

$$F(a, b, c, d) = \sum m(0, 1, 2, 3, 4, 5, 6, 8, 10) + d(11, 12)$$

cd \ ab	00	01	11	10
00	1	1	1	1
01	1	1	0	1
11	-	0	0	0
10	1	0	-	1

+6

PI	EPI
$\bar{a} \bar{d}$	$\bar{a} \bar{c}$
$\bar{a} \bar{c}$	$\bar{a} \bar{d}$
$\bar{a} \bar{b}$	
$\bar{b} c$	
$\bar{c} \bar{d}$	
$\bar{b} \bar{d}$	

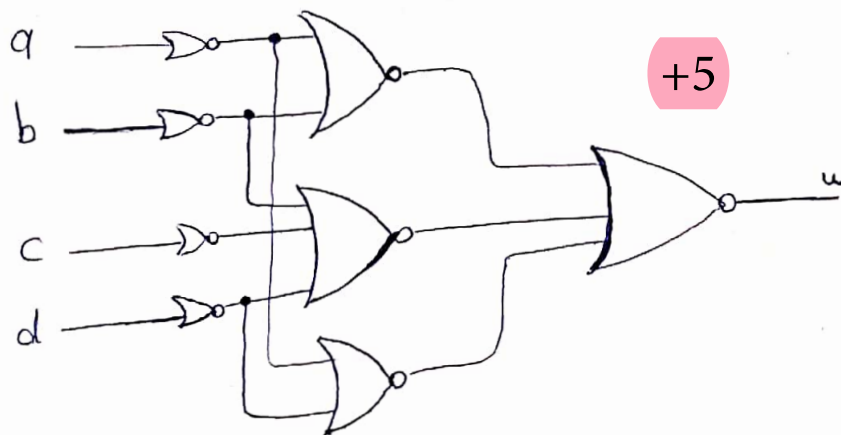
+2

$$SOP = \bar{a} \bar{c} + \bar{a} \bar{d} + \bar{b} c + \begin{matrix} \bar{c} \bar{d} \\ \bar{b} \bar{d} \end{matrix} + 4$$

-2 for missed other form of F

$$POS = (\bar{a} + \bar{b})(\bar{b} + \bar{c} + \bar{d})(\bar{a} + \bar{d})$$

مرب POS ← NOR مبر



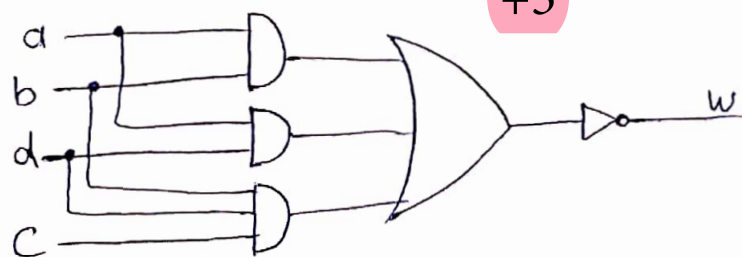
+5

AND-OR-INV

$$\bar{F} = \sum m(7, 9, 13, 14, 15) + d(11, 12)$$

cd \ ab	00	01	11	10
00				
01			1	
11	-	1	1	1
10		1	-	

$$SOP = ab + ad + bcd$$



+5

$$f = \sum m(0, 1, 2, 3, 4, 5, 6, 8, 10) + d(11, 12)$$

✓0	0000
✓1	0001
✓2	0010
✓4	0100
✓8	1000
✓3	0011
✓5	0101
✓6	0110
✓10	1010
✓12	1100
11	1011

✓000-	(0,1)
✓00-0	(0,2)
✓0-00	(0,4)
✓-000	(0,8)
✓00-1	(1,3)
✓0-01	(1,5)
✓001-	(2,3)
✓0-10	(2,6)
✓-010	(2,10)
✓010-	(4,5)
✓01-0	(4,6)
✓-100	(4,12)
✓10-0	(8,10)
✓1-00	(8,12)
✓-011	(3,11)
✓101-	(10,11)

✓00--	(0,1,2,3)
✓0-0-	(0,1,4,5)
✓00--	(0,2,1,3)
✓0--0	(0,2,4,6)
✓0-0-	(0,1,4,5)
✓0--0	(0,2,4,6)
✓--00	(0,4,8,12)
✓-0-0	(0,2,8,10)
✓-0-0	(0,2,8,10)
✓--00	(0,4,8,12)
✓-01-	(2,10,3,11)
✓-01-	(2,3,10,11)

+8

$$PI: \bar{a}\bar{b}, \bar{a}\bar{c}, \bar{a}\bar{d}, \bar{c}\bar{d}, \bar{b}\bar{d}, \bar{b}\bar{c}$$

+6

m _i	0	1	2	3	4	5	6	8	10
PI									
$\bar{a}\bar{b}$	x	x	x	x					
$\bar{a}\bar{c}$	x	x			x	x			
$\bar{a}\bar{d}$	x		x		x	x			
$\bar{c}\bar{d}$	x				x			x	
$\bar{b}\bar{d}$	x		x					x	x
$\bar{b}\bar{c}$			x	x					x
	✓	✓	✓		✓	✓	✓		

