U shaped.

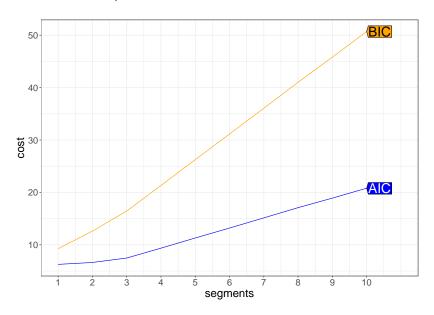
CV Error plot



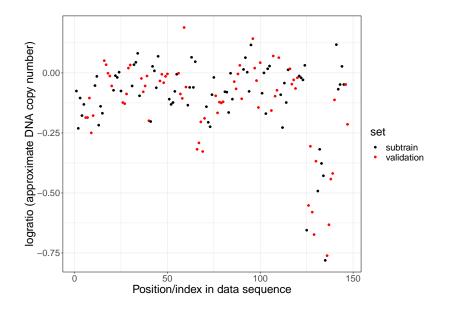
Another data set



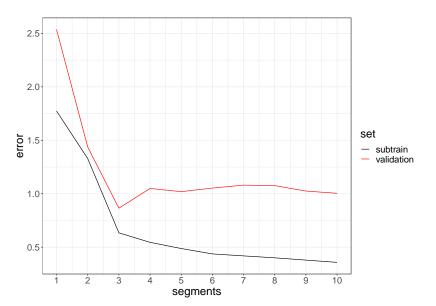
Model selection plot



Cross-validation for model selection



CV error plot



Labeled regions for evaluating accuracy of changepoint predictions

TODO

Possible exam questions

TODO