$$EPI = \bar{a}\bar{c} + \bar{a}\bar{d}$$

+6

$$SOP = \bar{a}\bar{c} + \bar{a}\bar{d} + \bar{b}\bar{c} + \bar{c}\bar{d}$$

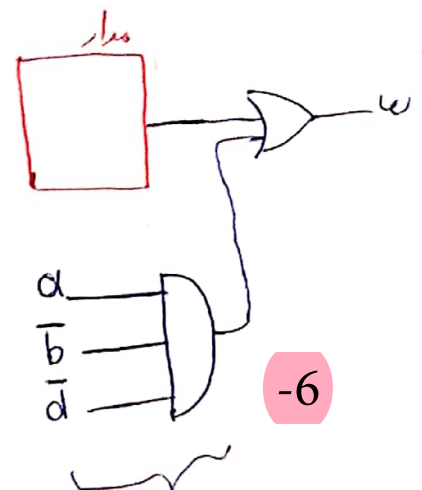
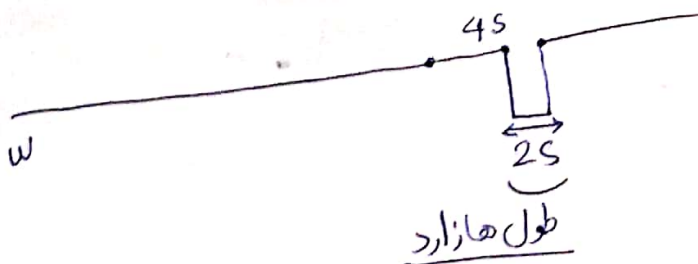
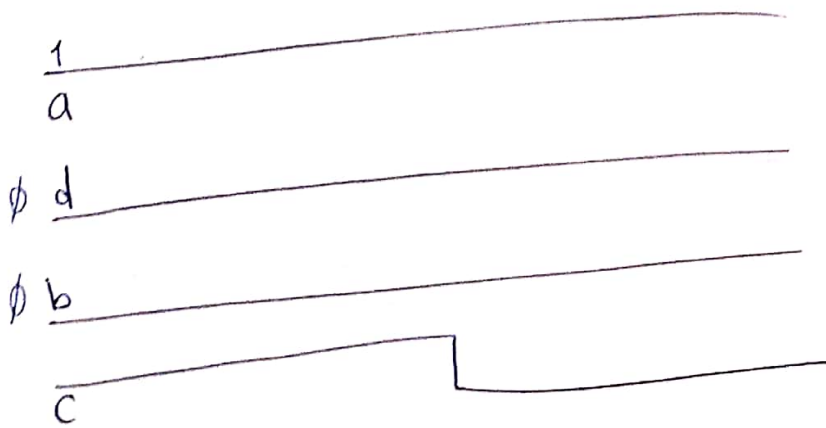
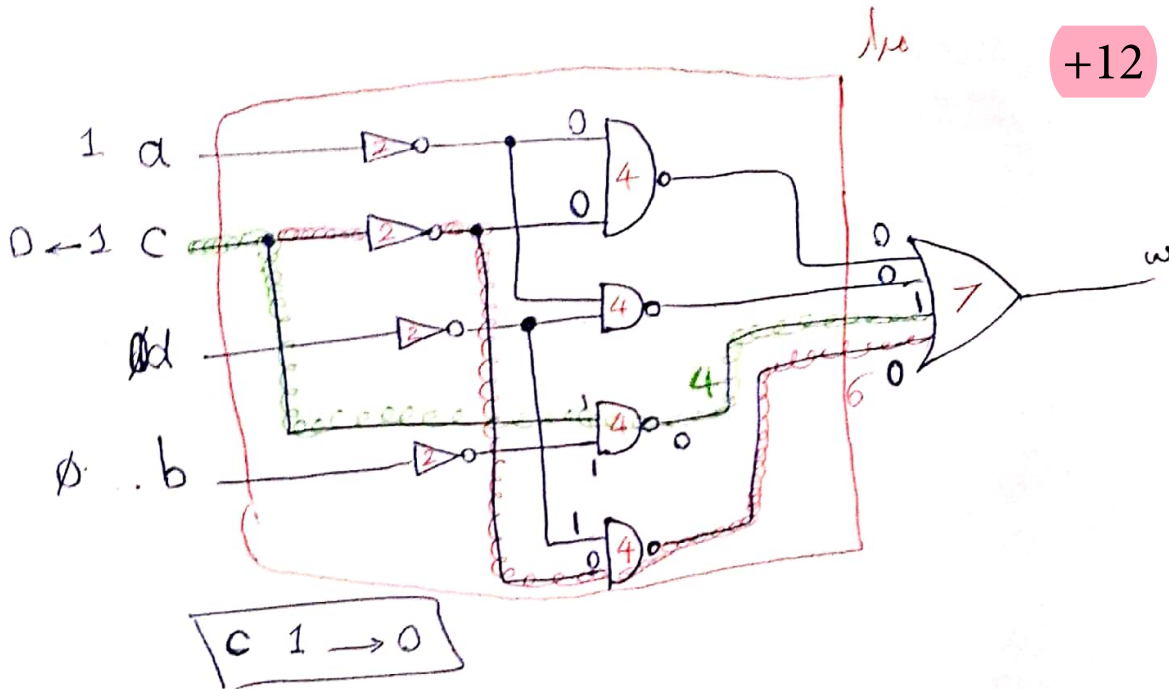
$$SOP: \bar{a}\bar{c} + \bar{a}\bar{d} + \bar{b}c + \bar{c}\bar{d}$$

cd \ ab	00	01	11	10
00	1	1	1	1
01	1	1		1
11	-			
10	1		-	1

$$0001 \leftrightarrow 0011$$

$$1000 \leftrightarrow 1010$$

} potential Hazard



گیت اضافی برای رفع هازارد
با به تغیر گرفتن میزوم $a\bar{b}\bar{d}$